

The Isotropic Diffusion Source Approximation for Multi-D Supernova Simulations

“also with FLASH”

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The Basel Supernova Group:

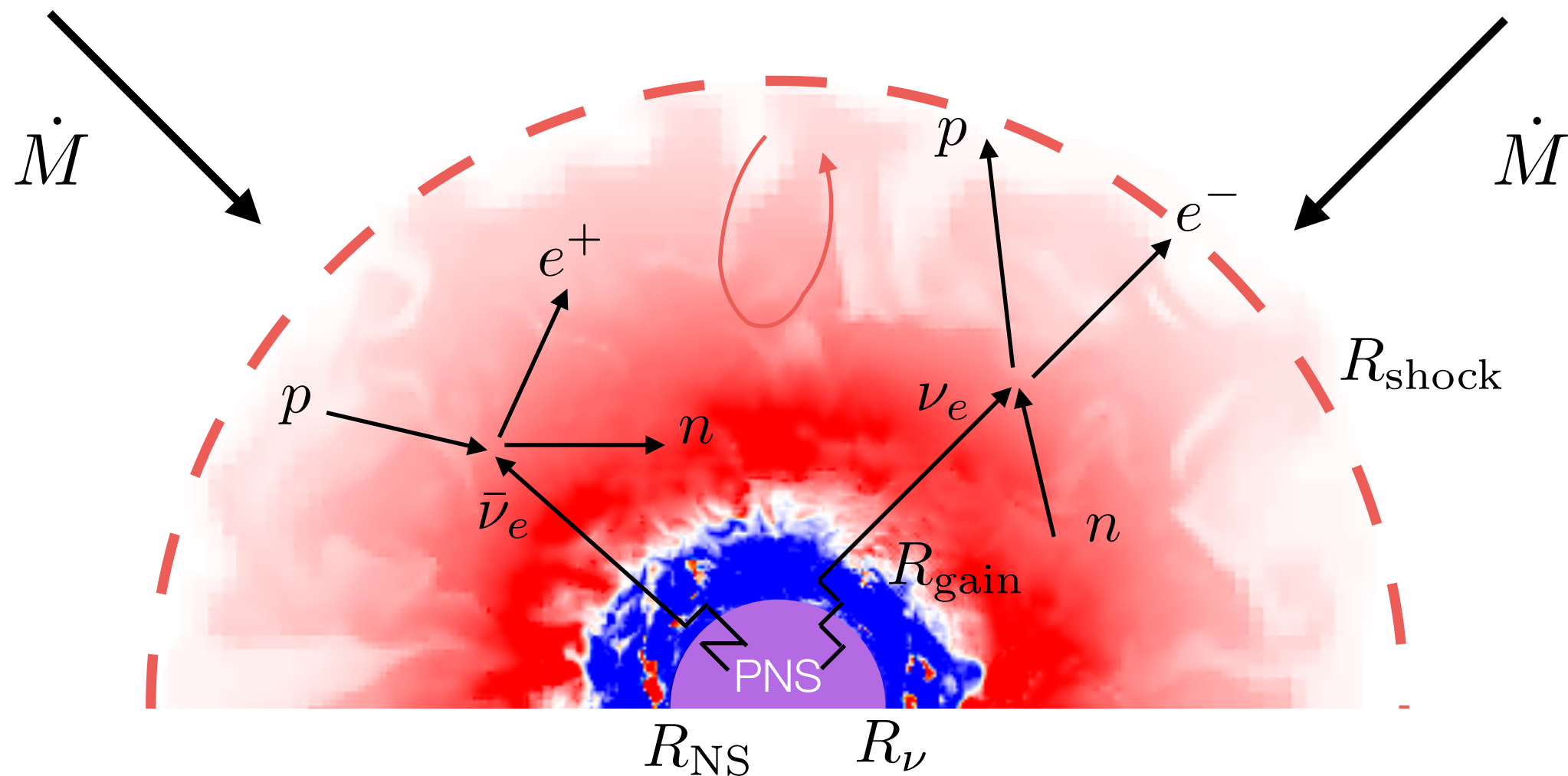
Friedrich-Karl Thielemann
Marius Eichler
Matthias Hempel
Oliver Heinemann
Andreas Lohs

Matthias Liebendörfer
Takami Kuroda
Rubén Cabezón
Kevin Ebinger



Basic Physics

- ▶ Direct hydrodynamics mechanism always fail!
- ▶ Neutrino-driven convection is the key



Adapted from Janka 01

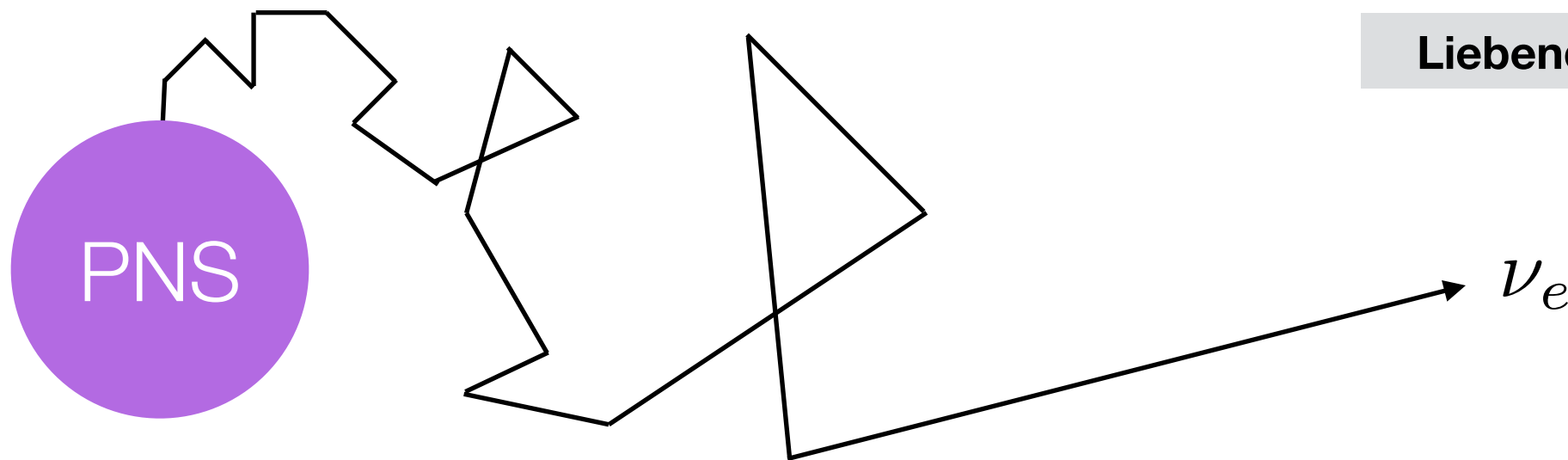
Isotropic Diffusion Source Approximation (IDSA)

IDSA (Liebendorfer+ 09)

$$f_l = f_l^t + f_l^s$$

$$D(f_l^t) = C_l^t - \Sigma_l$$

$$D(f_l^s) = C_l^s + \Sigma_l$$



Liebendorfer+ 09

Opaque

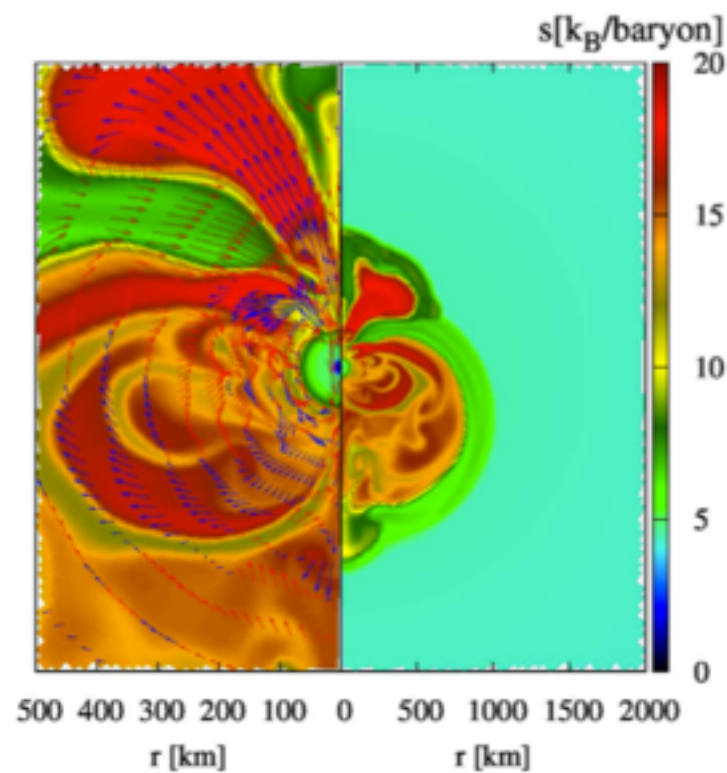
Semi-transparent

Transparent

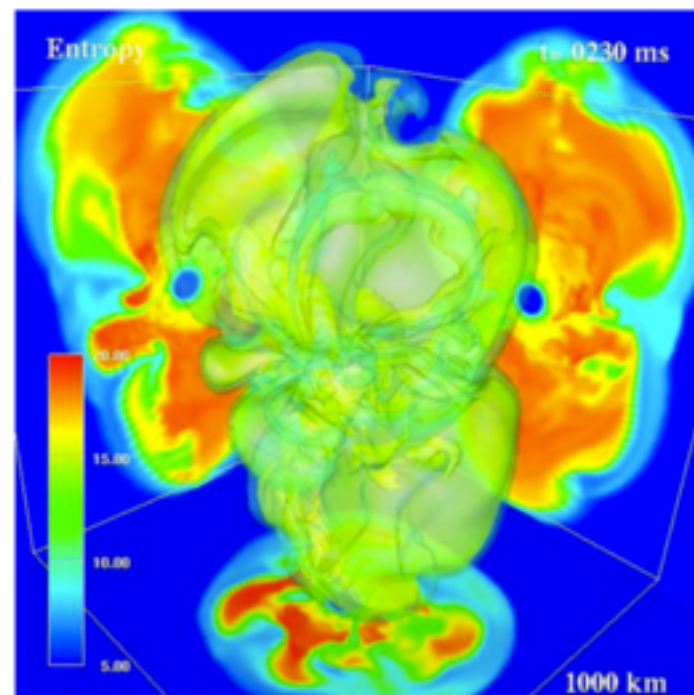
Multi-D Simulations with IDSA

- ▶ Multi-dimensional simulations with the IDSA have been studied by the Nippon groups
- ▶ ZEUS+IDSA in spherical coordinates with Ray-by-Ray approach

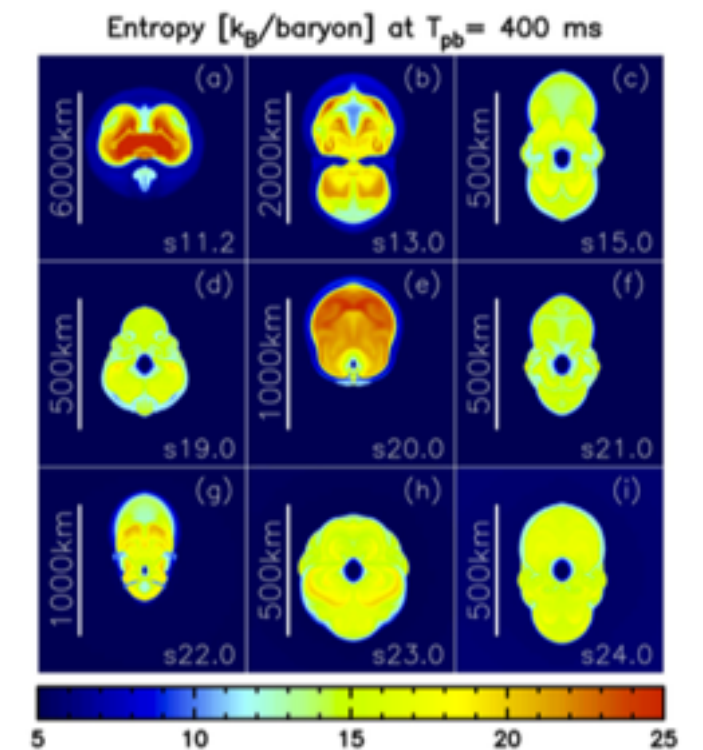
Suwa+ 13



Takiwaki+ 14



Nakamura+ 14



Multi-D IDSA with FLASH

$$f_l = f_l^t + f_l^s$$

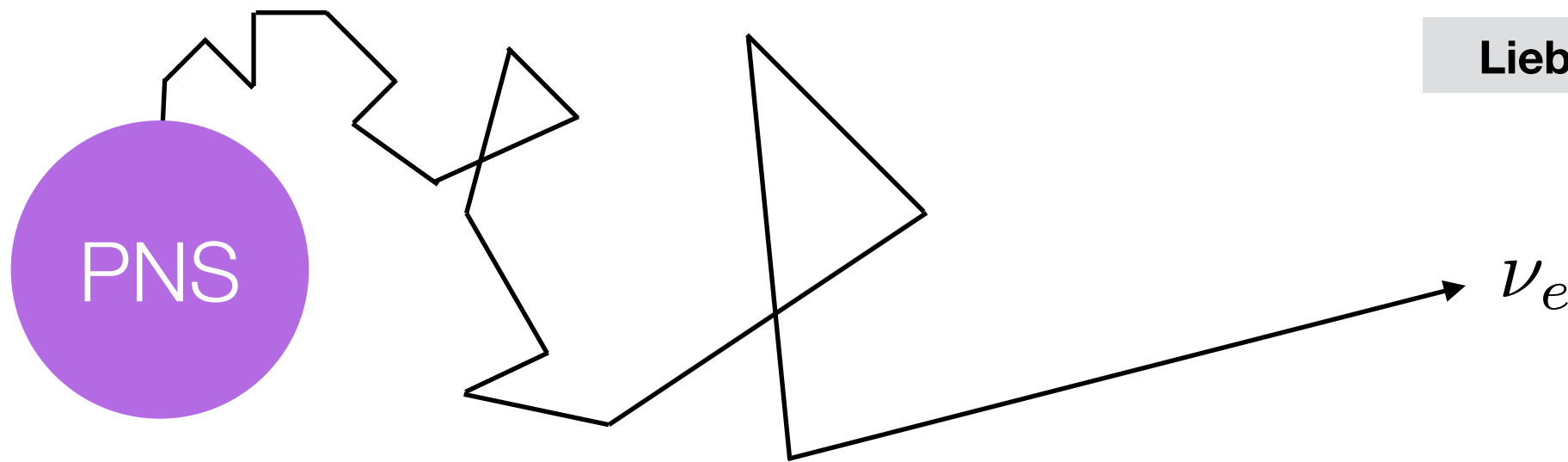
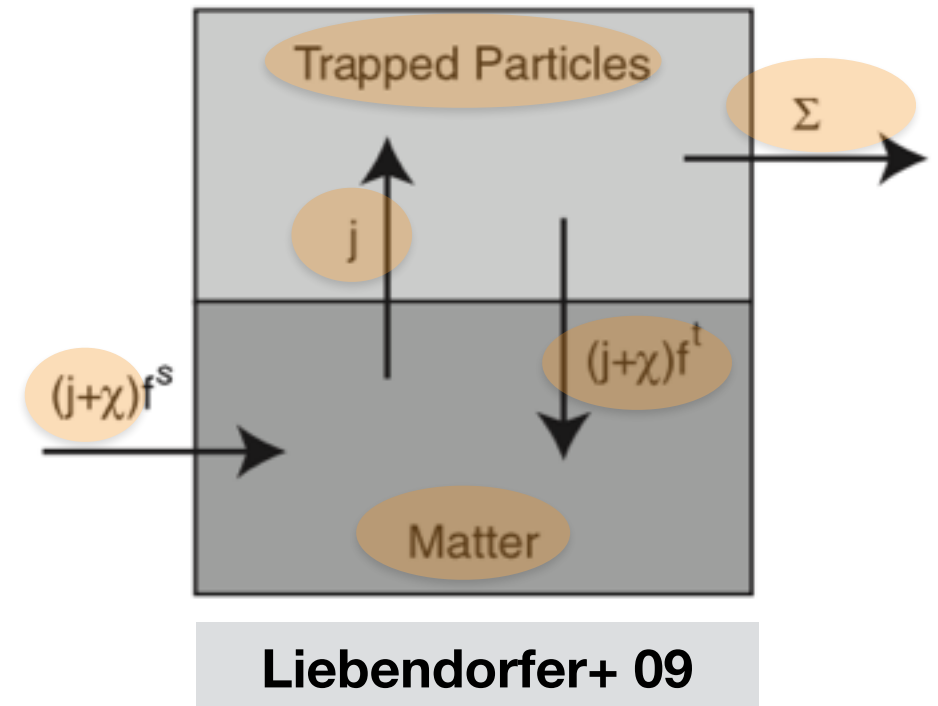
$$D(f_l^t) = C_l^t - \Sigma_l$$

$$D(f_l^s) = C_l^s + \Sigma_l$$

Spherical Symmetry:

$$R_\nu(E, l)$$

$$f^s(E, l)$$



Opaque

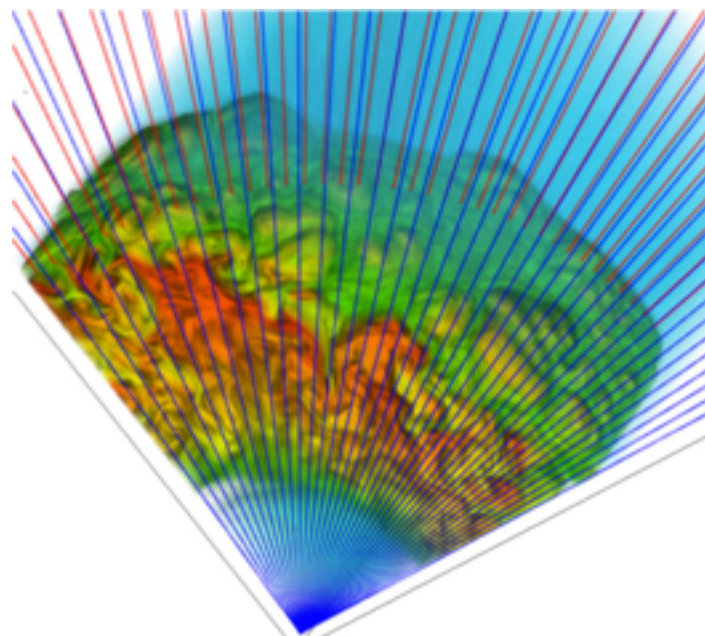
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Transparent

