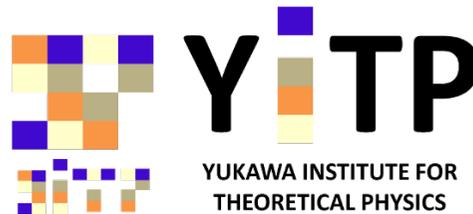


Setting stages: Status & issues of neutron-star binary merger in numerical relativity

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0 Background

- Numerical-relativity data are required for the coming observations.
- Numerical-relativity data will be tested for the next 5-10 yrs observation.
- Happy epoch will come.
- However, we need more carefulness and more efforts.

Major roles of numerical relativity for neutron-star binary mergers

1. **Deriving accurate gravitational waveforms:
clarifying dependence on EOS, mass, spin**
2. **Clarifying the remnant & its evolution:
Could it be central engine of short GRBs ?**
3. **Quantifying ejecta: mass, velocity,
temperature, neutron-richness (\rightarrow opacity)**

1 Gravitational waveforms: Inspiral

- **Goal:** Making an accurate template that depends on mass, spin, & EOS
- **Procedure:** Accurate numerical simulation
→ analytical or semi-analytical modeling
(e.g., by effective-one-body; Bernuzzi's talk)
- **Numerical relativists have to perform accurate simulations for a variety of mass, spin & EOS**

Current status in (my) understanding

Accurate simulations are getting possible:

- Eccentricity reduction for initial condition is crucial → getting standard: SXS, Kyoto, Jena, ..
- Long-term simulations are necessary: expensive but not problem for ~15-20 orbits → More ?? (although I don't think so)
- Taking convergence is a key (note that for hydro simulations, convergence is 3-4th order): Constraint propagation prescription is found to be robust for improving the convergence (e.g., Bernuzzi, Hilditch et al.)

Hydro results are at best, 3rd-4th-order convergence

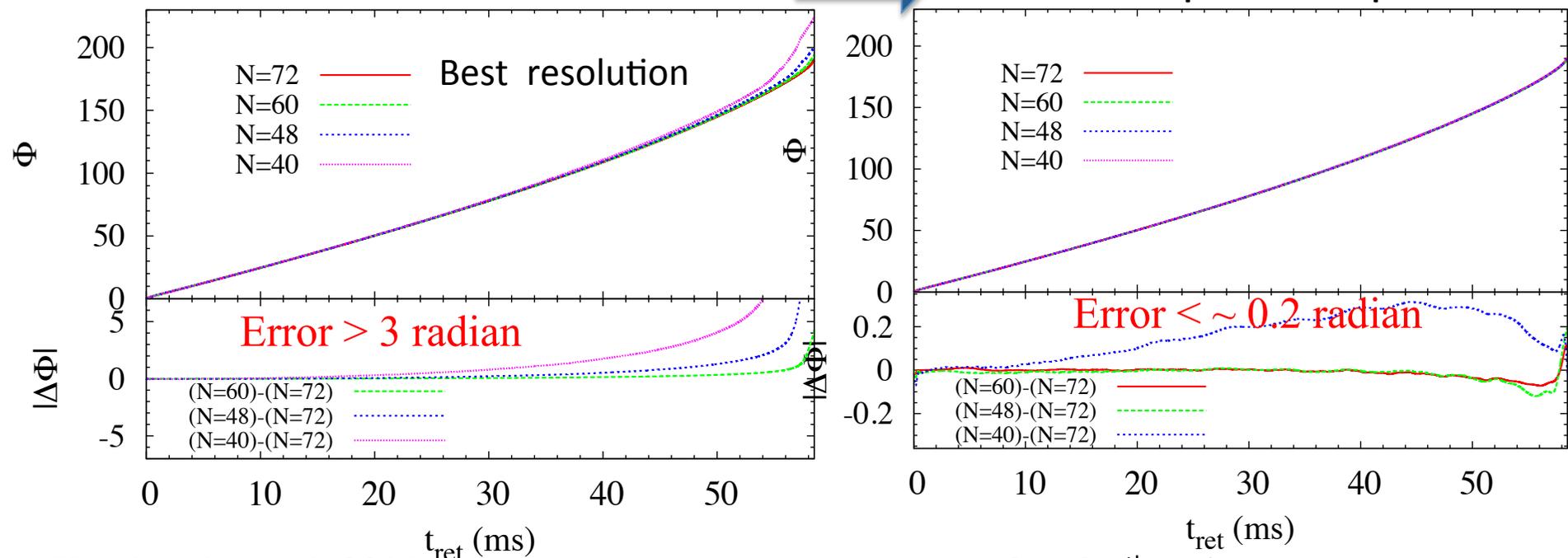
We can never obtain exact numerical waveform in hydrodynamics simulation !!