FLASH+IDSA

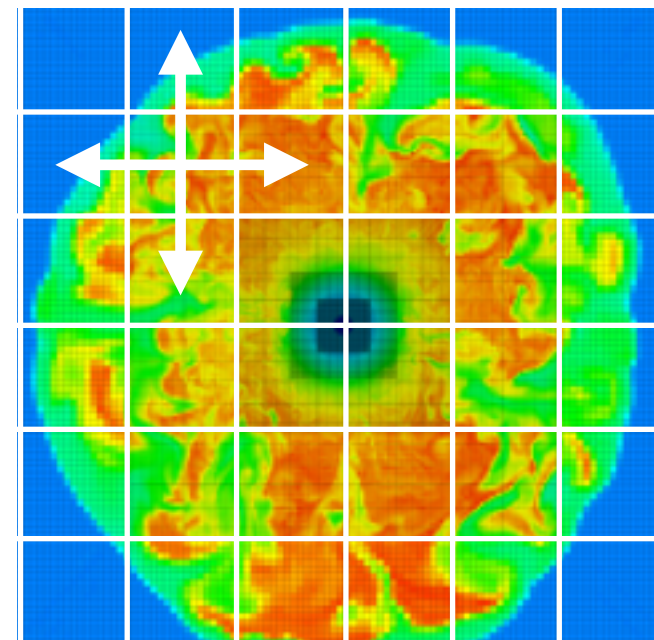
- ▶ 2D cylindrical and 3D Cartesian coordinates with AMR: better PNS but noisy
- ▶ Not “Ray-by-Ray” approach. We solve the diffusion source and trapped particle component in multi-dimensions, but keep the streaming component in spherical symmetry (Similar to the Elephant code)
- ▶ 20 energy bins from 3 MeV to 300 MeV
- ▶ Only for electron type neutrinos (Heavy neutrinos -> Leakage scheme)

Ray-by-Ray



Ott+ 12

Full 3D



This work

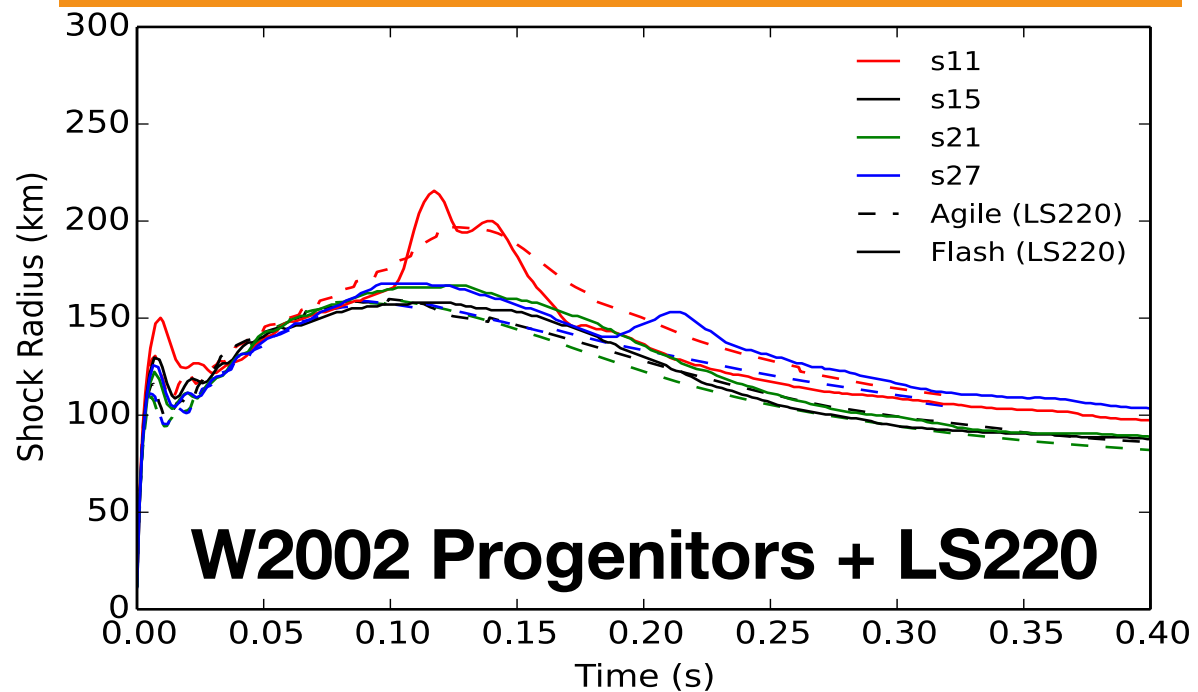
The FLASH code (v4.2.2)

Code Status:

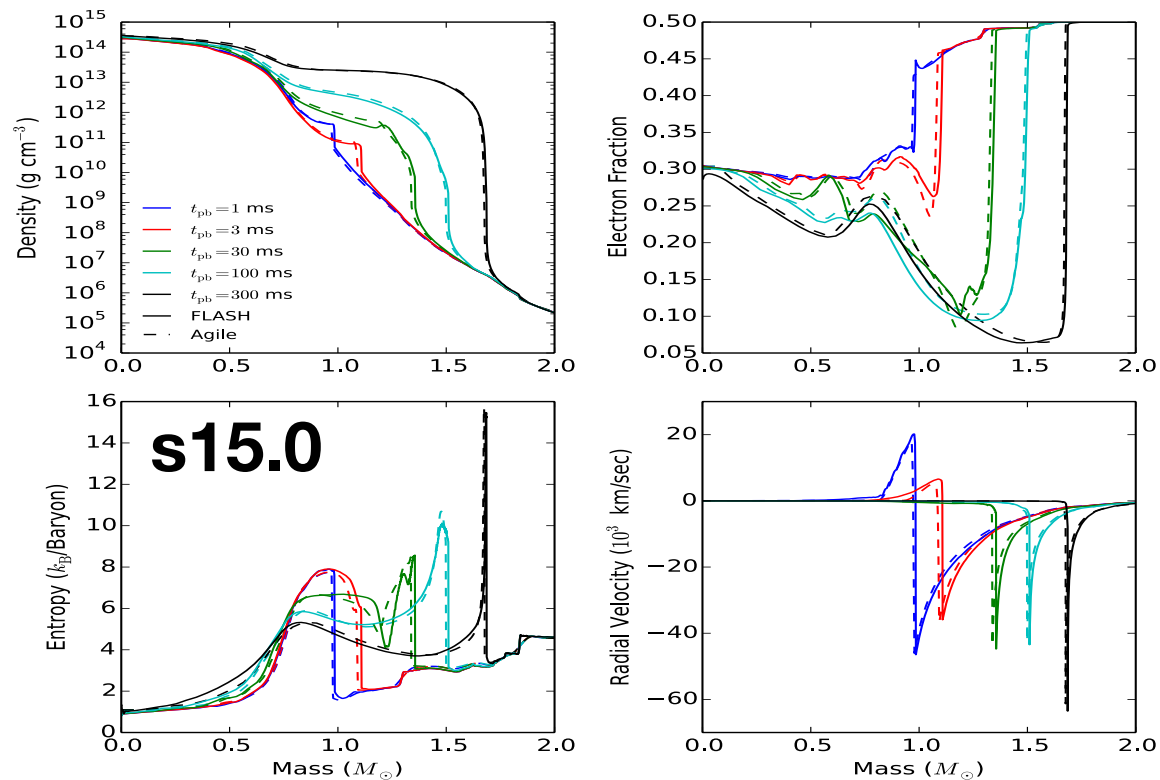
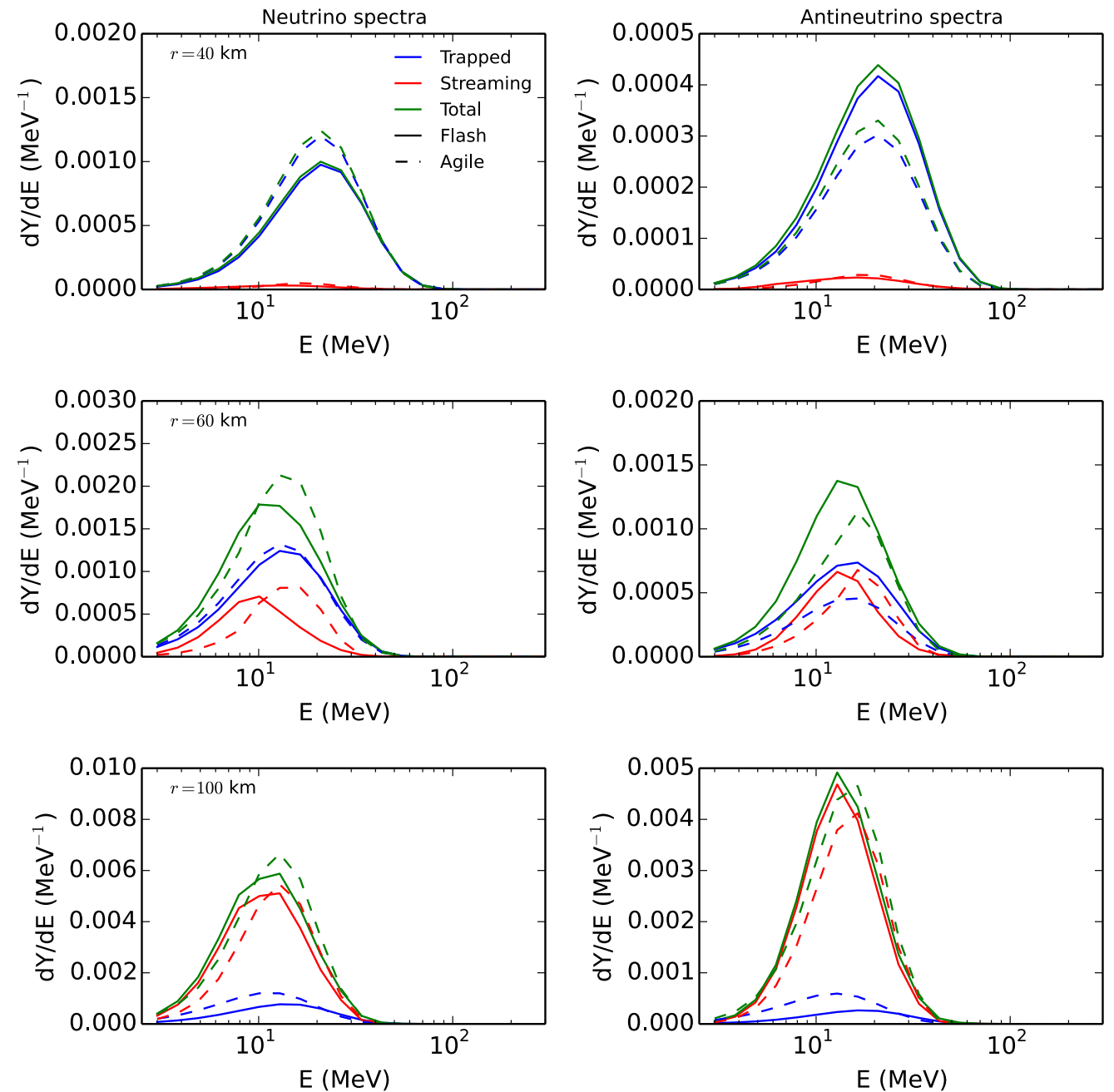
- ▶ **Geometry:** 1D spherical, 2D cylindrical, and 3D Cartesian (Similar to Couch+13)
- ▶ **Hydrodynamics:** 3rd PPM with HLLC Riemann solver with AMR
- ▶ **Resolution:** effective angular resolution (2D: $\sim 0.3-0.6^\circ$, 3D: $\sim 1-2^\circ$)
- ▶ **Simulation box:** $r=0$ to $r=10,000$ km
- ▶ **Gravity:** The new improved multi-pole solver (Couch+13; Newtonian or eff. GR)
- ▶ **EoS:** Supernova EoS from <http://stellarcollapse.org>
- ▶ **Neutrino transport:** Isotropic Diffusion Source Approximation (IDSA)
 - ▶ Collapse: **IDSA** or parametrized deleptonization (**PD**; Liebendorfer+05)
 - ▶ Postbounce: IDSA (Liebendorfer+09)

1D Code Comparison: FLASH v.s. AGILE

Shock Radius

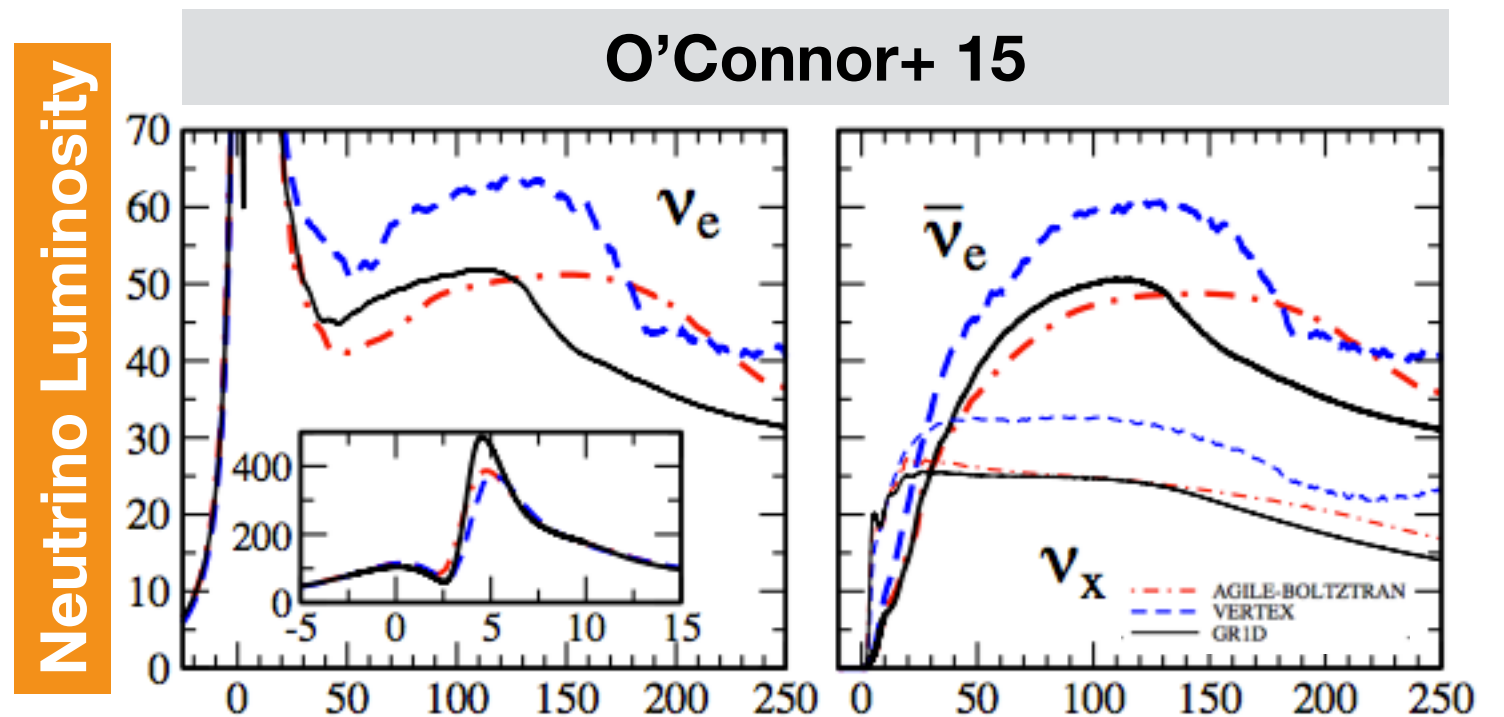
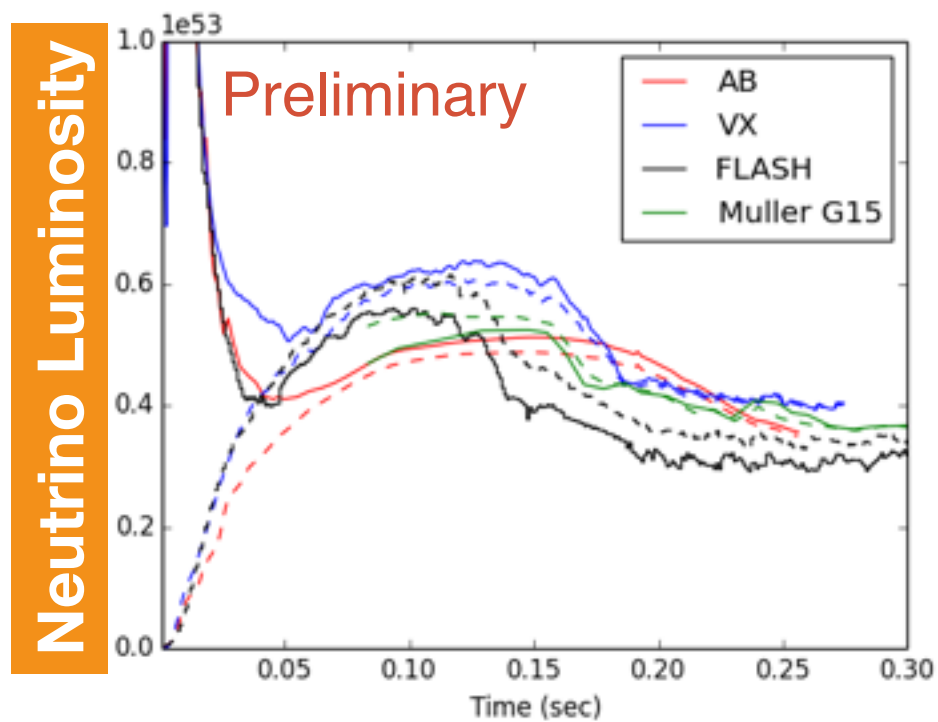
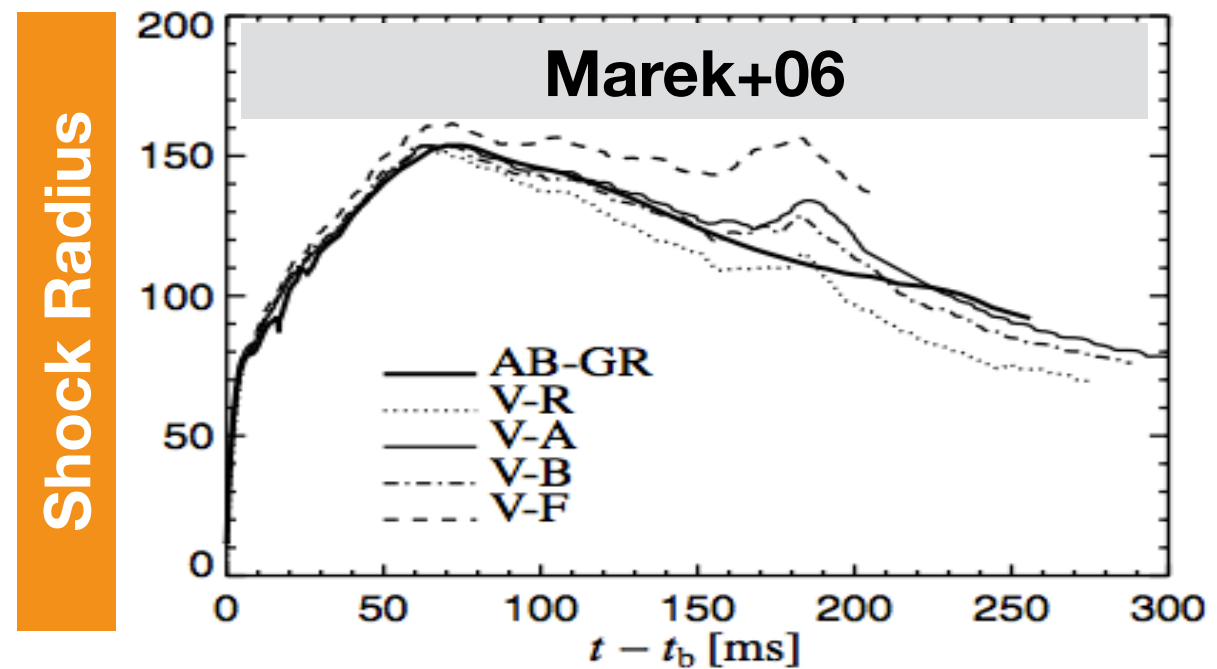
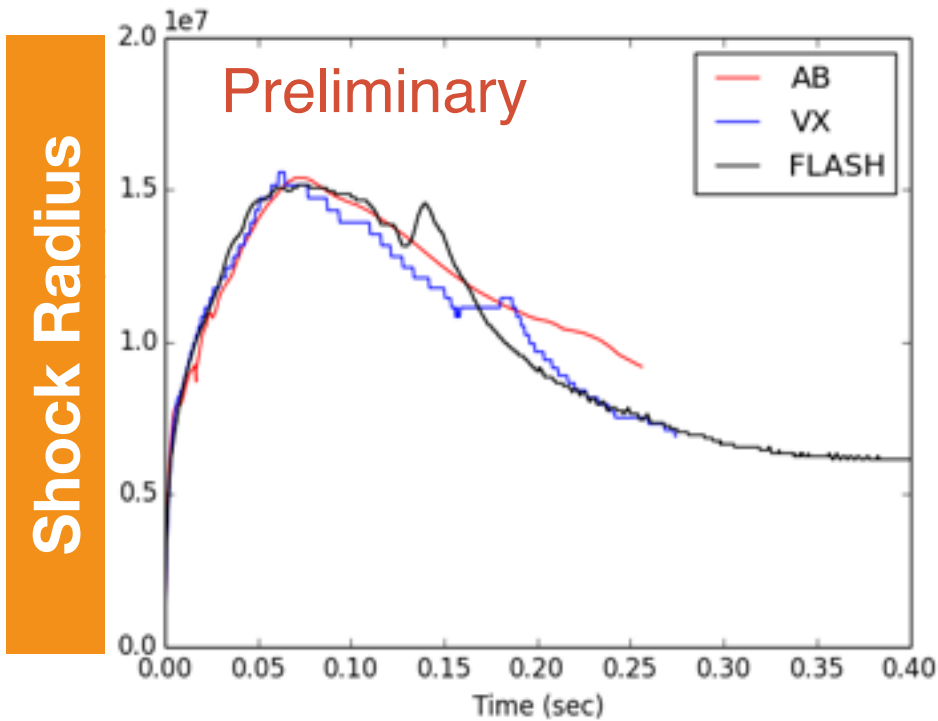


Neutrino Spectra



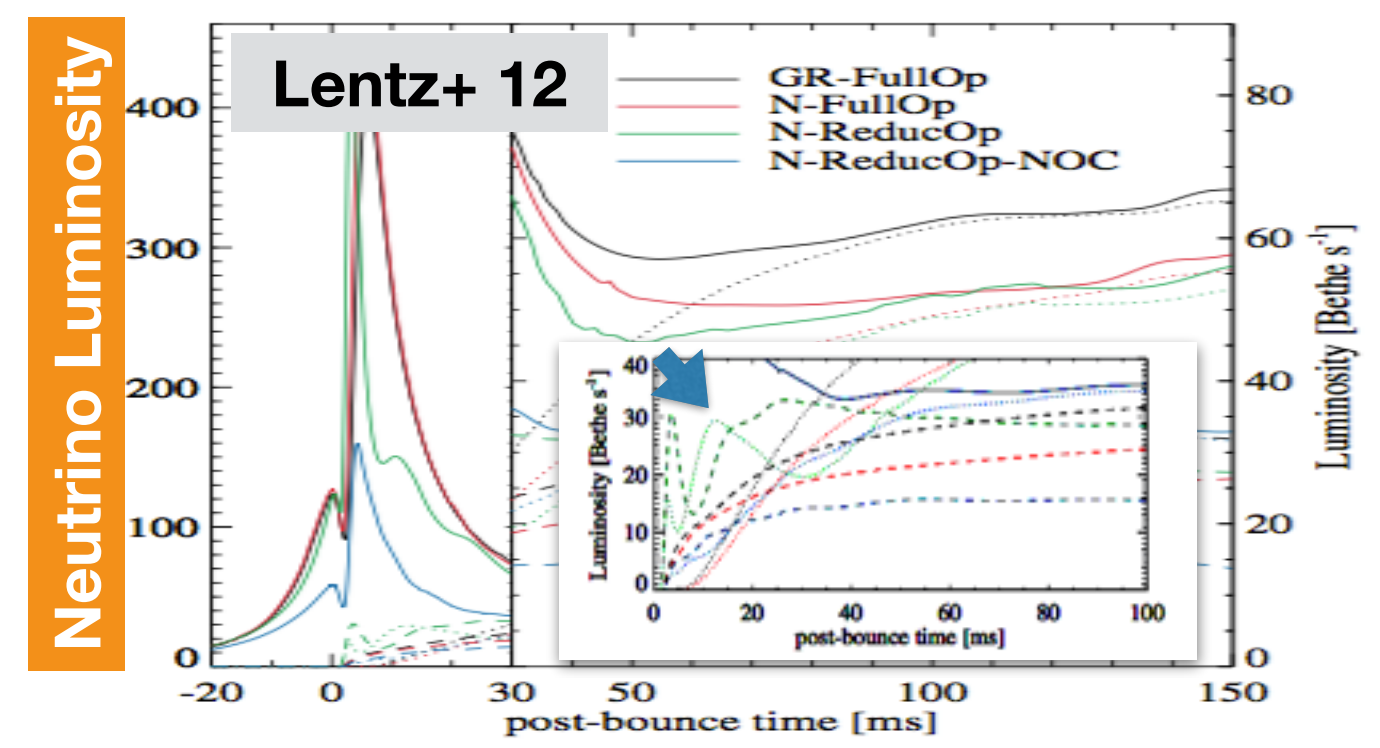
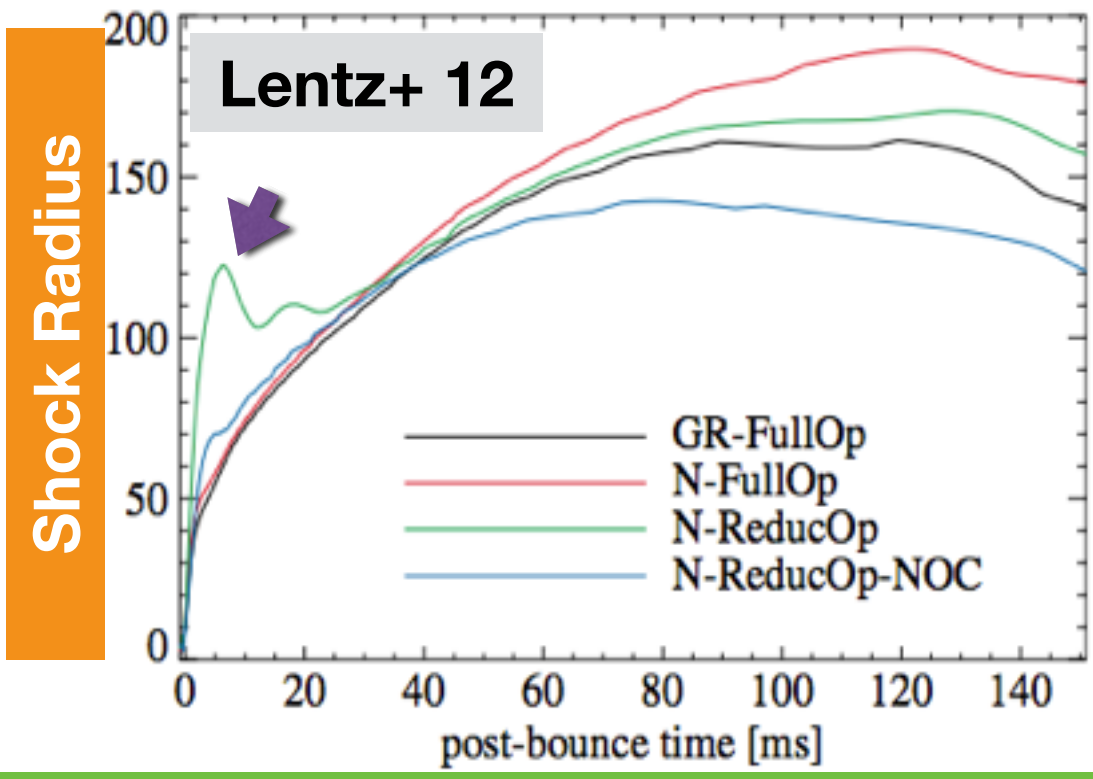
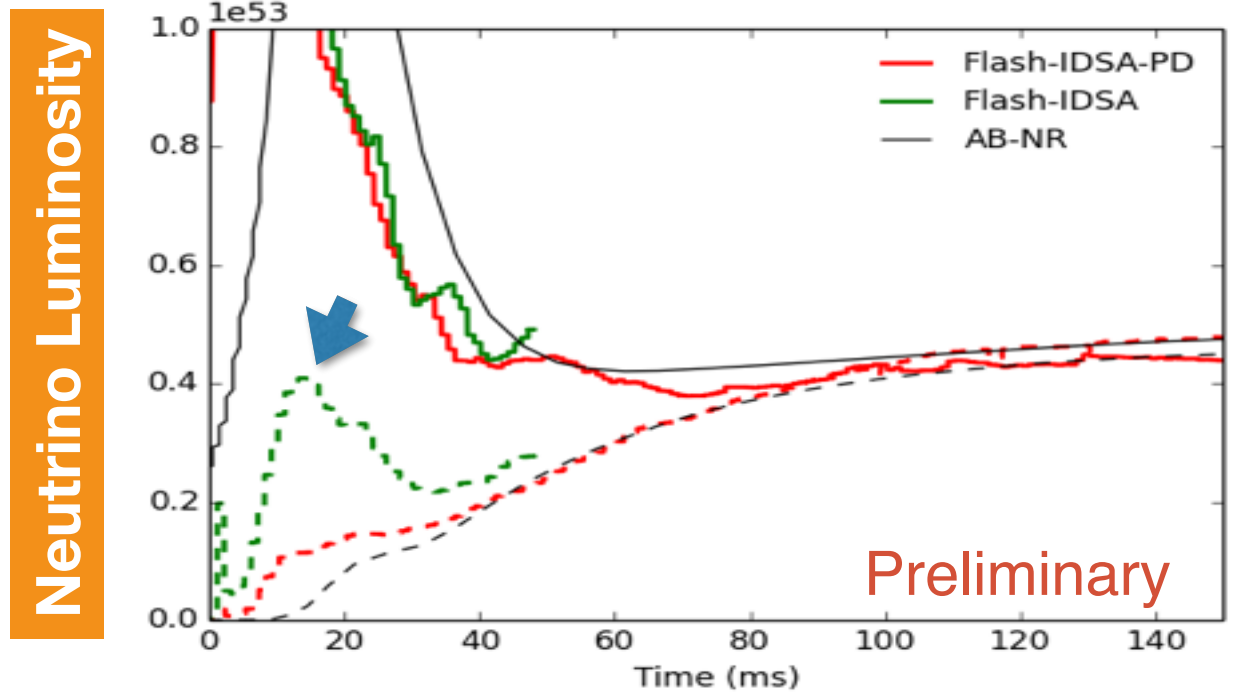
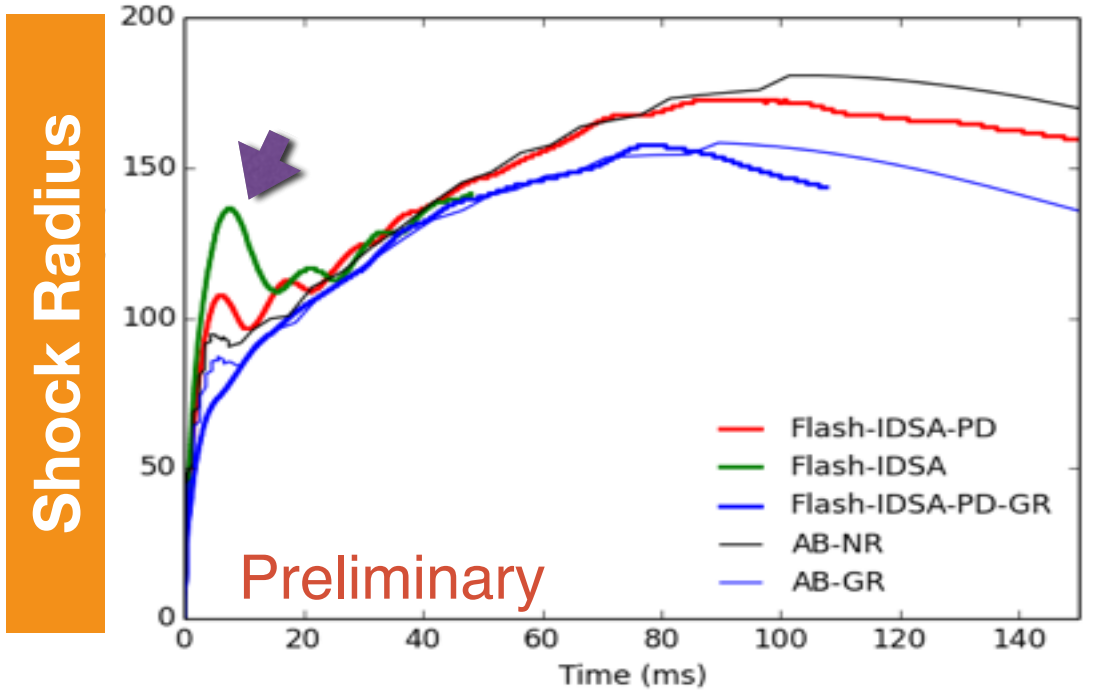
1D Code Comparison: Eff. GR