But, extrapolation can give an “almost” solution fortunately

$$t \rightarrow \eta t, \quad \Phi = \int 2\pi f d(\eta t)$$

Gravitational wave phase

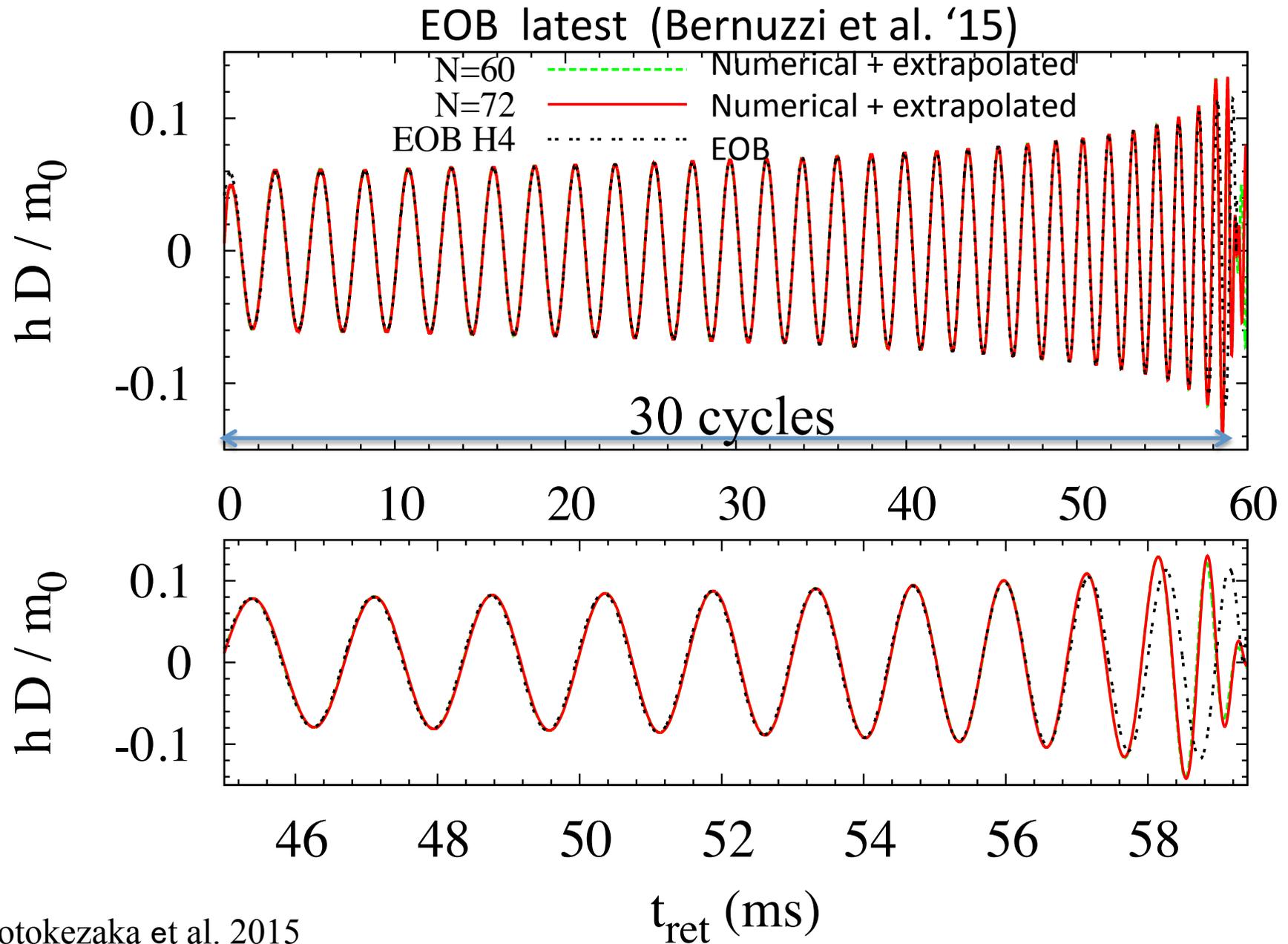
Extrapolated phase



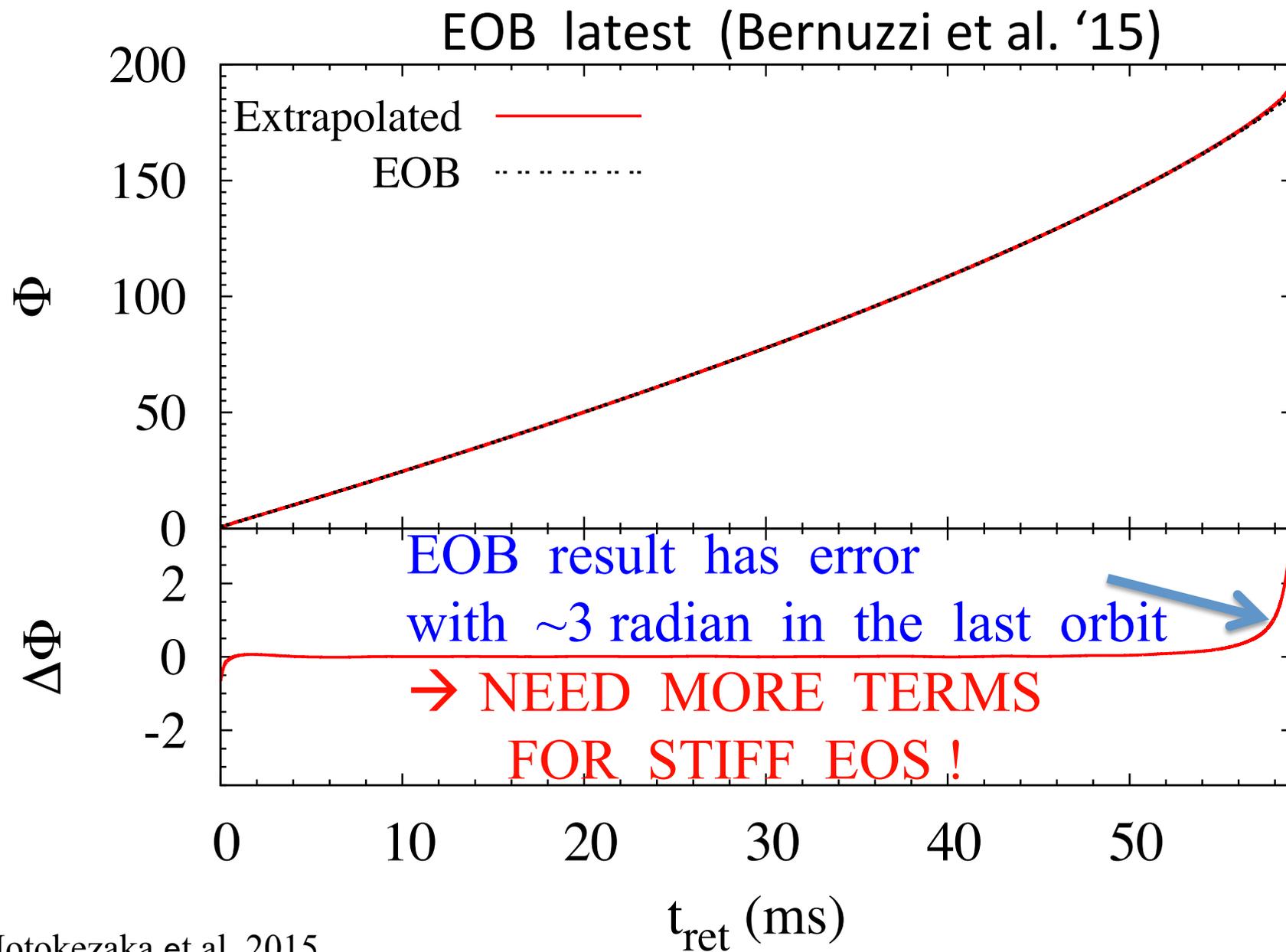
Hotokezaka et al. 2015 t_{ret} (ms)

$\sim 3.5 \pm 0.5^{\text{th}}$ -order convergence

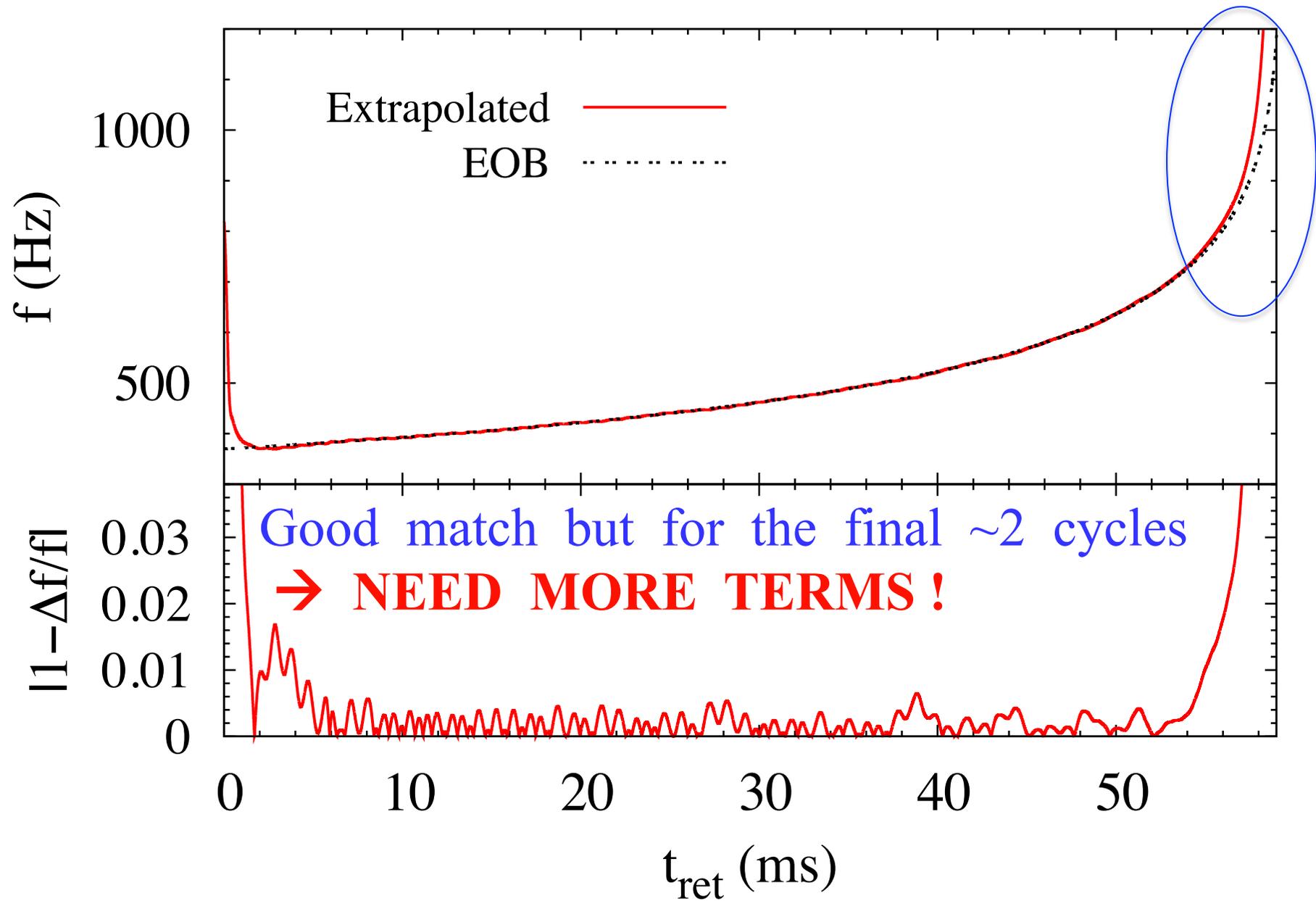
Extrapolated waveform vs EOB for R=13.6 km



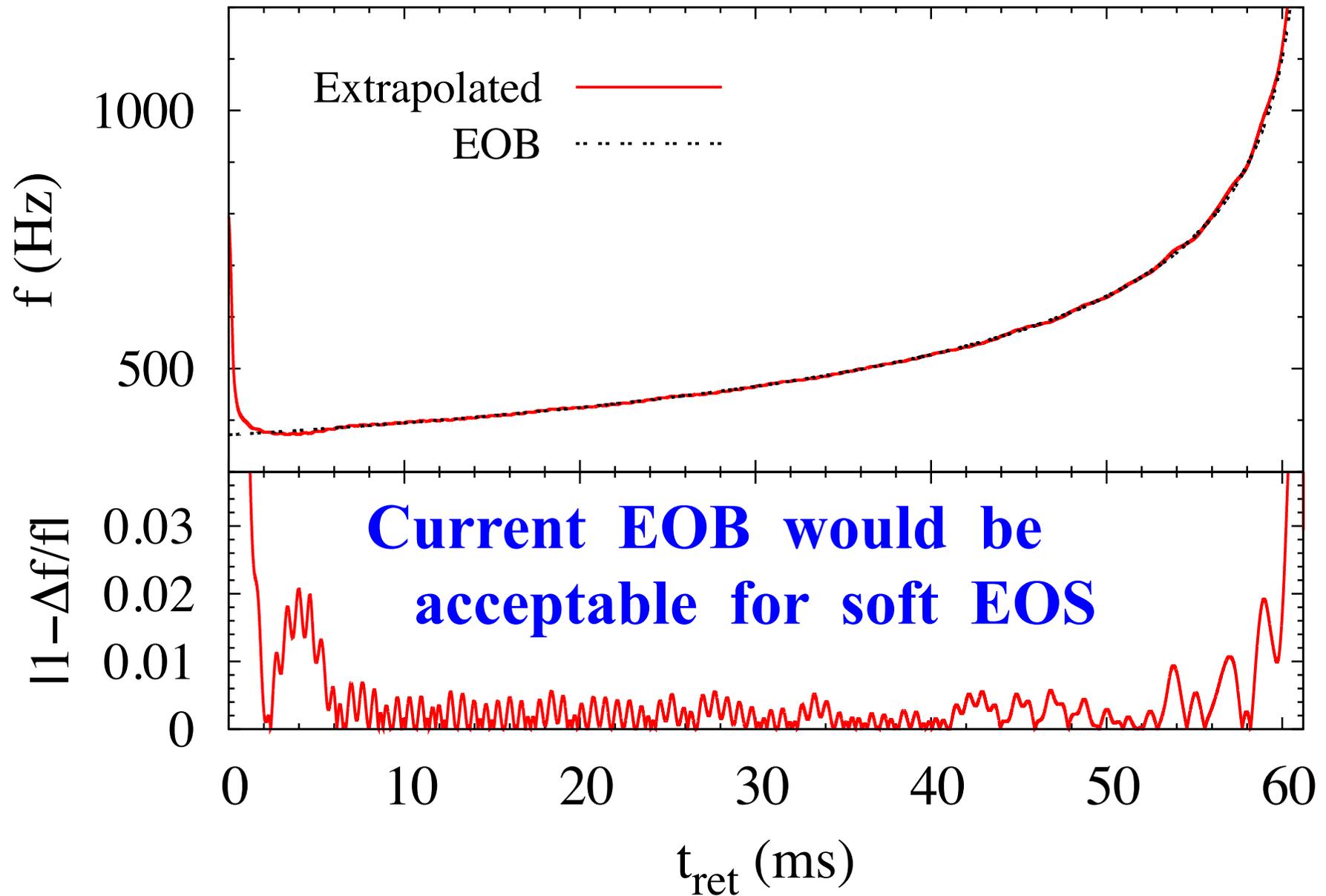
Comparison with effective-one-body approach