s15s7b2 (W1995) + LS180



The Bruenn rates (1985) in IDSA

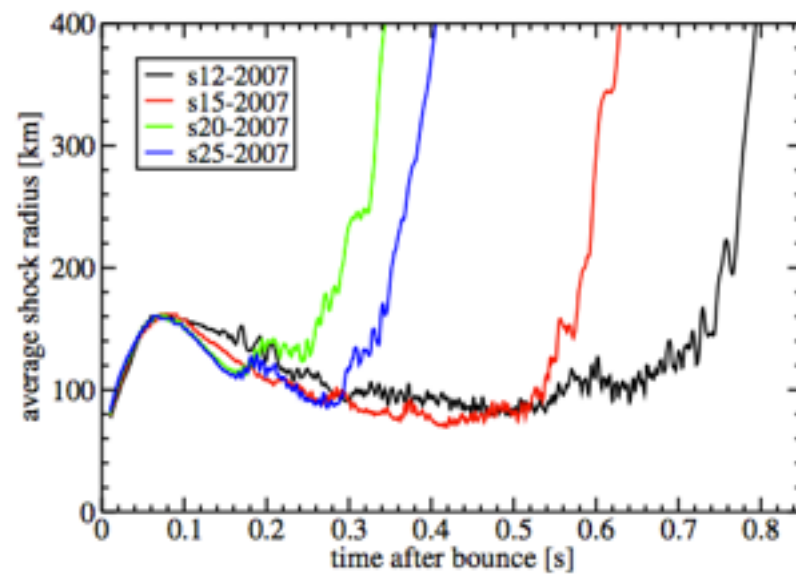
s15 (W2007) + LS220



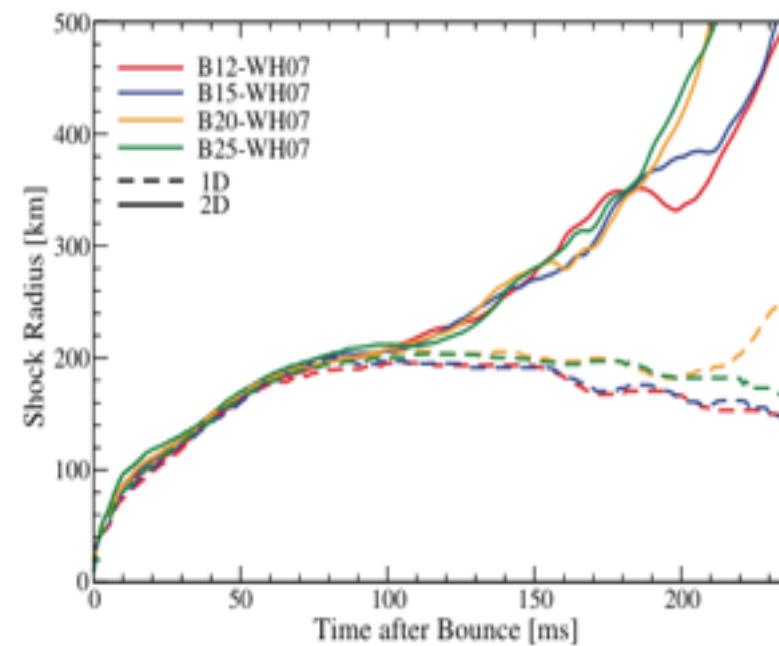
2D Code Comparison

The 2007 (WHW) Progenitors

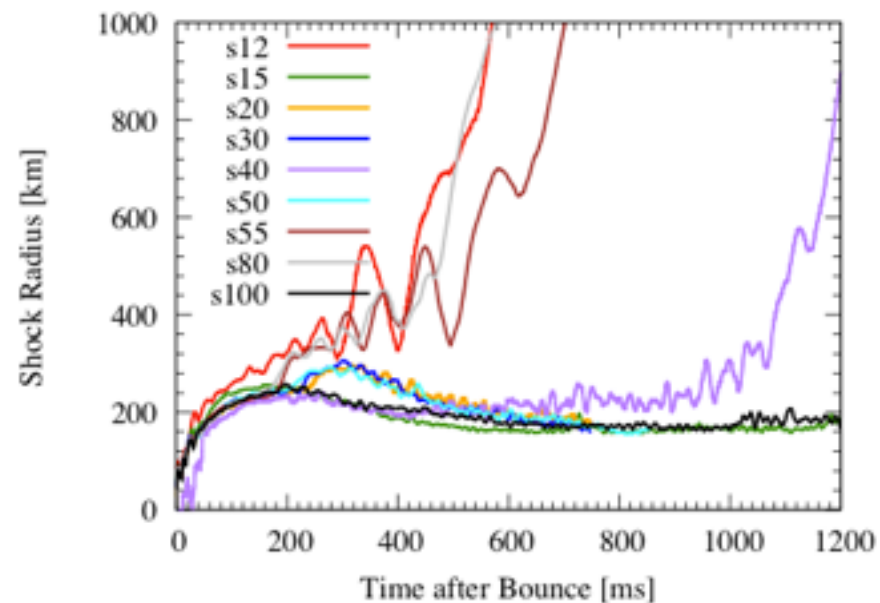
Hanke 14



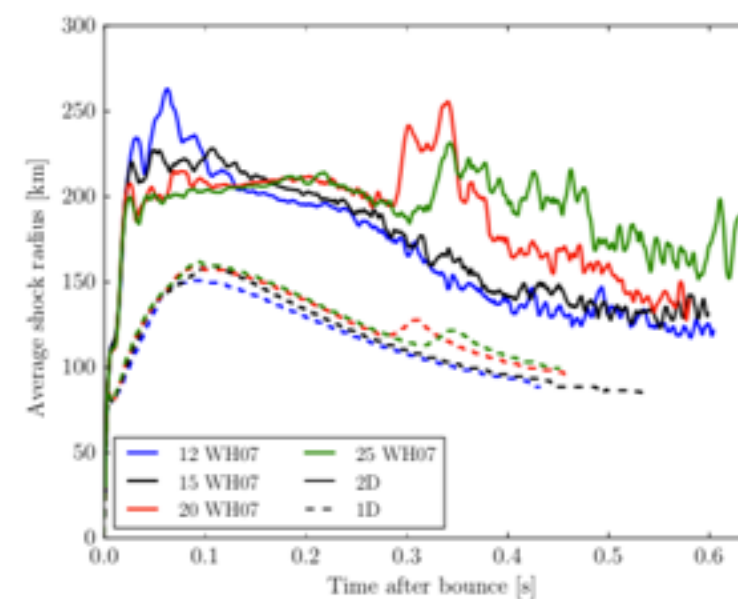
Bruenn +13



Suwa +14



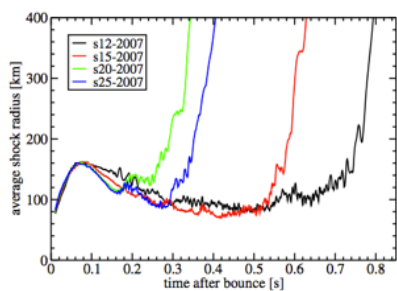
Dolence+15



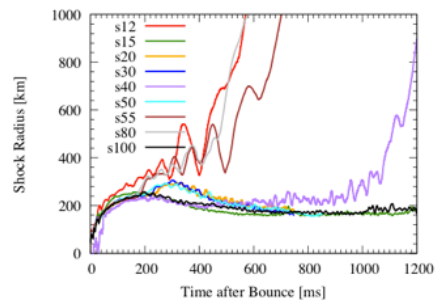
2D Code Comparison

The 2007 (WHW) Progenitors

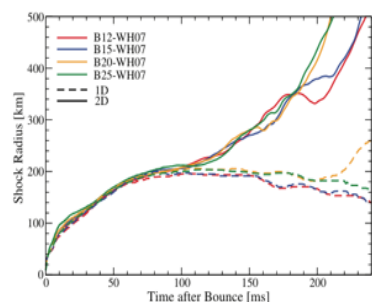
Hanke 14



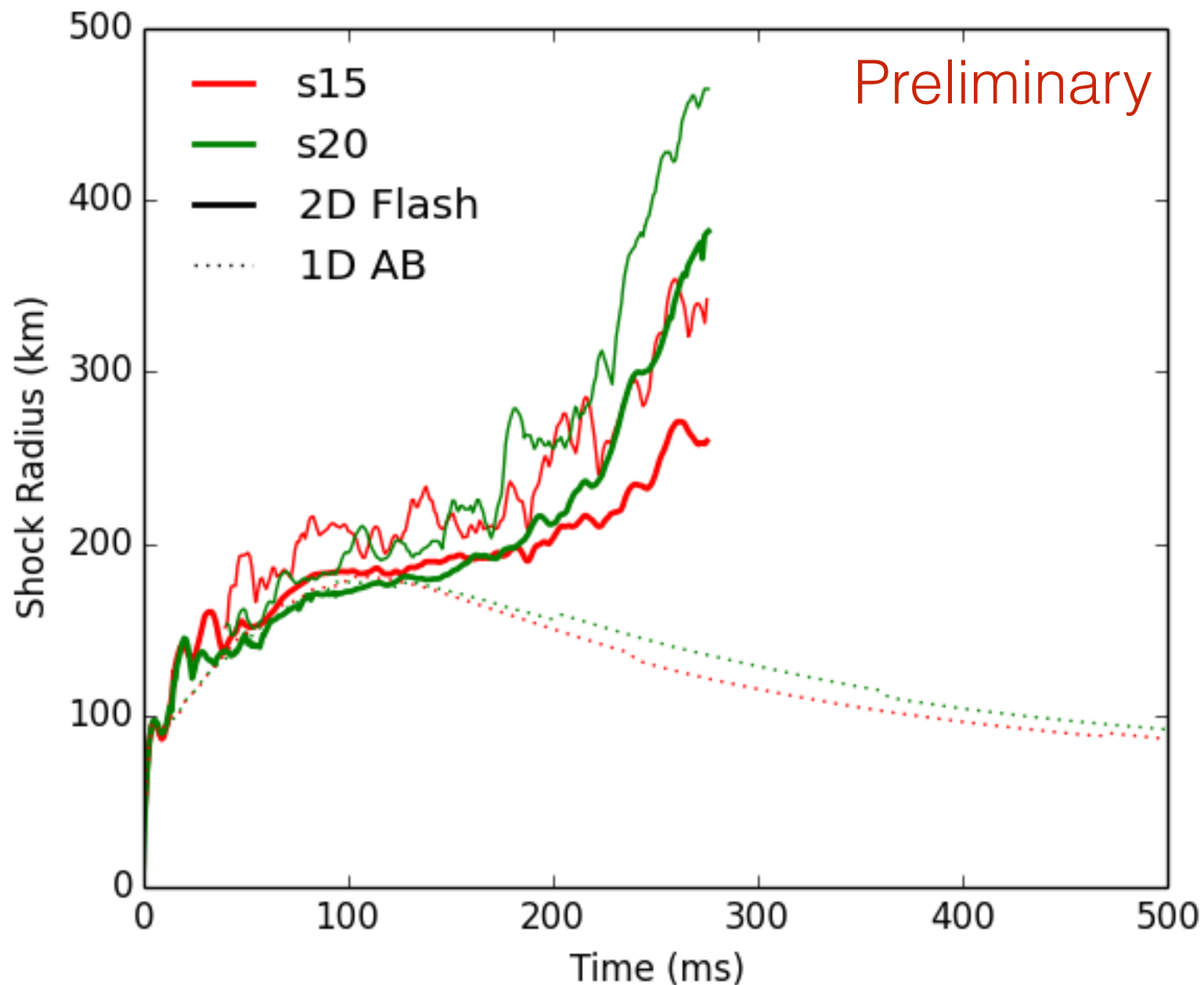
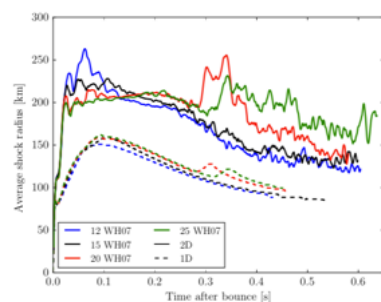
Suwa +14



Bruenn +13

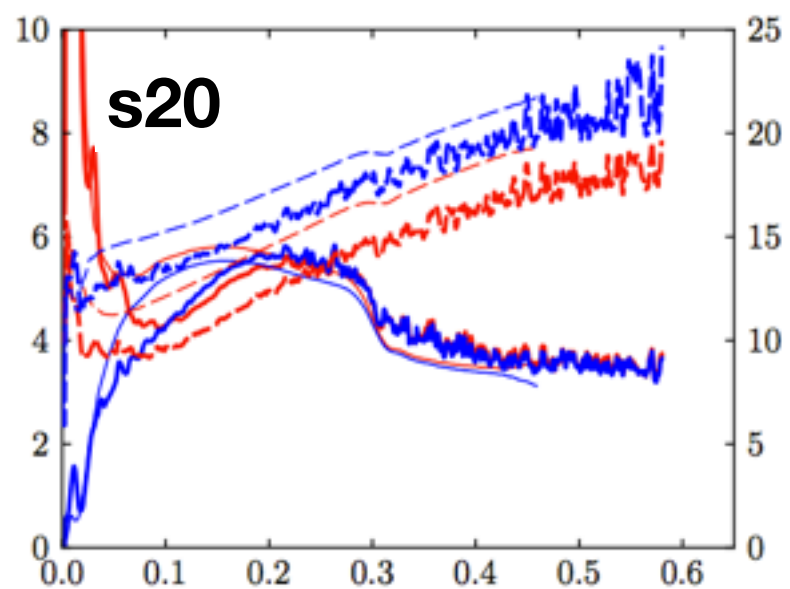
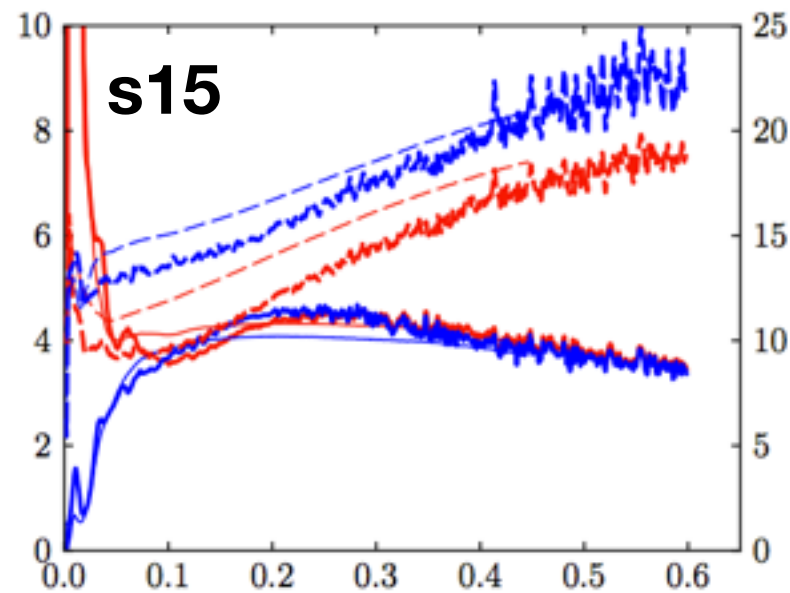


Dolence+15



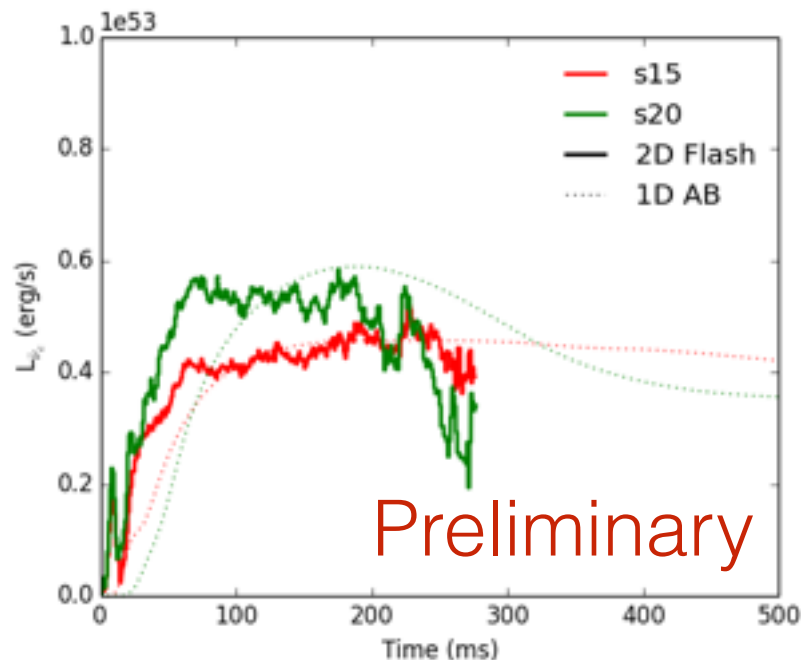
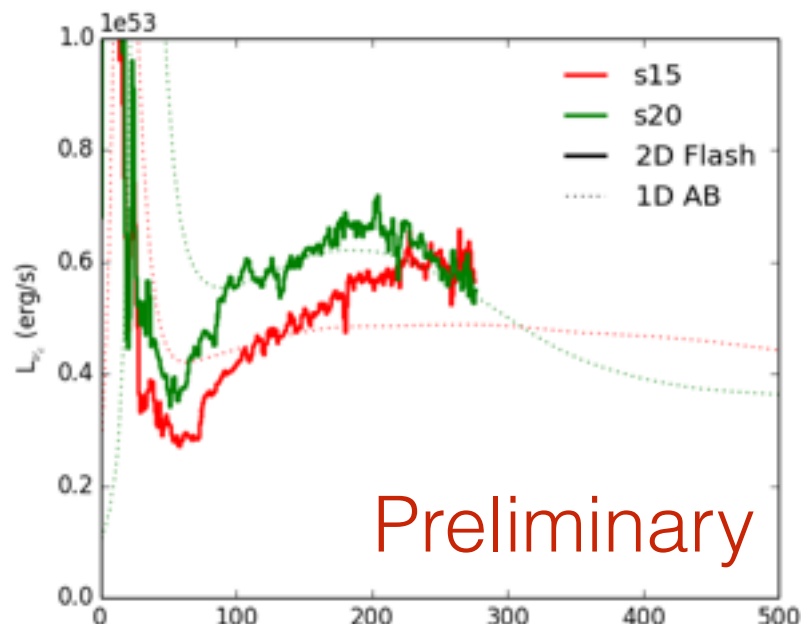
2D Code Comparison

Dolence+15



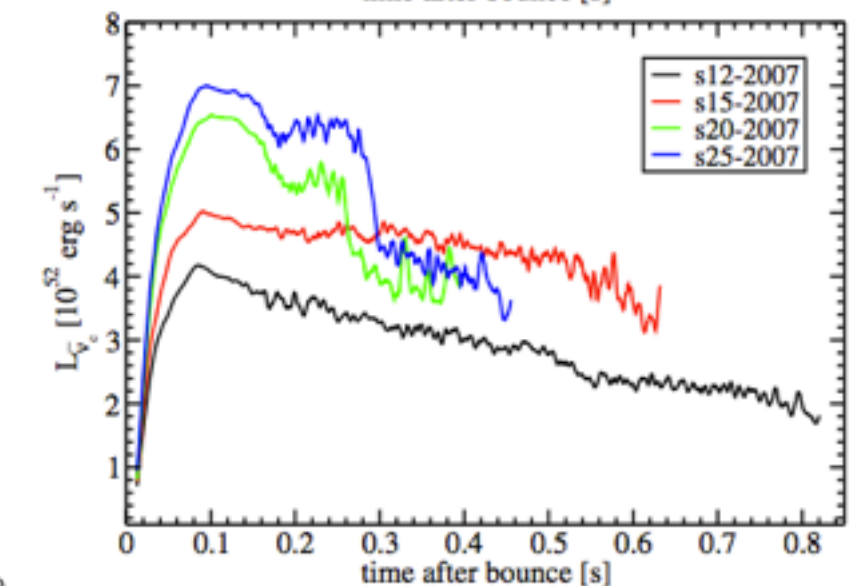
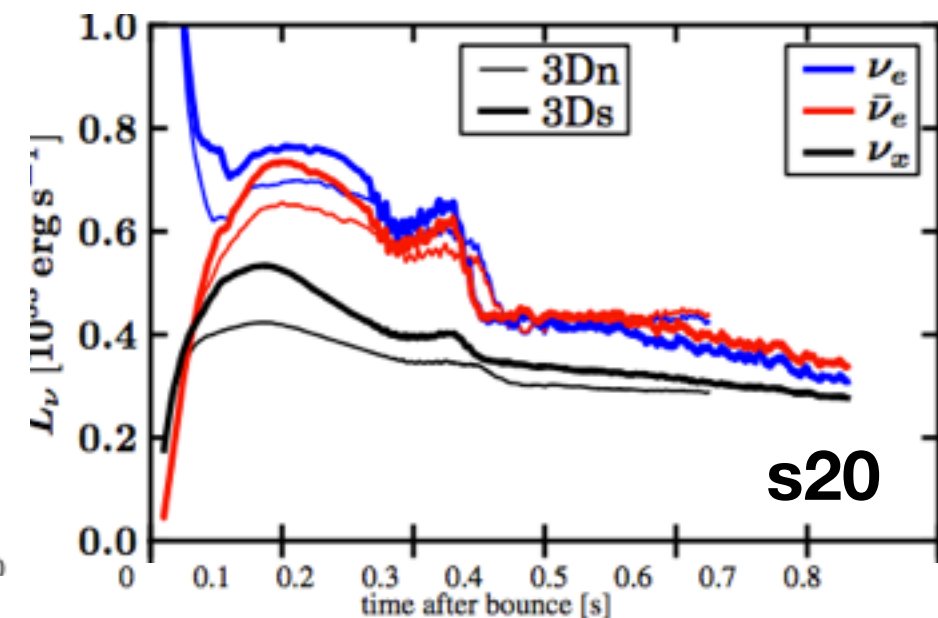
NR+ShenEoS