Comparison with EOB: frequency



Good match for R=11.1 km (APR4)

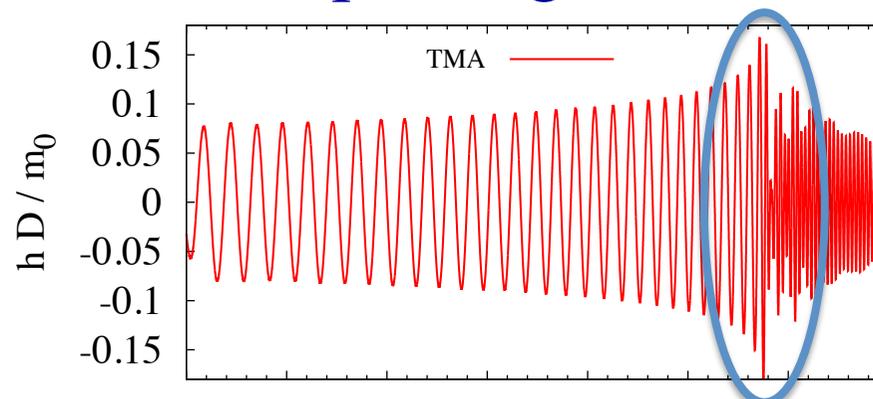


1 Gravitational waveforms: Inspiral

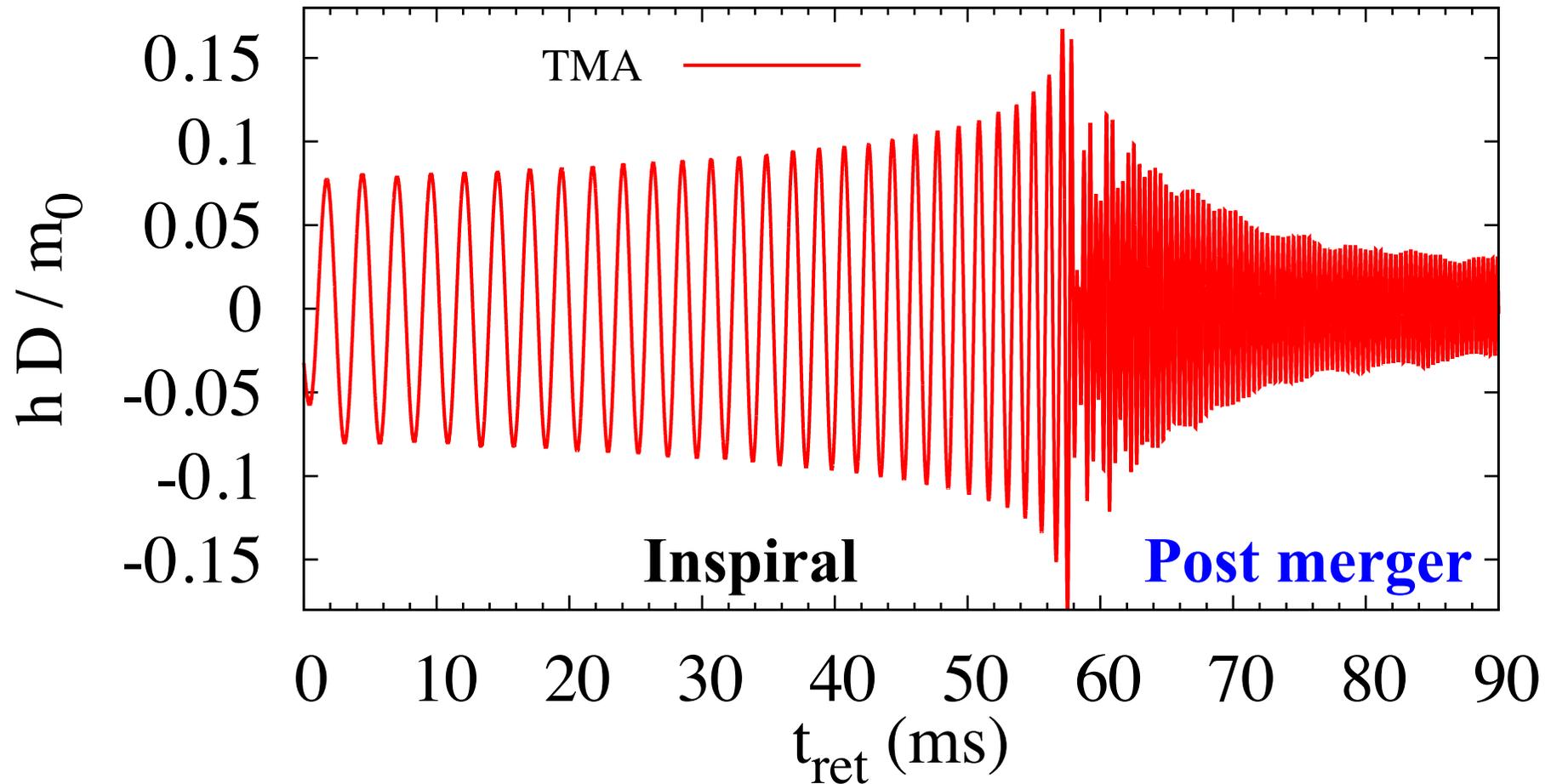
Issues

- EOB is promising (Bernuzzi's talk) but modeling by EOB + static tidal deformability is not enough:
→ + resonance ? (Hinderer et al.) + more ?
- Only a few accurate works for BH-NS (Foucart et al.)
→ need more systematic simulations for this
- How we model NS-NS inspiral + early *merger* waveform ?

This is crucial for improving of SNR for $f \sim 1\text{kHz}$



1 Gravitational waveforms: post Merger



- **Inspiral:** cold EOS, no shock heating, no MHD
- **Post merger:** Shock \rightarrow Hot, MHD, neutrinos ...

Issues

- **After merger = after shock heating**
- Effect of shock heating changes waveforms:
 $\Delta f \sim 0.1\text{kHz} ?? \rightarrow$ **need to clarify systematics**
- MHD/viscous effects may be important
- Effect of microphysics ? Neutrino cooling may play a role for long-term evolution.
- **Note : The latest universal relation argument usually ignores all these uncertainties**

\rightarrow Systematic error should be clarified

2 Merger & remnant

NS-NS: Typical remnant = massive neutron star for typical mass (e.g., $1.35-1.35 M_{\text{sun}}$ NS)

BH-NS: BH + torus (if NS is tidally disrupted)

Questions:

- How hyper/supramassive neutron stars evolve ?
- How resulting BH + torus evolve ?

More specifically:

- How is the neutrino effect ?
- How is the magnetohydrodynamics effect ?

Simulations for merger remnant

Current status:

- GR radiation hydro simulations are ongoing:
Leakage or M1 grey (Sekiguchi, Foucart, Palenzuela ...)
→ semi-quantitative study (quite interesting results)
- A high-resolution MHD simulation is ongoing:
Kiuchi et al. demonstrate high-resolution is crucial

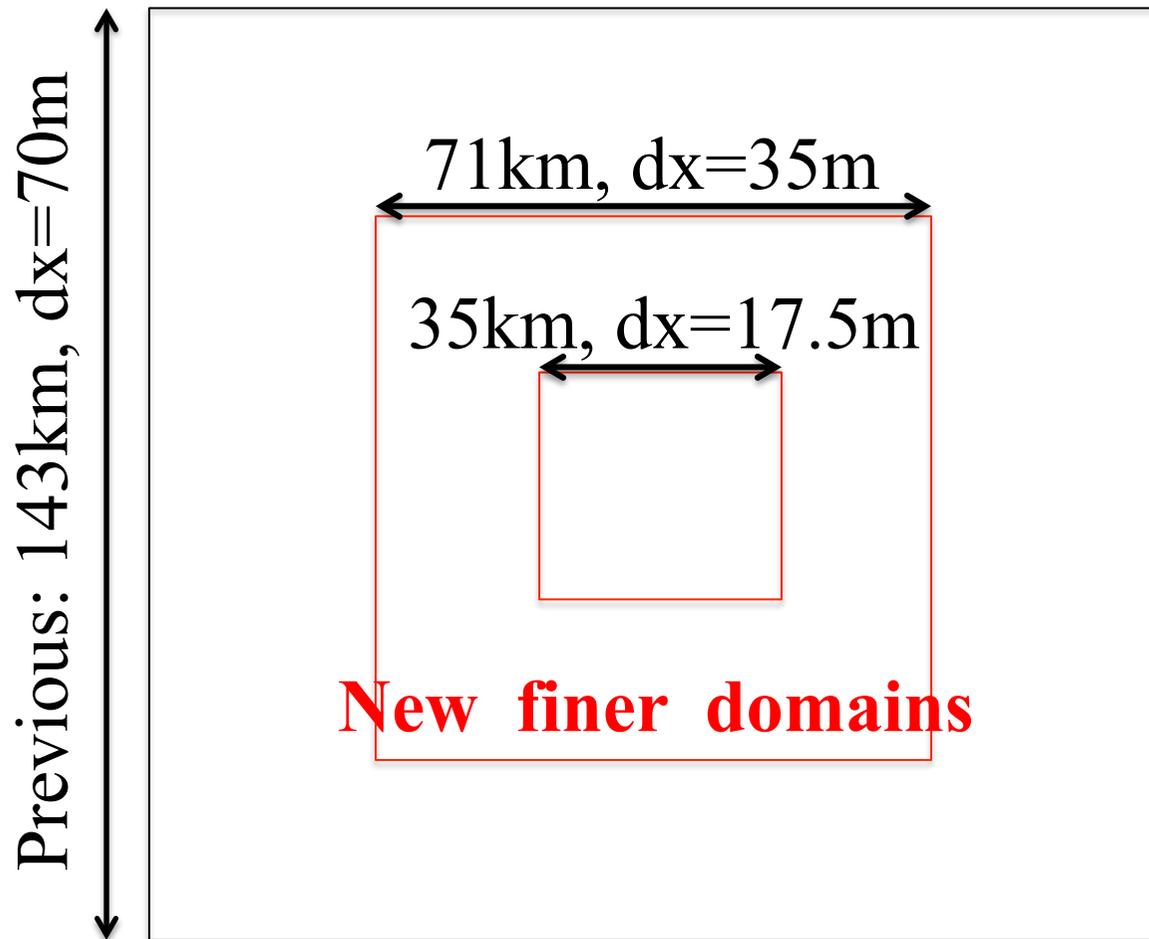
Questions:

- Are more detailed radiation transfer effects needed?
→ anyway, need try and comparison
- Probably, **radiation hydro + angular momentum transport effects** would be keys → GRRMHD ?
- For GRBs, pair-annihilation should be considered
(Just's talk)