FLASH+IDSA



NR+LS220

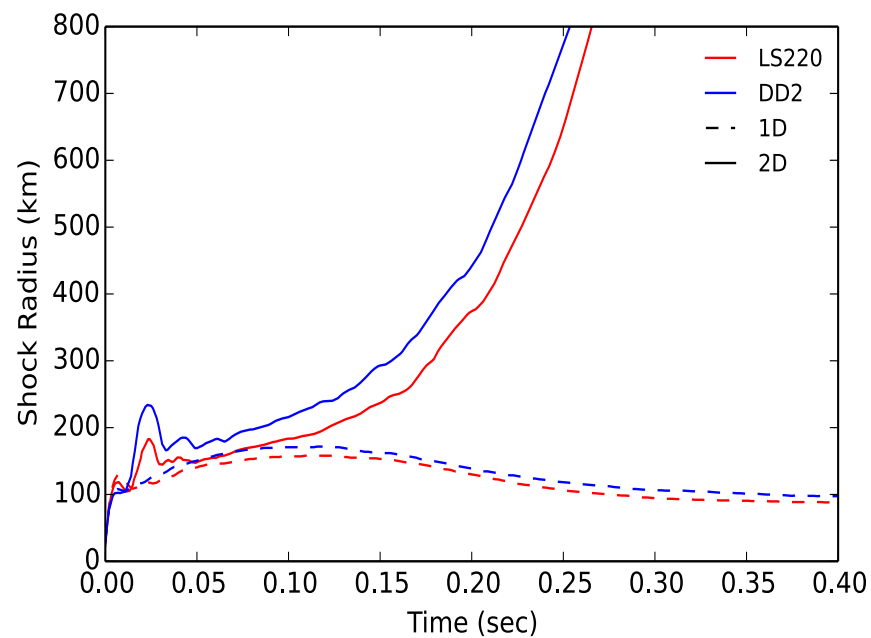
Melson+15



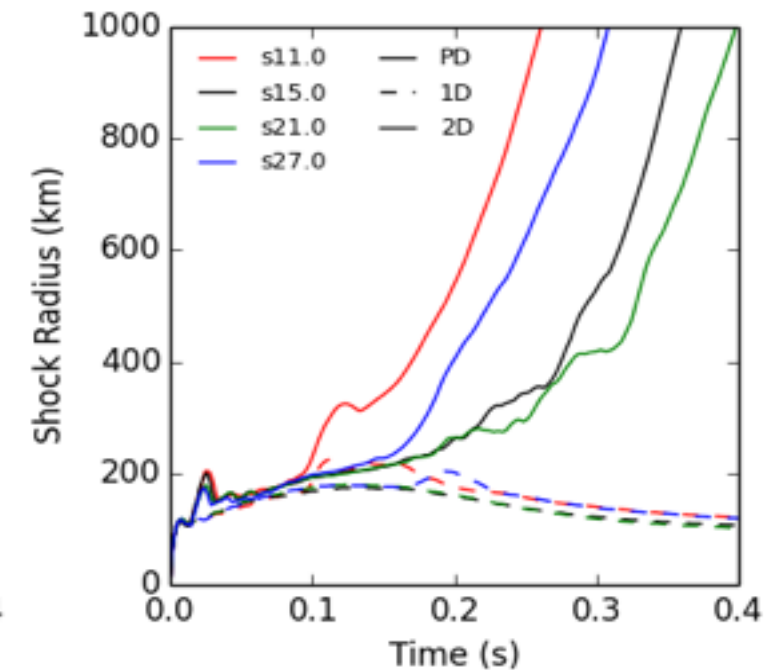
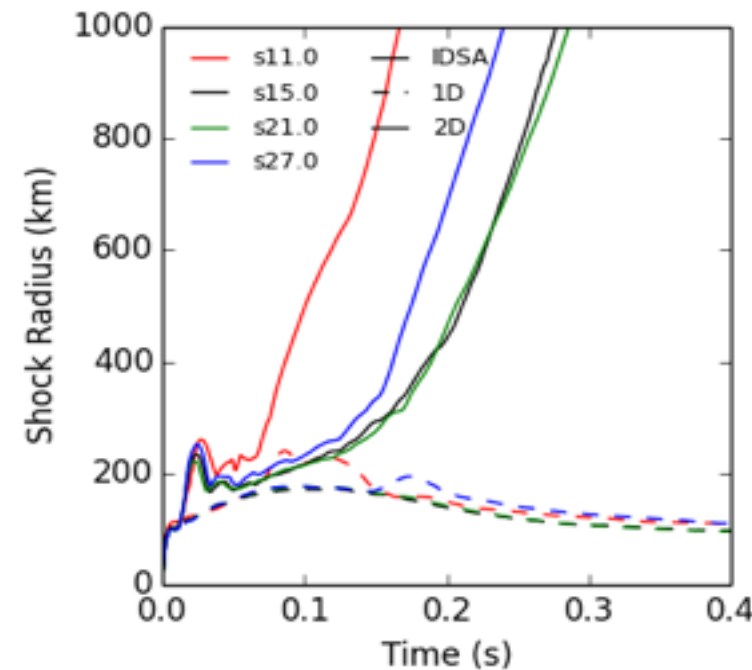
GR+LS220

2D: W2002 Progenitors

DD2 vs. LS220



FLASH+IDSA+DD2



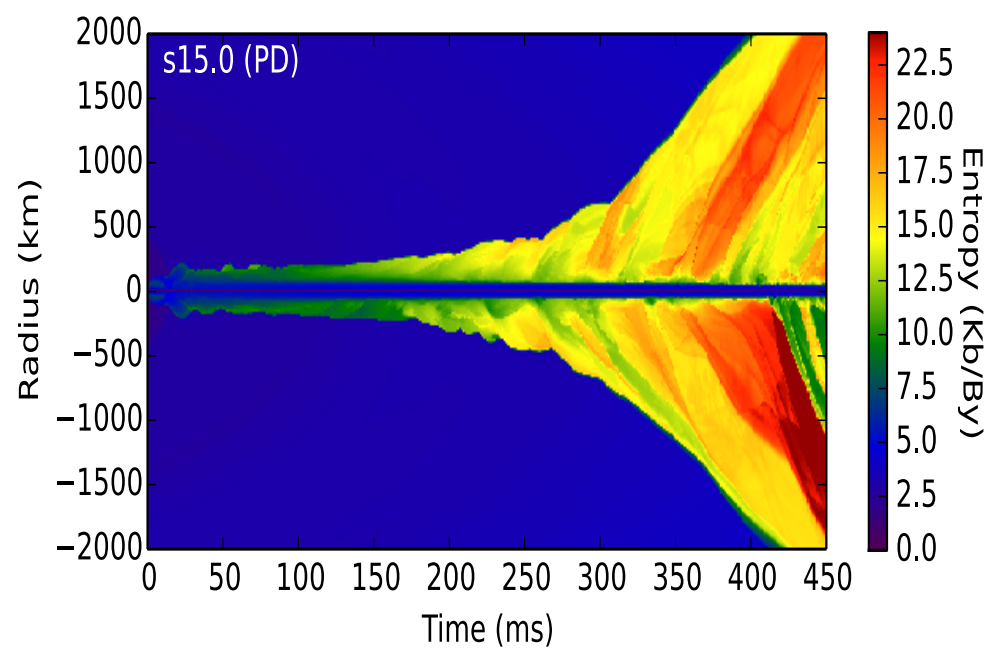
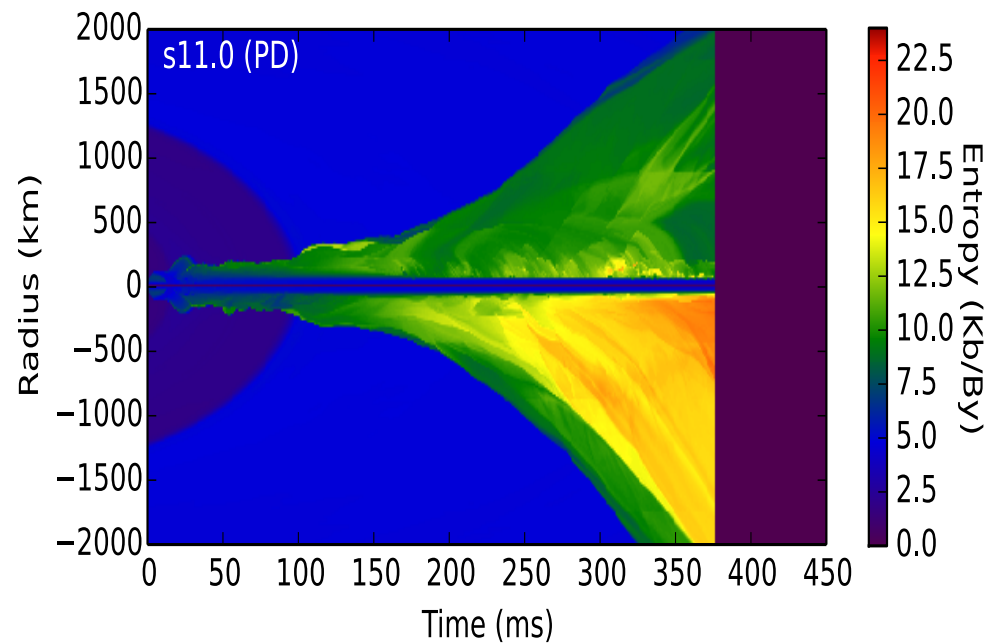
Pan+15

The HS(DD2) EoS

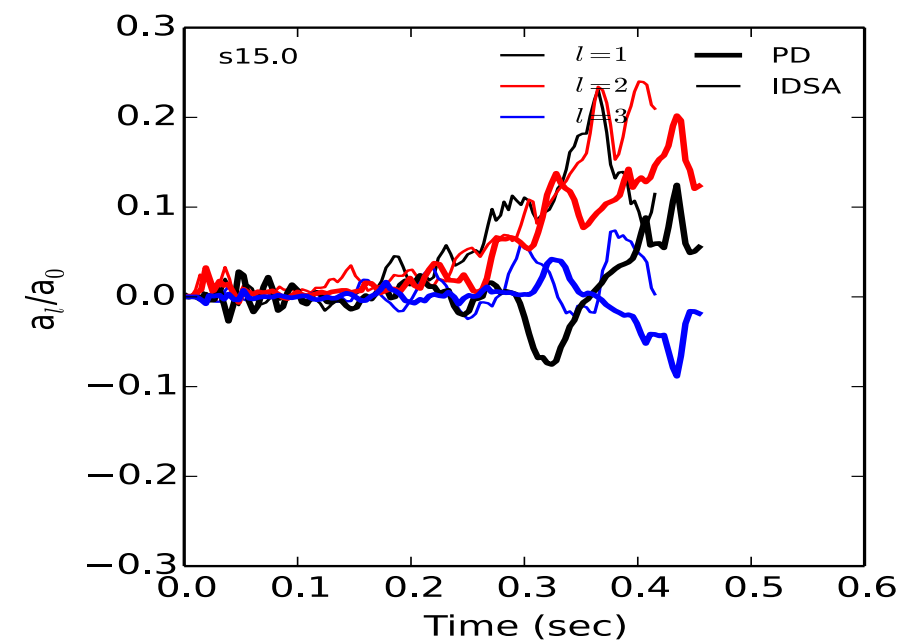
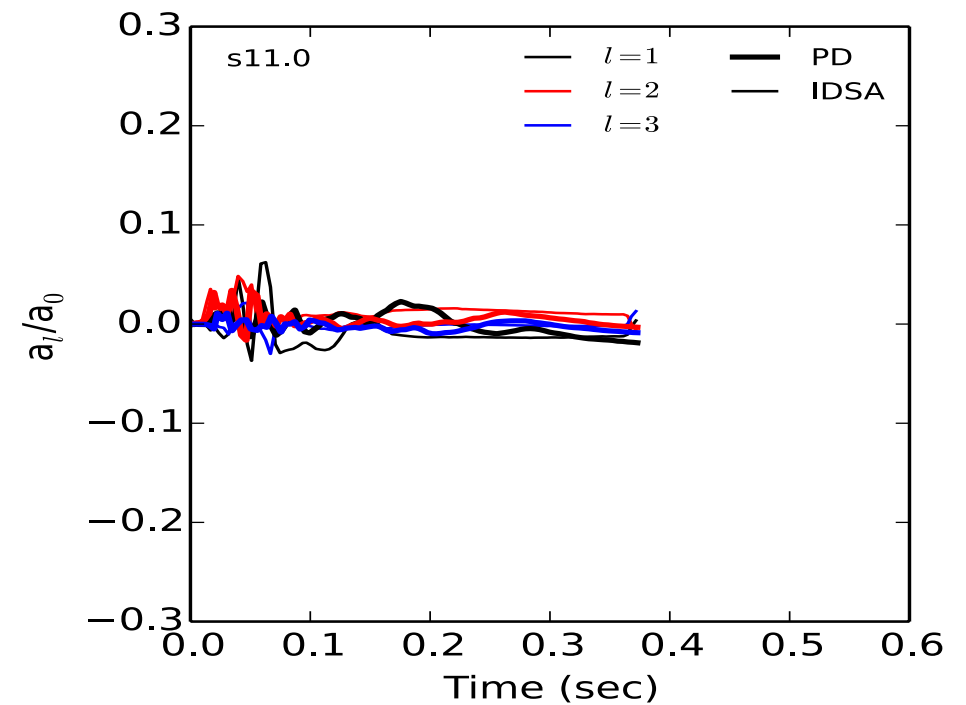
The new SN EoS HS (DD2) shows a better agreement with nuclear experiments (Kruger+13; Fischer+14; Hempel+15)

2D Results: SASI

Pole Entropy

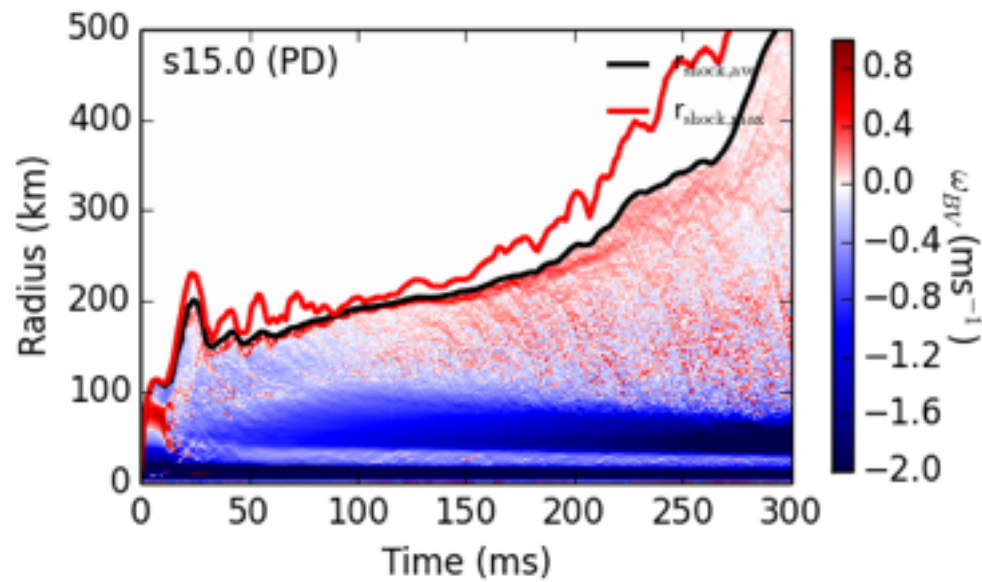
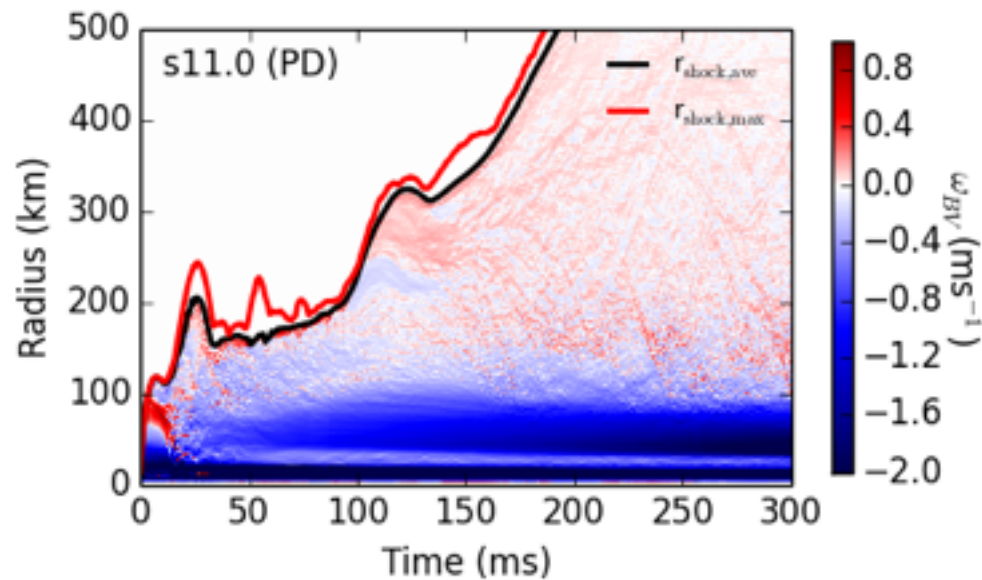