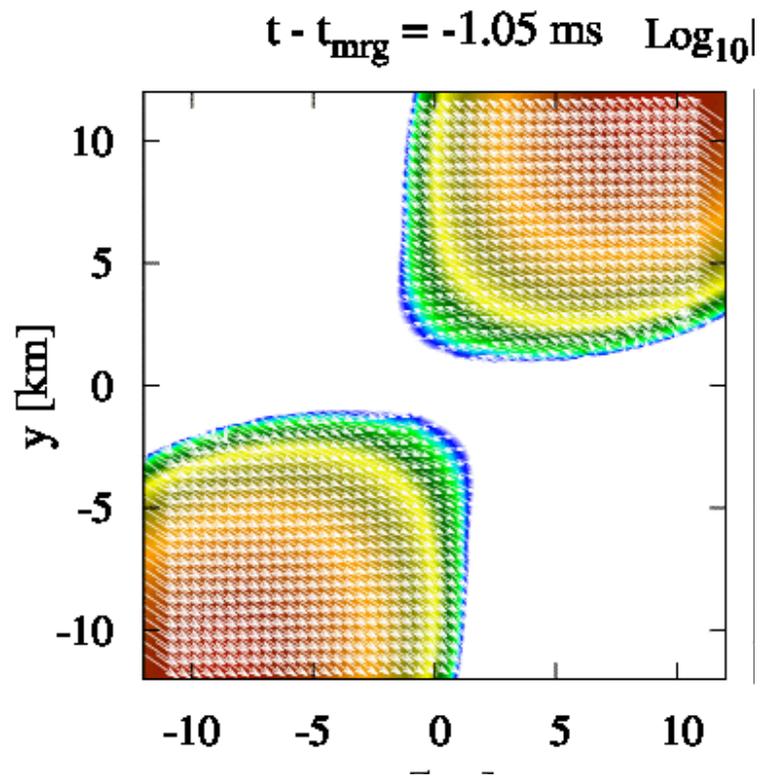
High-resolution GRMHD simulations

Kiuchi et al. 2015 in prep

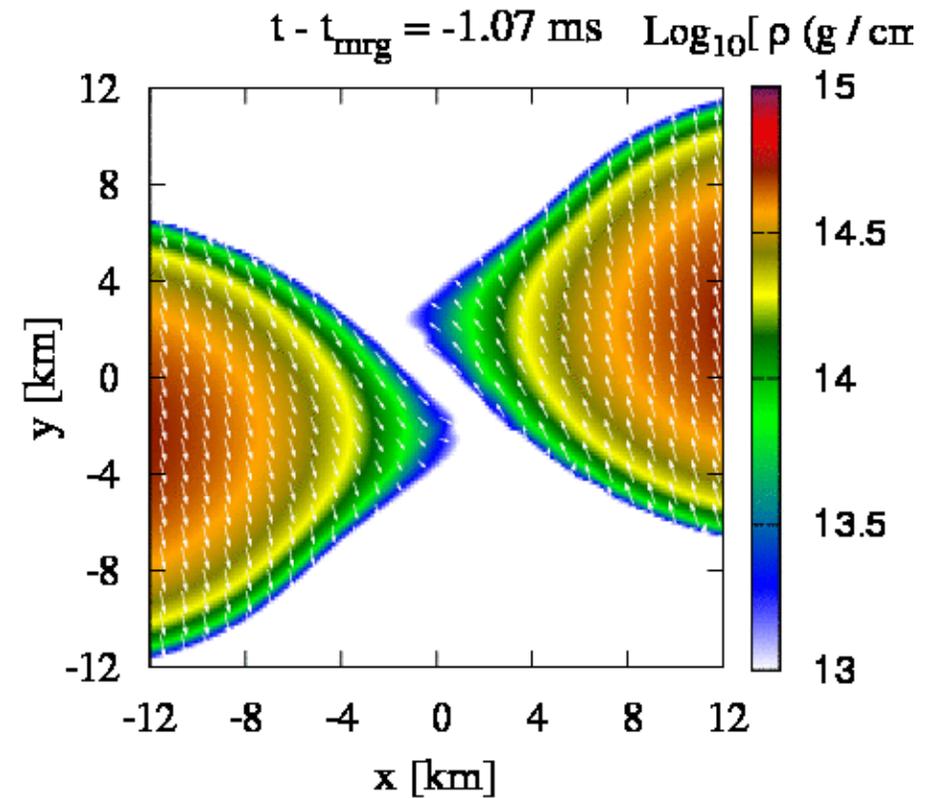
- Fixed mesh refinement: $dx=70\text{m} \rightarrow 35\text{m} \rightarrow 17.5\text{m}$



High-resolution GRMHD for NS-NS

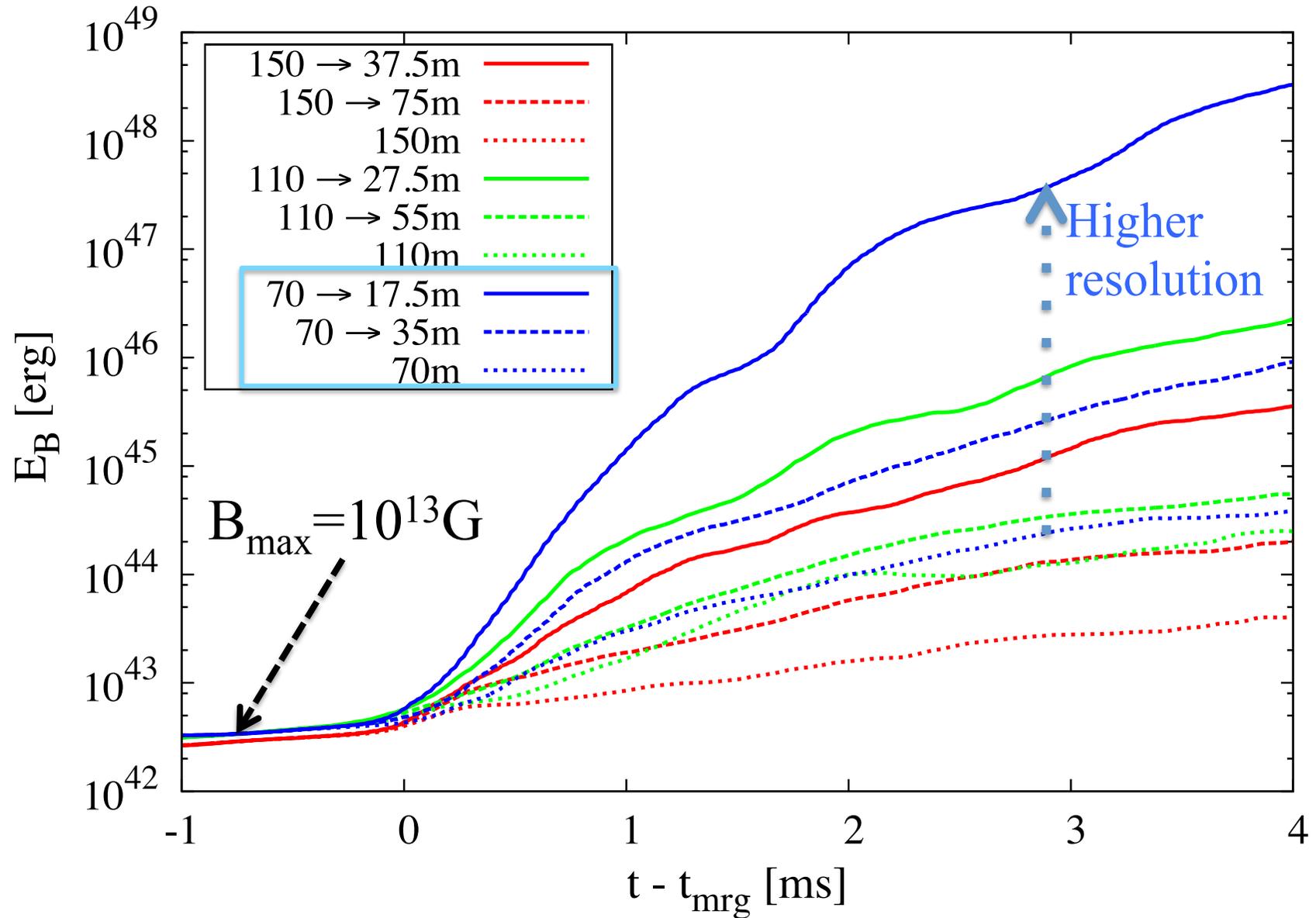


$\Delta x = 17.5 \text{ m}$

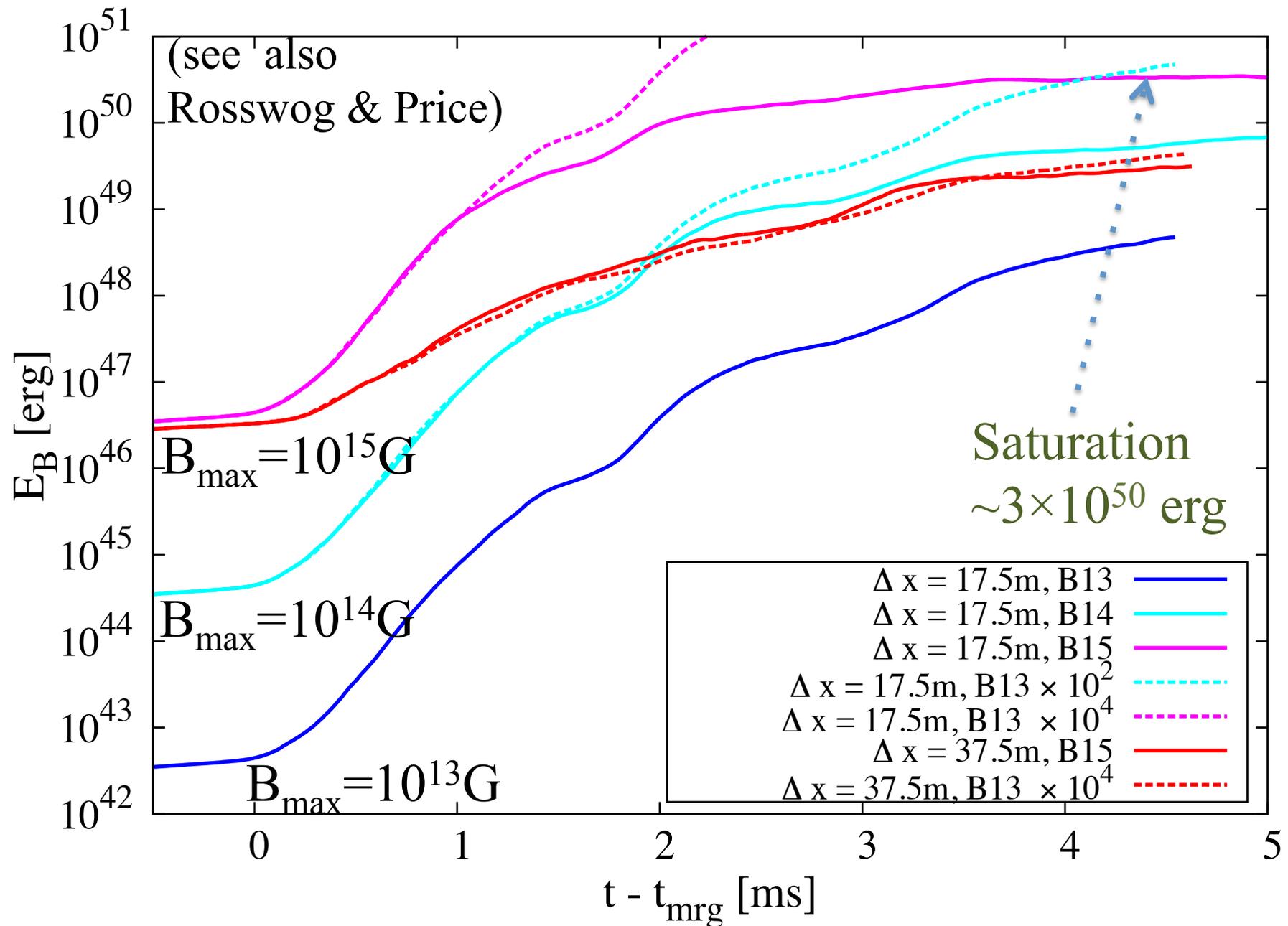


$\Delta x = 70 \text{ m}$

Magnetic energy: resolution dependence



Magnetic energy soon after merger



Merger remnant would be magnetized

Questions:

- Is highly magnetized remnant NS equivalent to highly viscous NS ?
- If so, how large is the effective viscosity ?
- High-resolution GRRMHD is the best one, but too expensive. Alternative approach ?
Sub grid models ? (Giacomazzo et al.)