SASI Amplitude

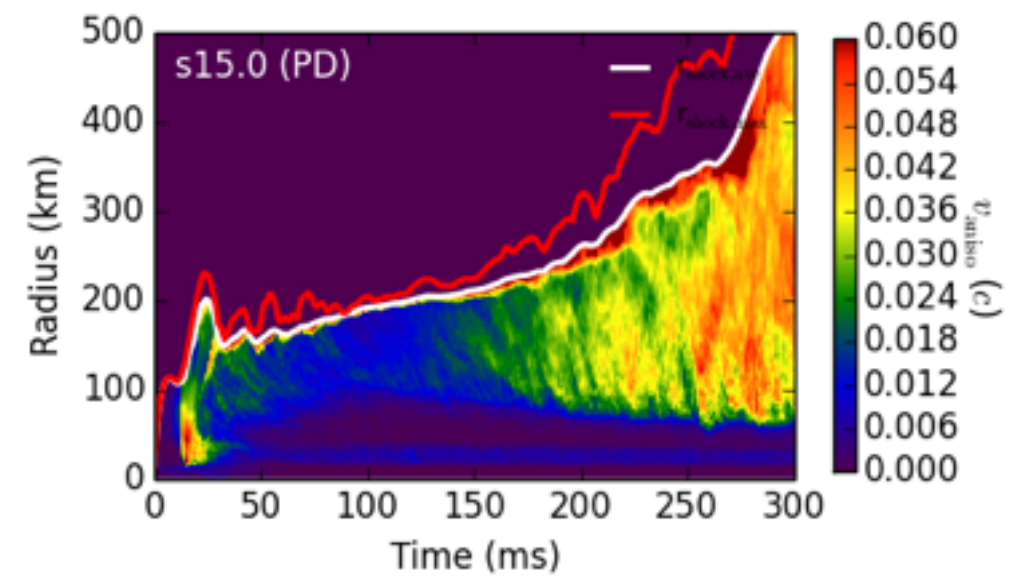
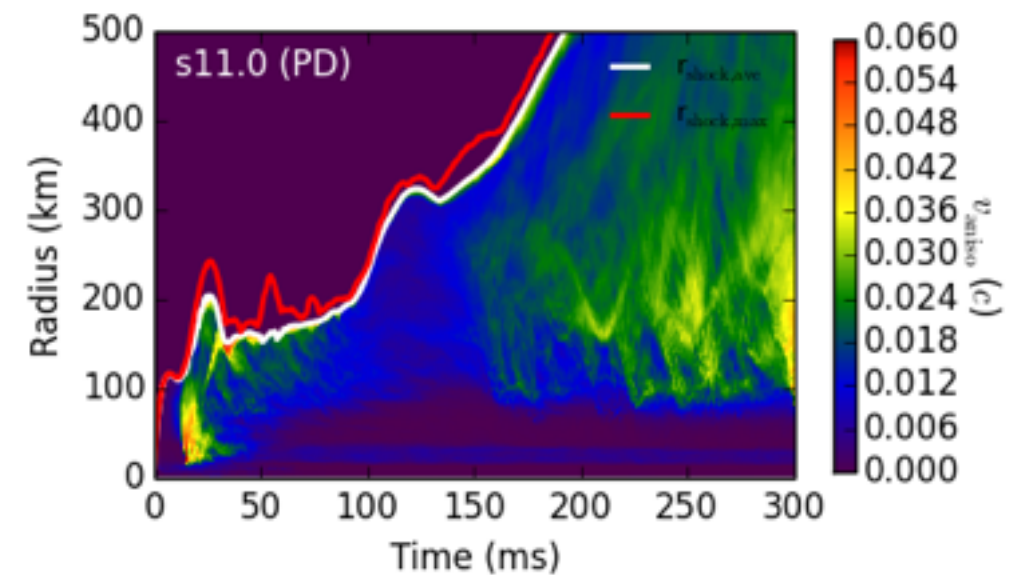


2D Results: Convection-Driven

Brunt-Vaisala Frequency

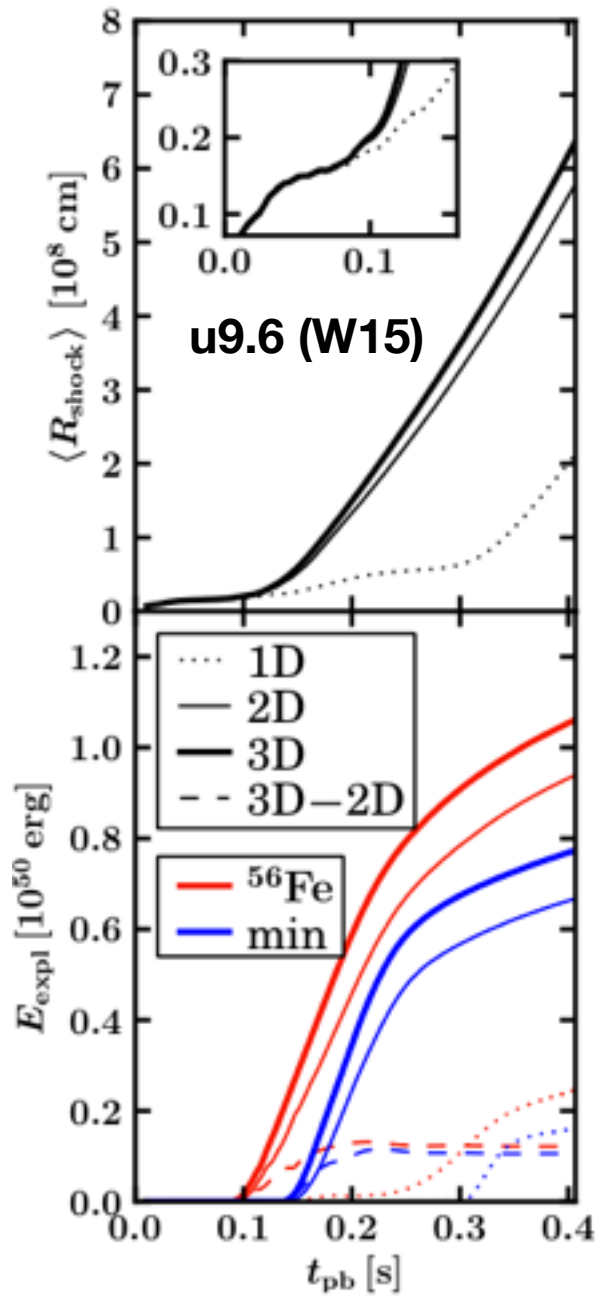


Anisotropic Velocity

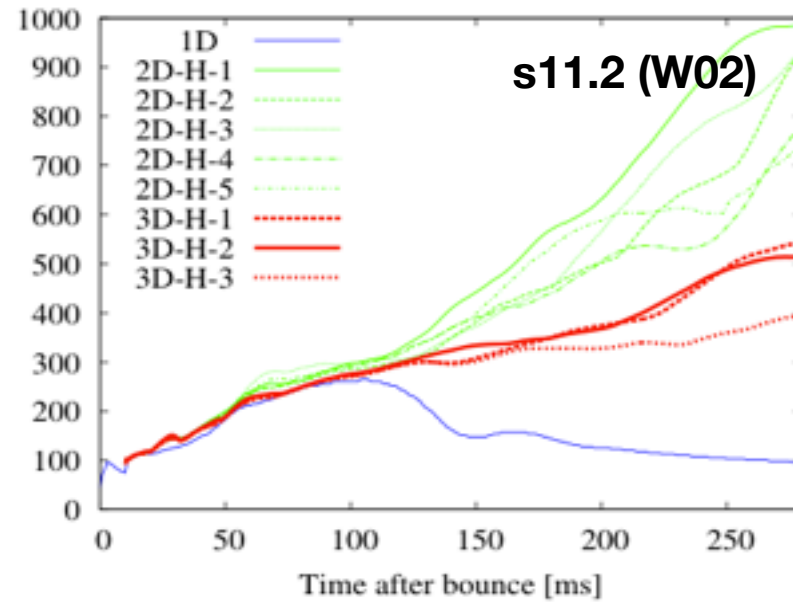


2D vs. 3D

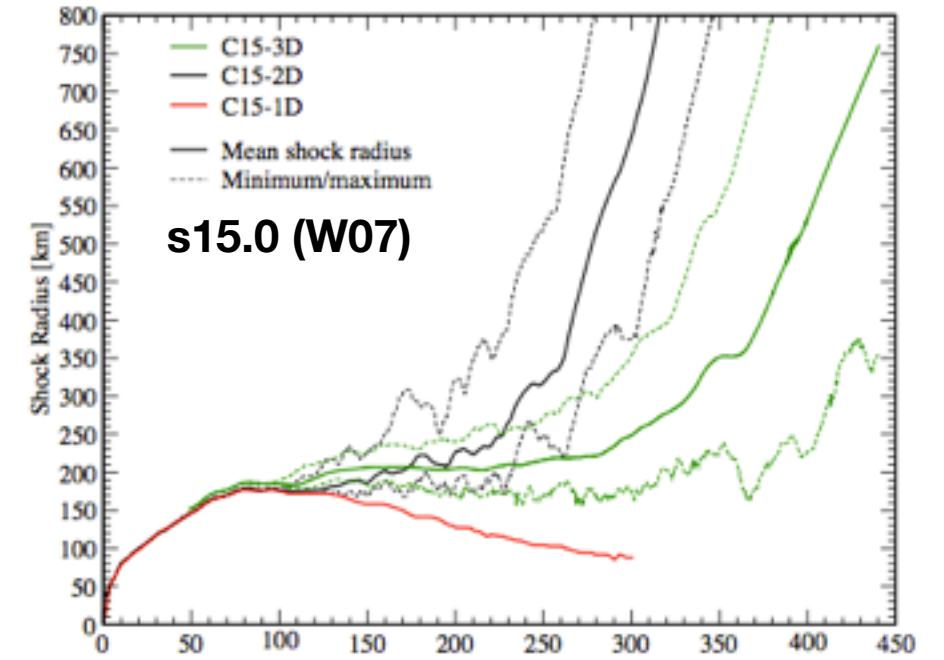
Melson+15



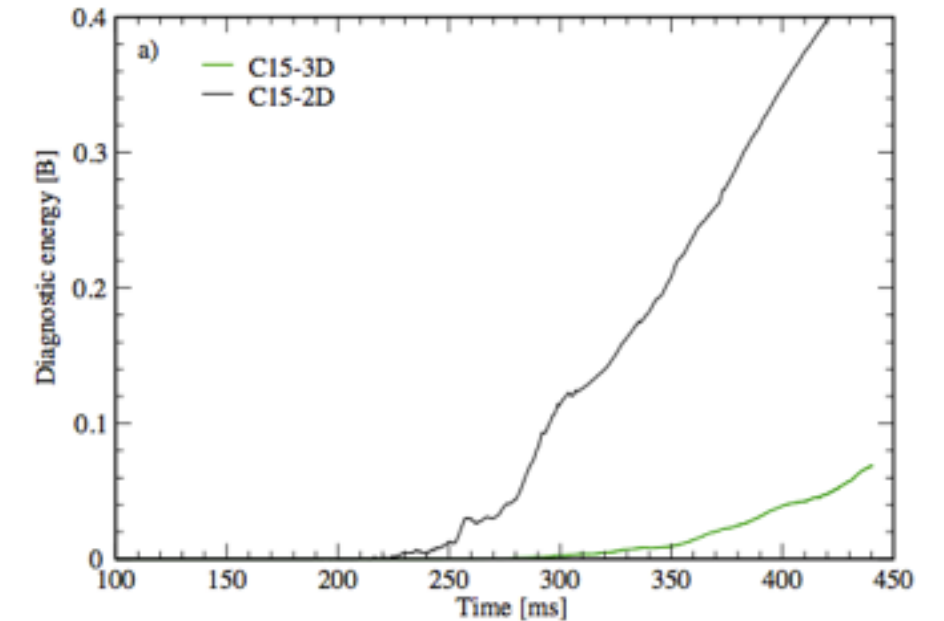
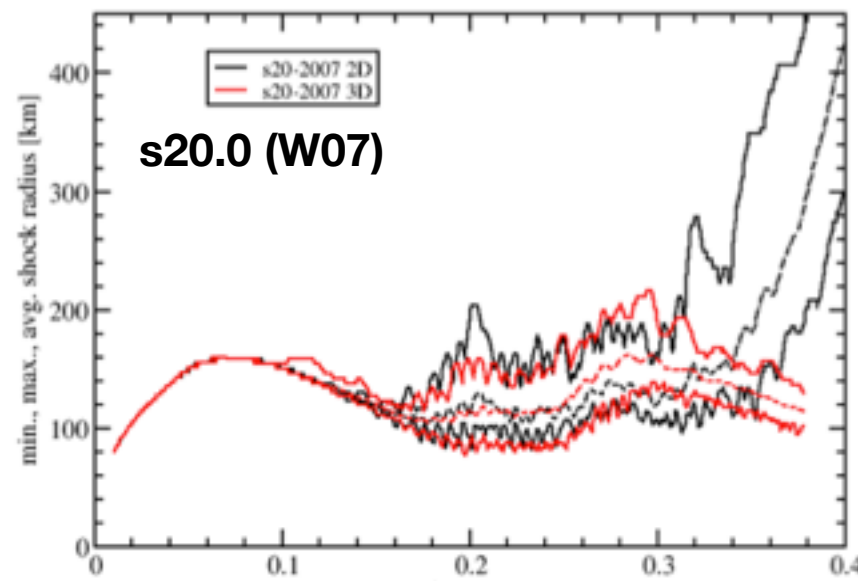
Takiwaki+14