Note: anyway, calibration is necessary for new ideas

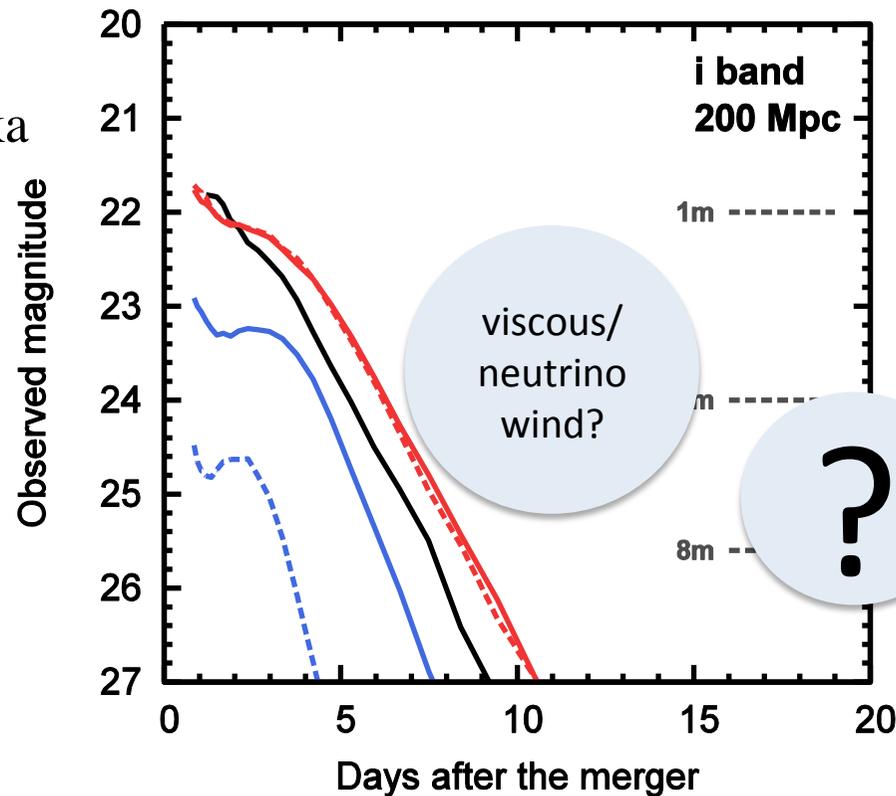
- How is magnetar (NS with force-free strong magnetic field) produced ?
→ Ultra long-term run is necessary

3 Merger & mass ejection

Detailed quantitative studies are awaited for an efficient macronova search

Tanaka & Hotokezaka
2013

SUBARU gives
only 2 nights
in this year



κ is really 10 ?

When we should observe ?

According to Li-Paczynski (ApJ, 1998)

Maximum Luminosity @ $R/v = R^2 \rho \kappa / c$:

$$L_{\max} \sim 4 \times 10^{41} \text{ ergs/s} \left(\frac{M}{0.01 M_{\odot}} \right)^{1/2} \left(\frac{v}{0.2c} \right)^{1/2} \left(\frac{\kappa}{10 \text{ cm}^2 / \text{g}} \right)^{-1/2} \left(\frac{f_{\text{r-proc}}}{3 \times 10^{-6}} \right)$$

$$\text{at } t \sim 5 \text{ days} \left(\frac{M}{0.01 M_{\odot}} \right)^{1/2} \left(\frac{v}{0.2c} \right)^{-1/2} \left(\frac{\kappa}{10 \text{ cm}^2 / \text{g}} \right)^{1/2}$$

$$3 \times 10^{41} \text{ ergs/s} \Leftrightarrow M = -15.0 \text{ mag} \Rightarrow \underline{\underline{m = 21.5 \text{ mag @ 200Mpc}}}$$

- These depend strongly on *mass, velocity, & opacity*
- Opacity $\sim 10 \text{ cm}^2/\text{g}$ for 2nd--3rd peak elements

(Barnes & Kasen, Tanaka & Hotokezaka 2013)

Mass ejection mechanisms

- Dynamical ejection by tidal torque (Rosswog, ..)
- Dynamical ejection by shock heating with GR gravity (Hotoke+, Bauswein+)
- Ejection by viscous wind from torus surrounding a black hole (Fernandez-Mezger, Just+, ...)
- Ejection by neutrino heating (Dessart+, Perego+,...)
- Ejection by magnetohydrodynamics (Kiuchi+)
- **All these effects could play important roles**

Ejecta property

Dynamical ejection

- NS-NS: Mass $\sim 0.001-0.02 M_{\text{sun}}$ depending on EOS, $v/c \sim 0.15-0.25$, $\langle Y_e \rangle \sim 0.1-0.4$
- BH-NS: Mass $\sim 0-0.1 M_{\text{sun}}$, $\langle Y_e \rangle < 0.1$

Viscous ejection from torus

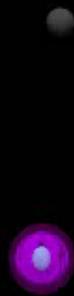
- Mass $\sim 0.001-0.01 M_{\text{sun}}$ depending on viscous parameter, initial velocity profile: **uncertainties**
- Velocity $< \sim 0.1c$, mildly neutron-rich

Neutrino heating

- Mass $\sim 0.001-0.01 M_{\text{sun}}$ depending on source model (**uncertainty**)
- Velocity $< \sim 0.1c$
- Mildly neutron rich is the result (Perego's talk)

BH-NS: Mass ratio=4, BH spin $a=0.75$

t = 0.0000 ms



$10^{14.0}$ G

$10^{14.5}$ G

$10^{15.0}$ G

Simulation by “K” computer: Kiuchi et al.

Need self-consistent & systematic study

- **Very long-term self-consistent simulation for merger and remnant evolution is necessary**
- **Both angular momentum transport effect & neutrino transport are the keys for the evolution of remnant**
 - **long-term GRRMHD simulation is awaited** (targets for exa-scale computer) or some effective model simulation ?
- **Not only optimistic suggestion but also the systematic study is necessary for observers:**
Should clarify the possible systematic error bar

Summary

- Numerical-relativity data will be tested for the next 5-10 yrs observation !
- Happy epoch will come soon



- We need more careful and systematic numerical simulations by many groups

**Announcement
from Yukawa Institute,
Kyoto University**

- **Long-term workshop on
“Nuclear Physics, Compact Stars,
Compact-star mergers 2016”
Oct.17 (Mon.) -- Nov.18 (Fri.), 2016.**

Neutron-unrichness (Y_e) and opacity ?

- Is abundance pattern of r-elements similar to solar pattern ?
- Lanthanides (2nd peak) are significant for increasing the opacity (Kasen+, Tanaka+)
- **Are the 3rd-peak elements significant to increase opacity ?**