Lentz+15



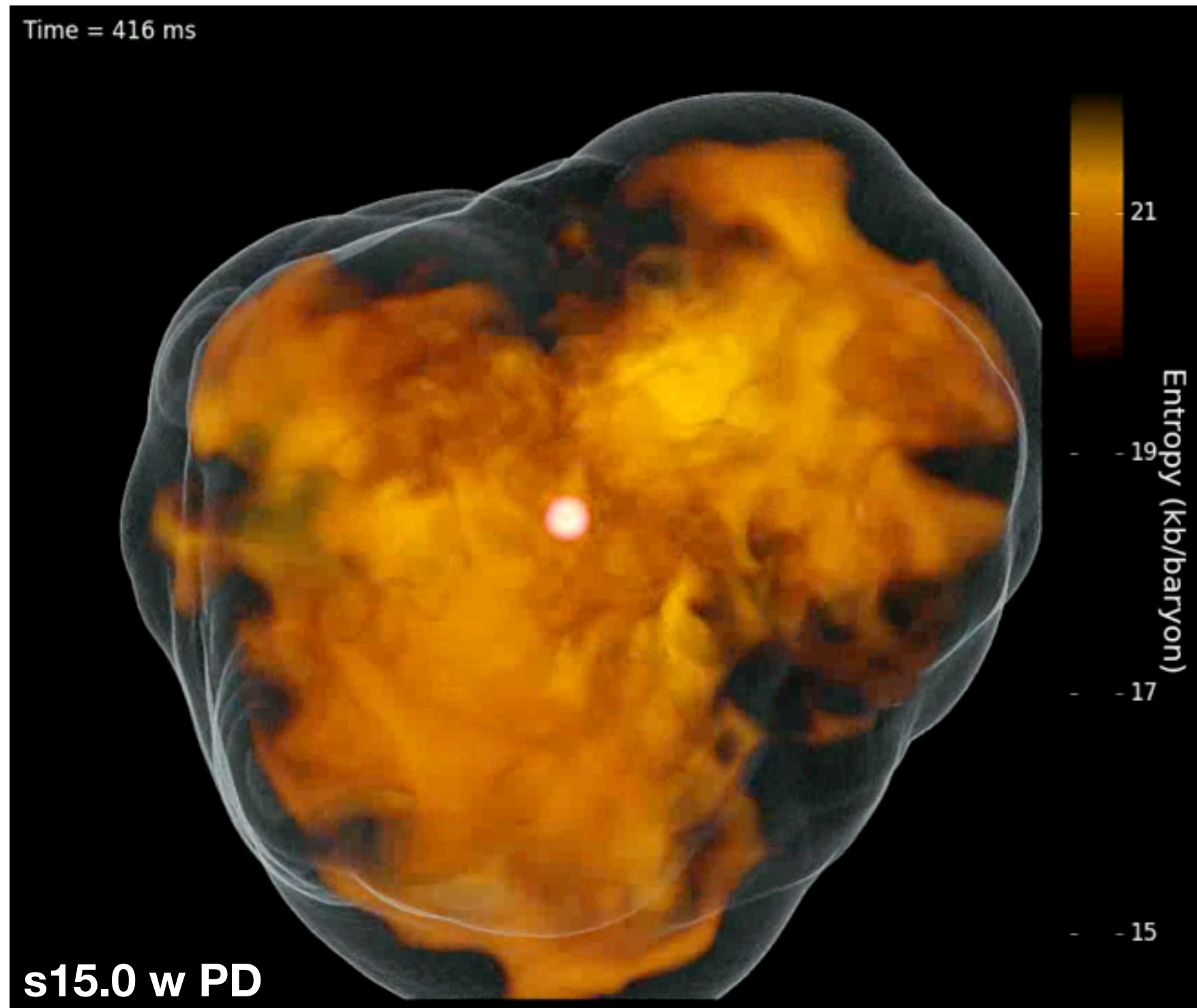
Muller+13



3D FLASH-IDSA results

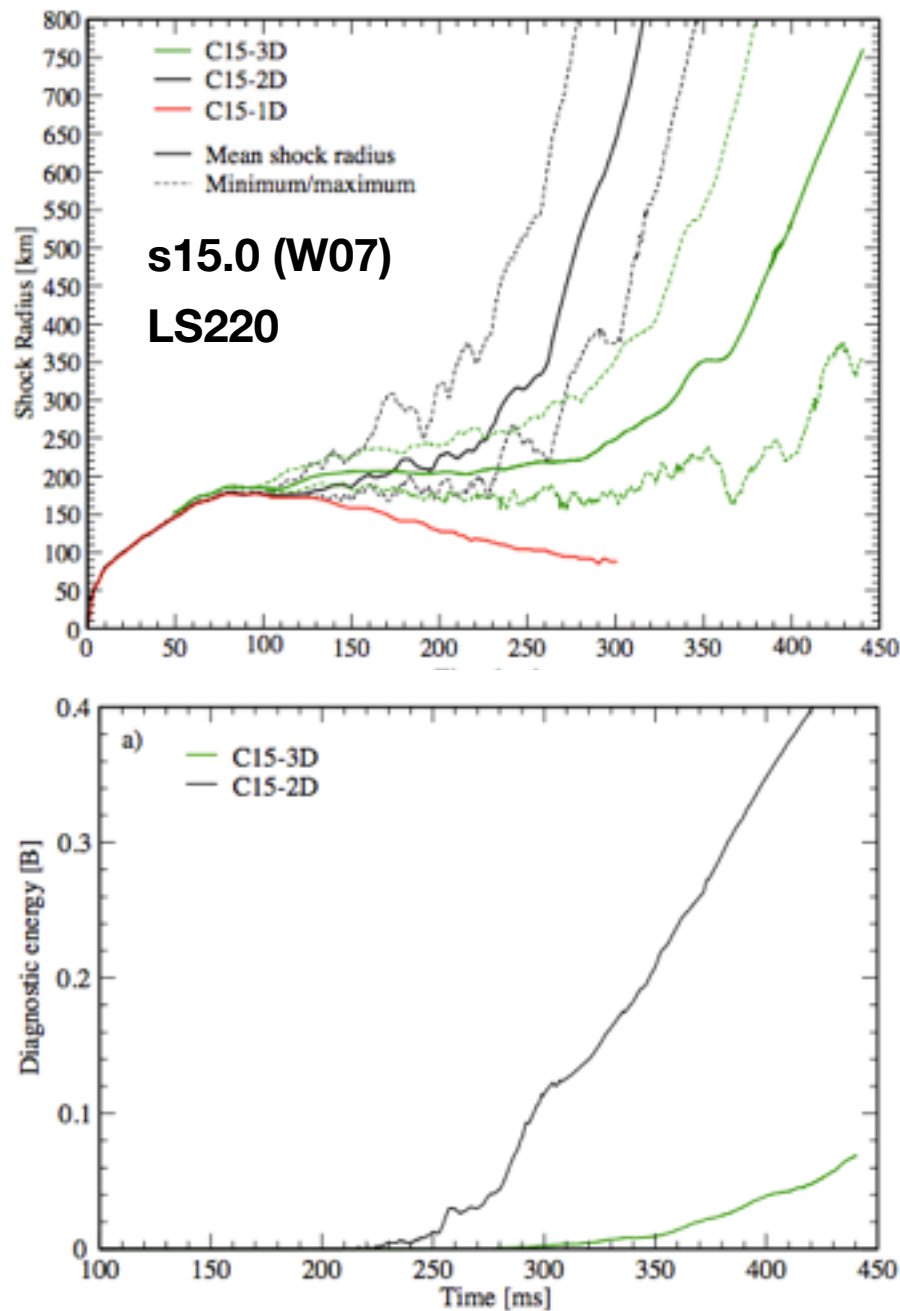
Pan+ in prep.

- ▶ 3D IDSA+PD
- ▶ $15M_{\text{sun}}$ (WHW+02)
- ▶ HS (DD2) EoS
- ▶ Newtonian
- ▶ Resolution: 1.8°
- ▶ Only **0.5M** cpu-hours

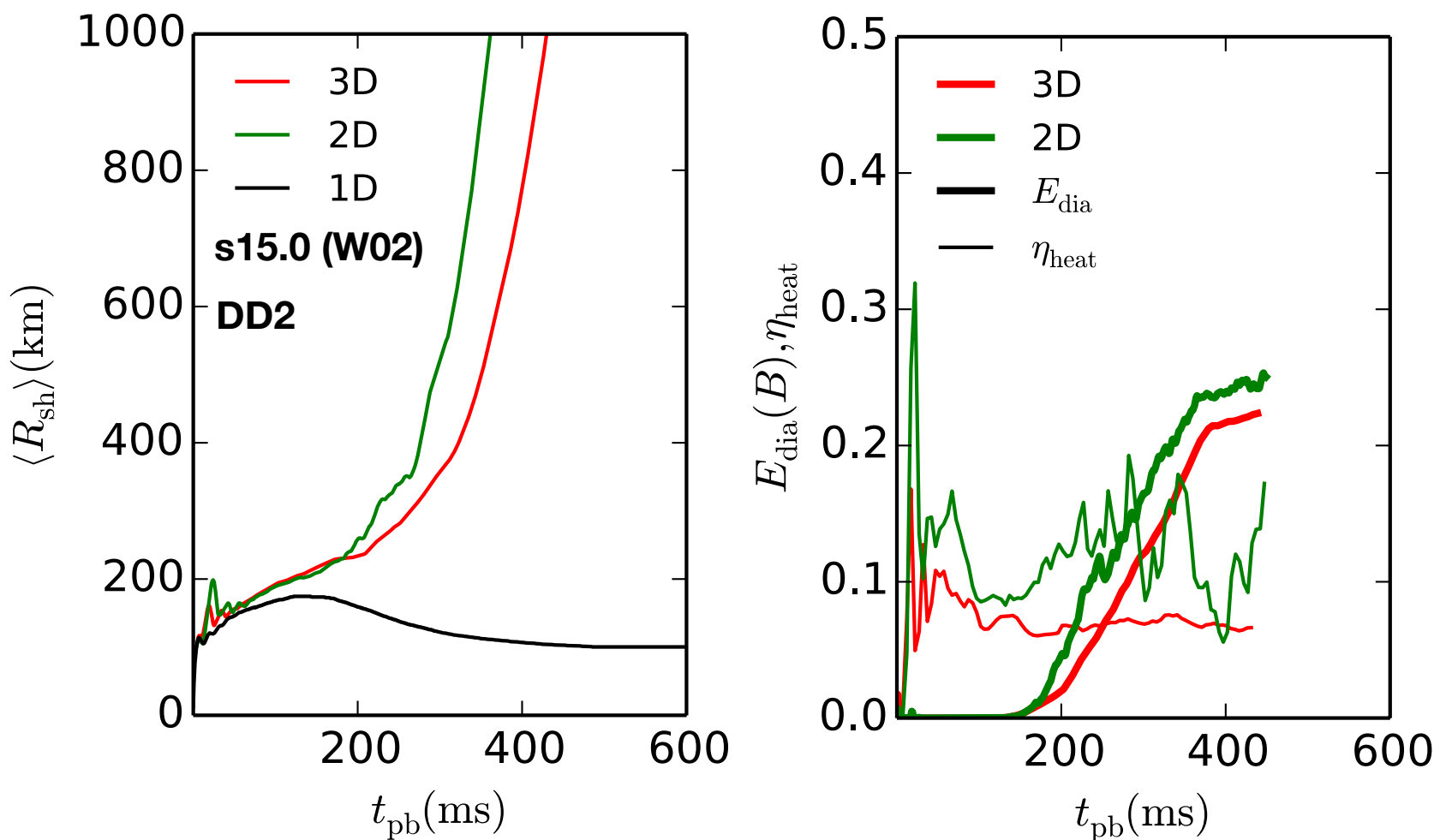


3D simulations with the 15.0 progenitor

Lentz+15

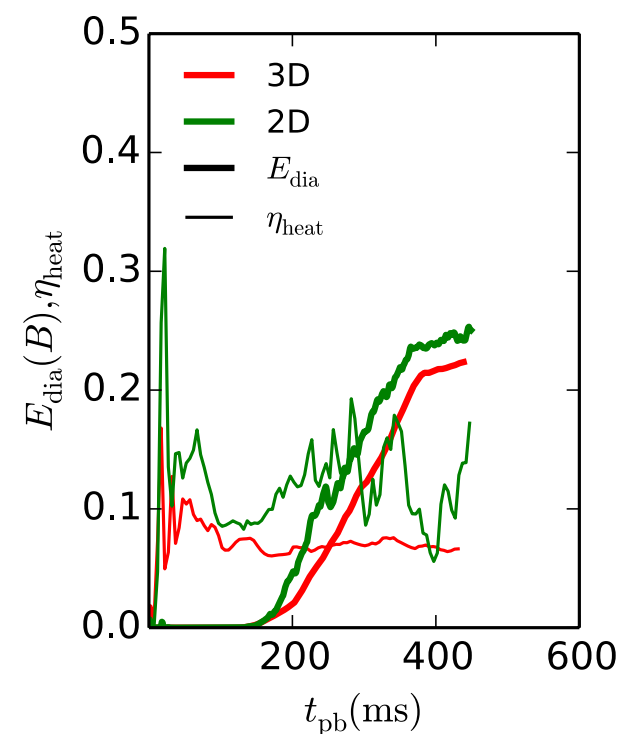
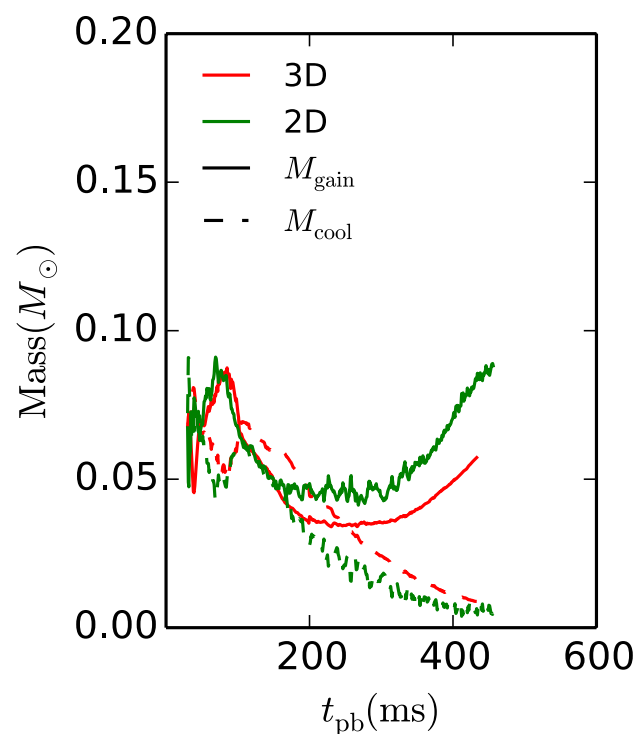
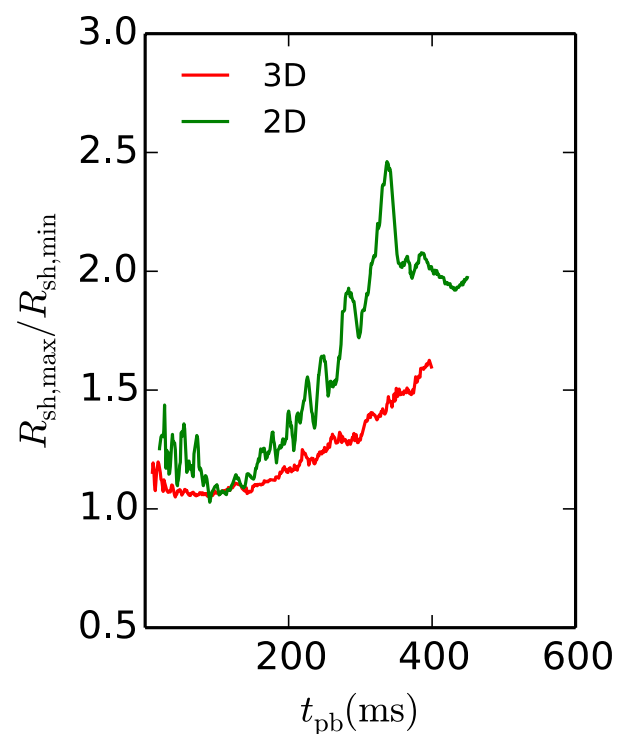
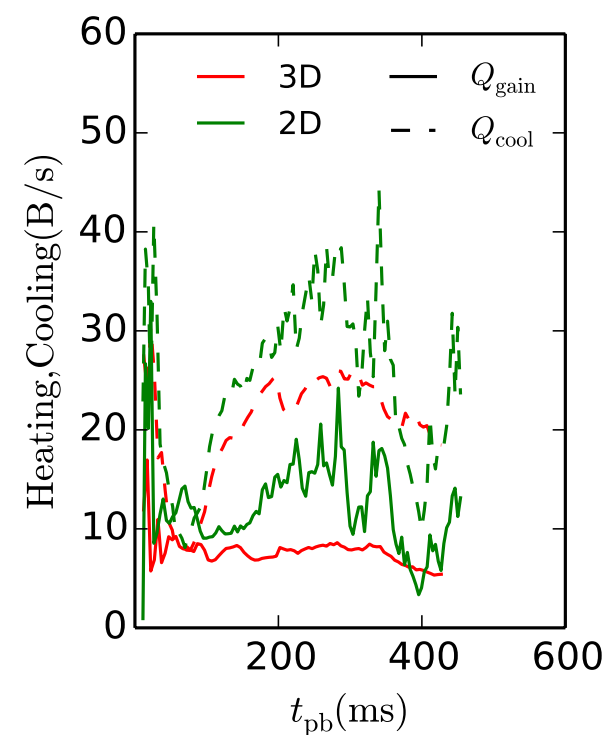
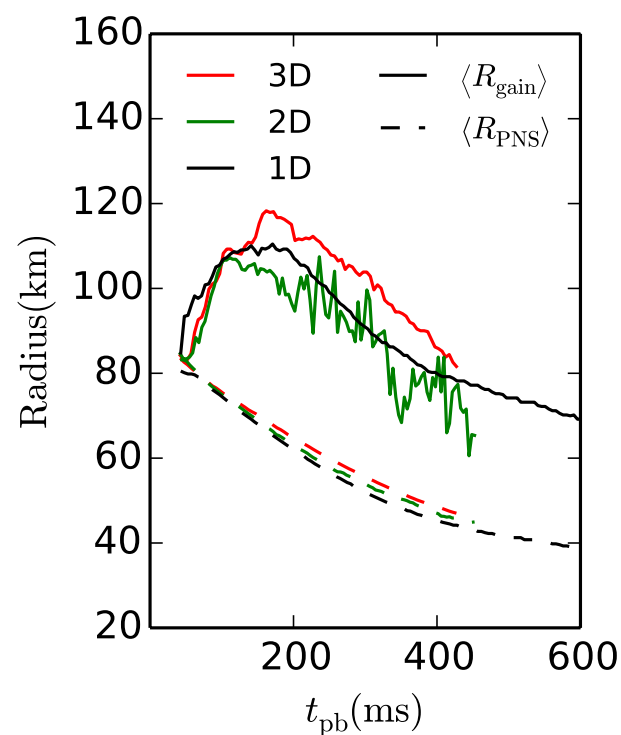
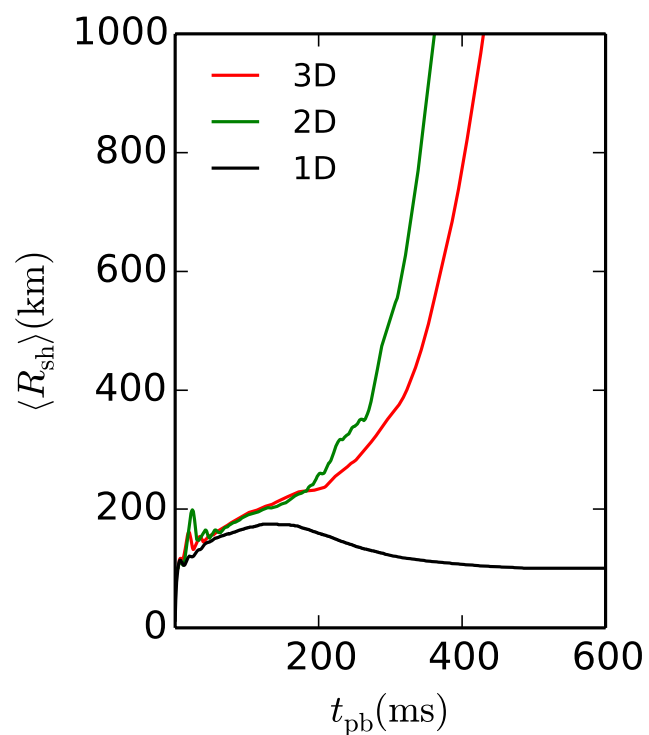


Pan+ in prep.



Note that the physics employed and the progenitors used are different

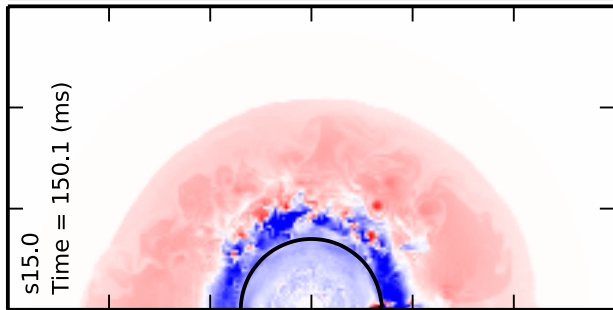
2D vs. 3D (conti.)



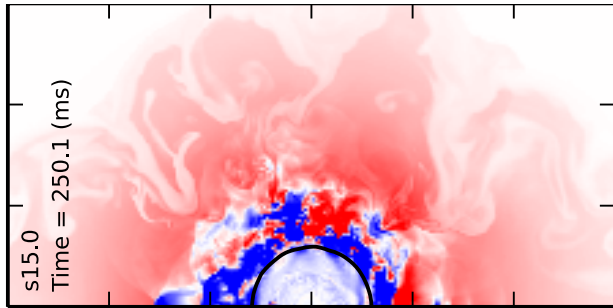
Neutrino Heating in 3D

2D

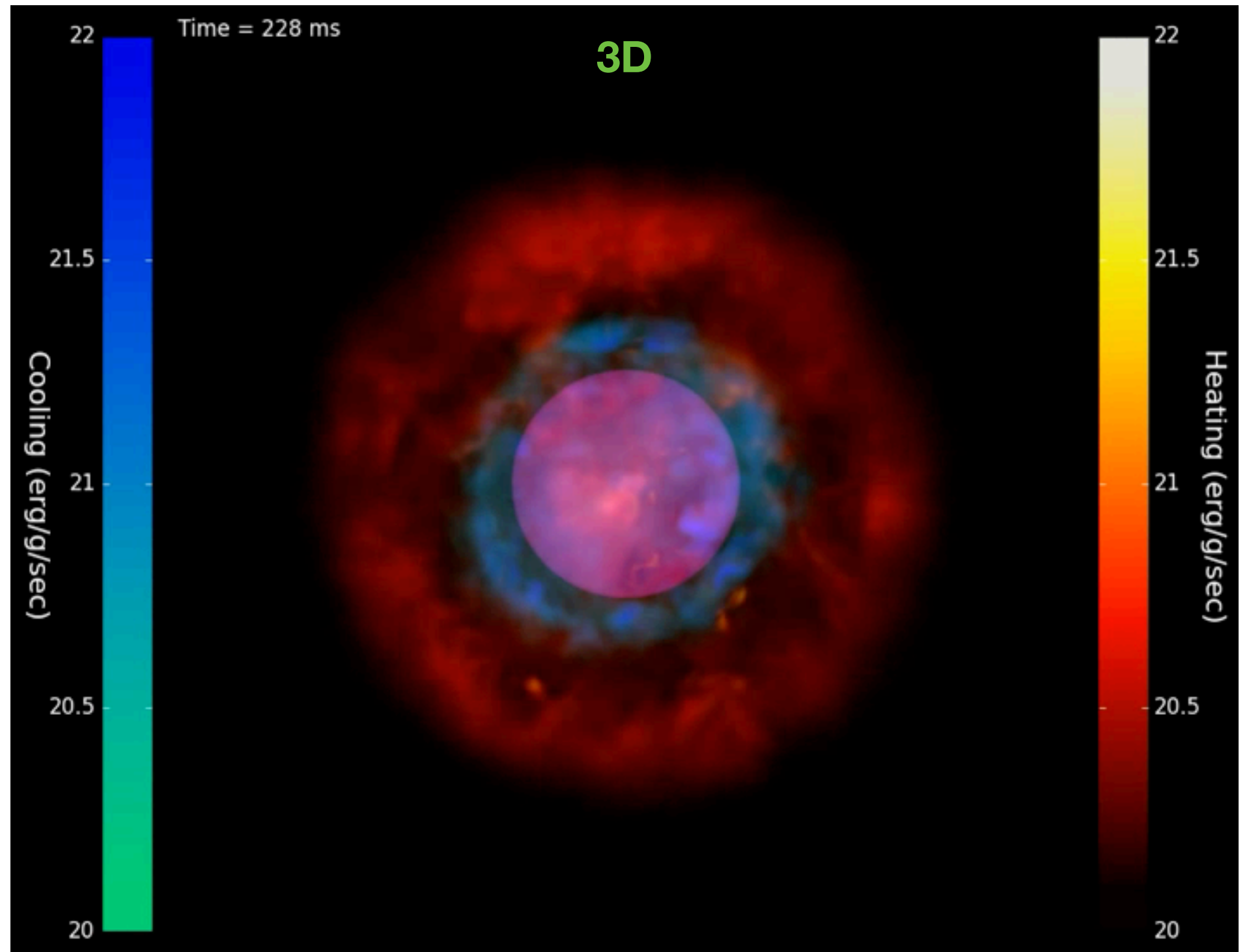
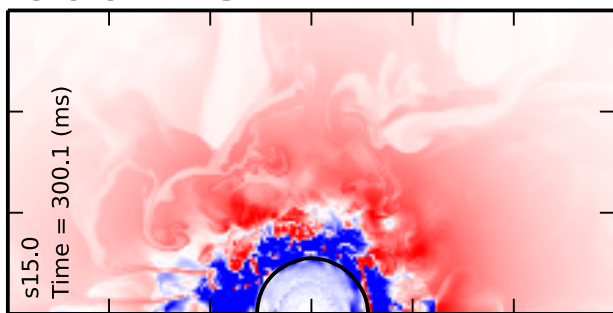
150 ms



250 ms



300 ms



500 km

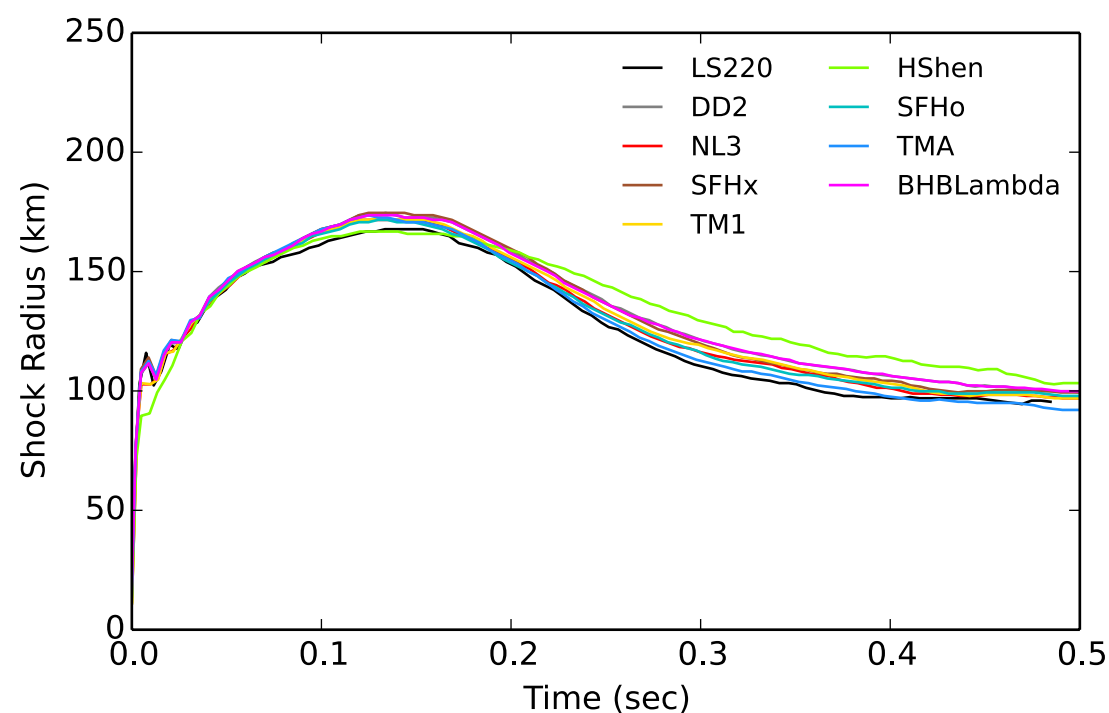
Conclusions

- ▶ Our IDSA implementation seems robust (or too optimistic; all 2D and 3D models exploded) with diagnostic explosion energies $\sim 0.1-0.5 B$ (at $\sim 400\text{ms}$)
- ▶ Neutrino interactions (e.g. NES) during collapse are important in Multi-D
- ▶ Neutrino-driven convection with little SASI (W2002 Progenitors)
- ▶ DD2 is slightly easier to explode than LS220
- ▶ 3D seems harder to explode than 2D
- ▶ IDSA is promising to achieve high-resolution 3D simulations (good for progenitor studies, long-term evolutions and nuclear synthesis)

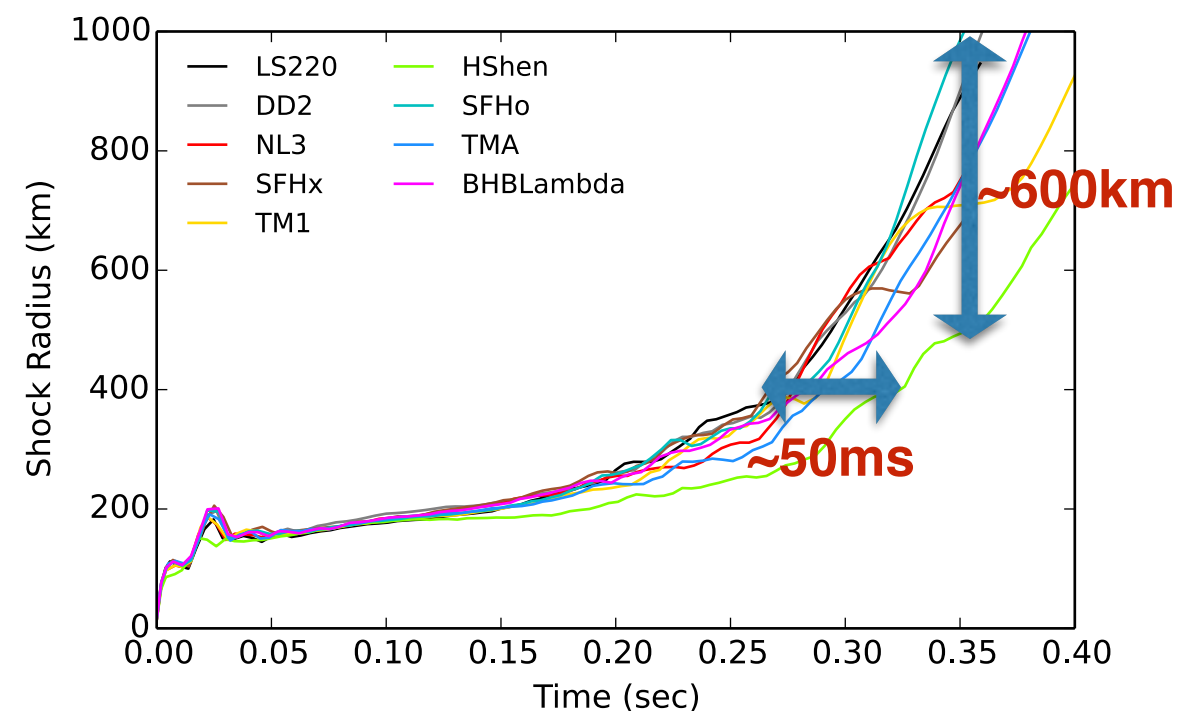
EoS Dependence

9 EoS from StellarCollapse with the s15.0 (W2002) progenitor

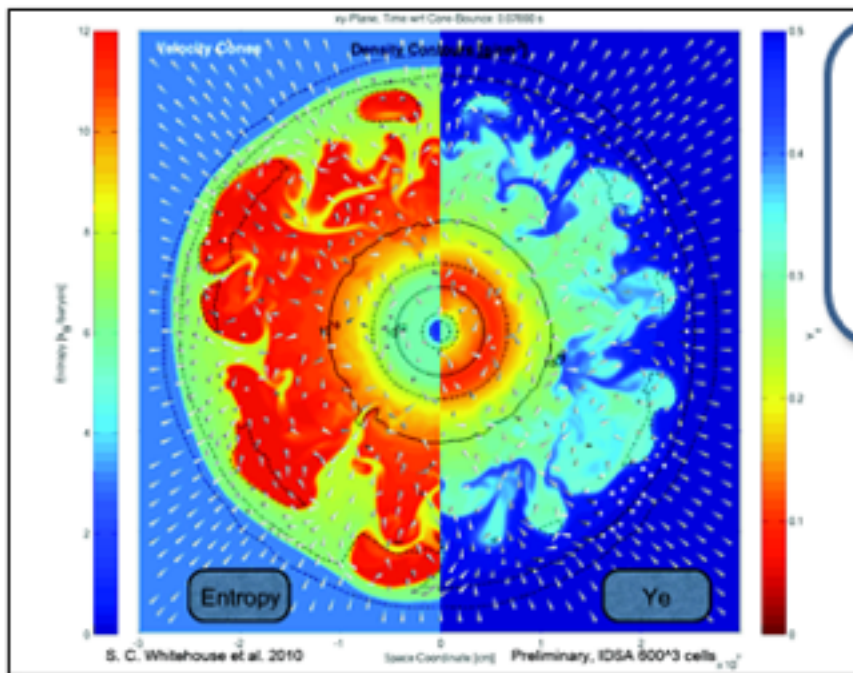
1D



2D

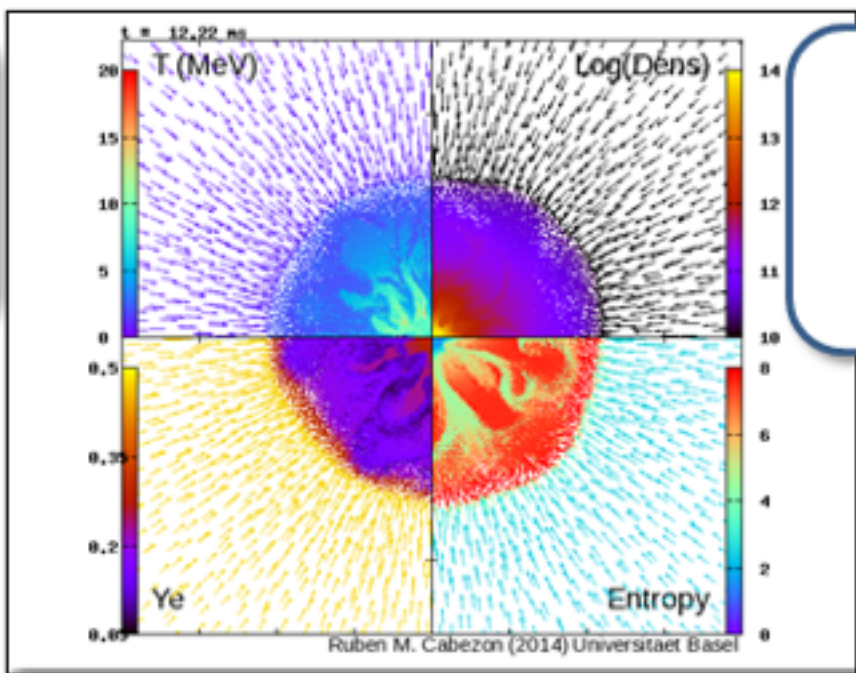


3D Code comparison



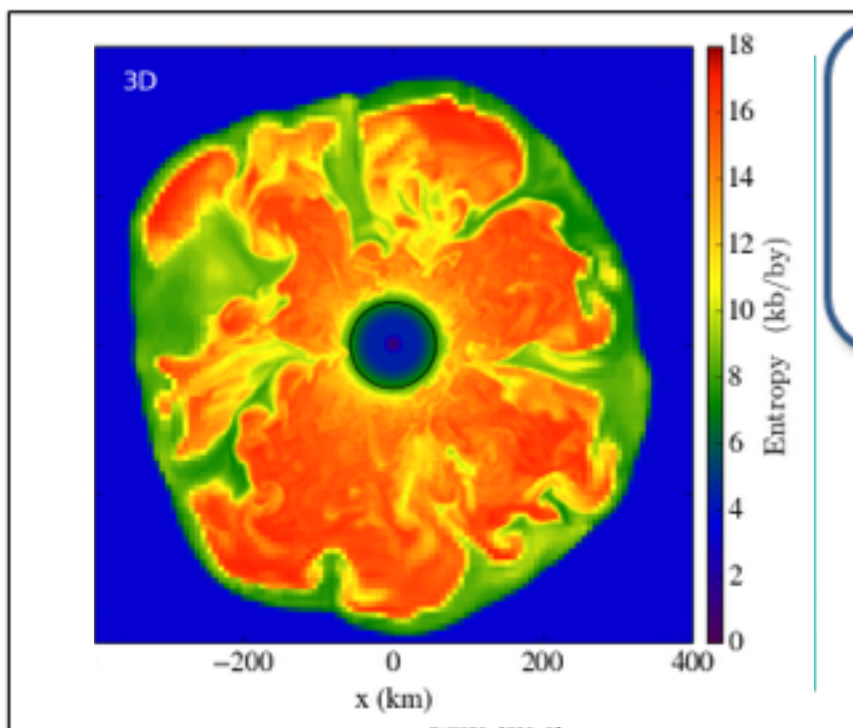
Elephant
 3D IDSA
 Cartesian mesh
 NR/ eff. GR

M. Liebendörfer
 S. C. Whitehouse
 R. Käppeli



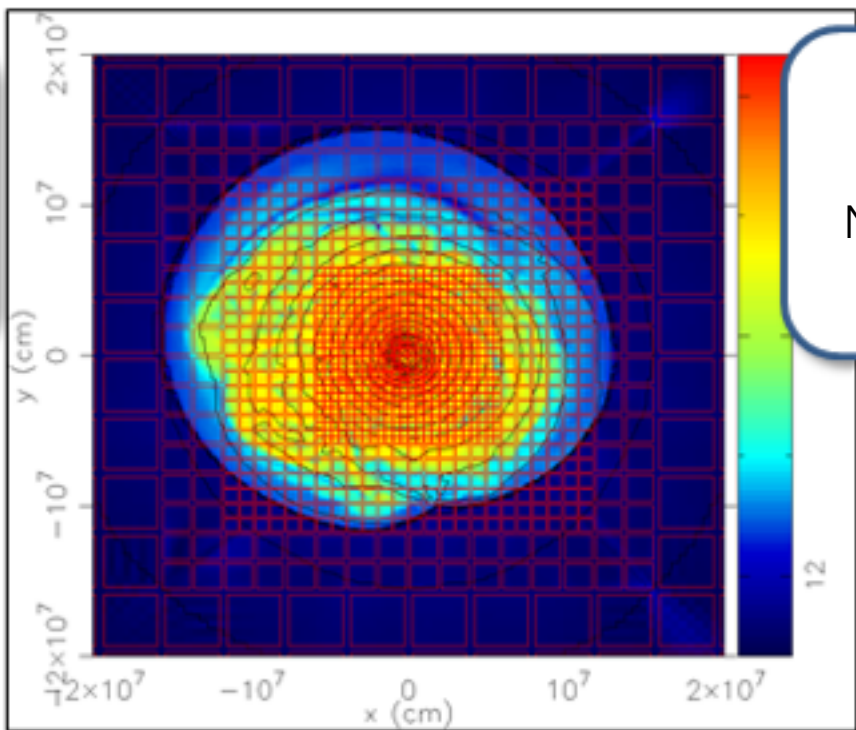
SPHYNX
 ASL/IDSA
 SPH
 3D Newtonian

R. M. Cabezón



FLASH
 1-3D IDSA
 AMR
 NR/eff. GR

K.-C. Pan



fGR_M1
 M1
 Nested meshes
 3D full GR

T. Kuroda

2D vs. 3D

Time = Time = 400 ms

