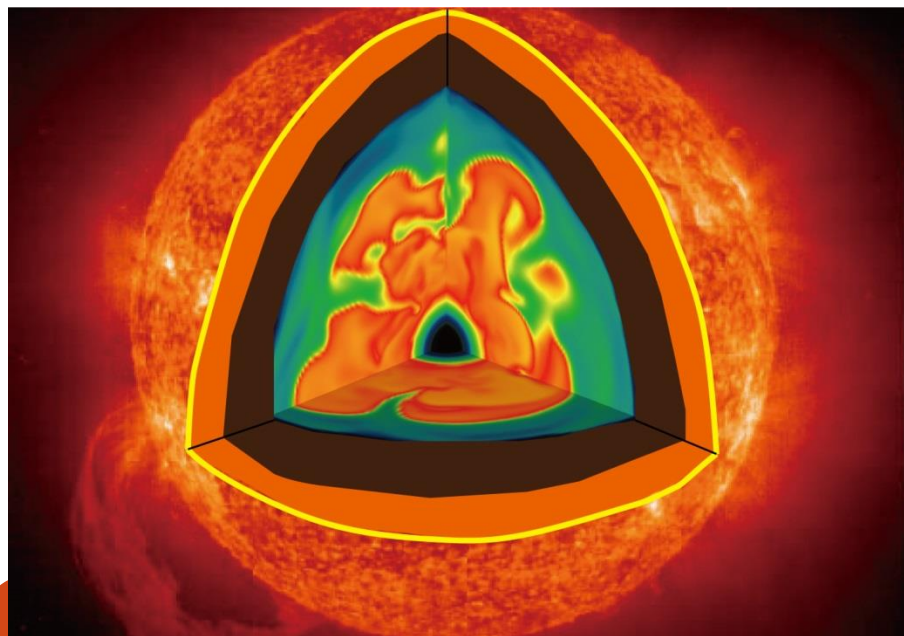


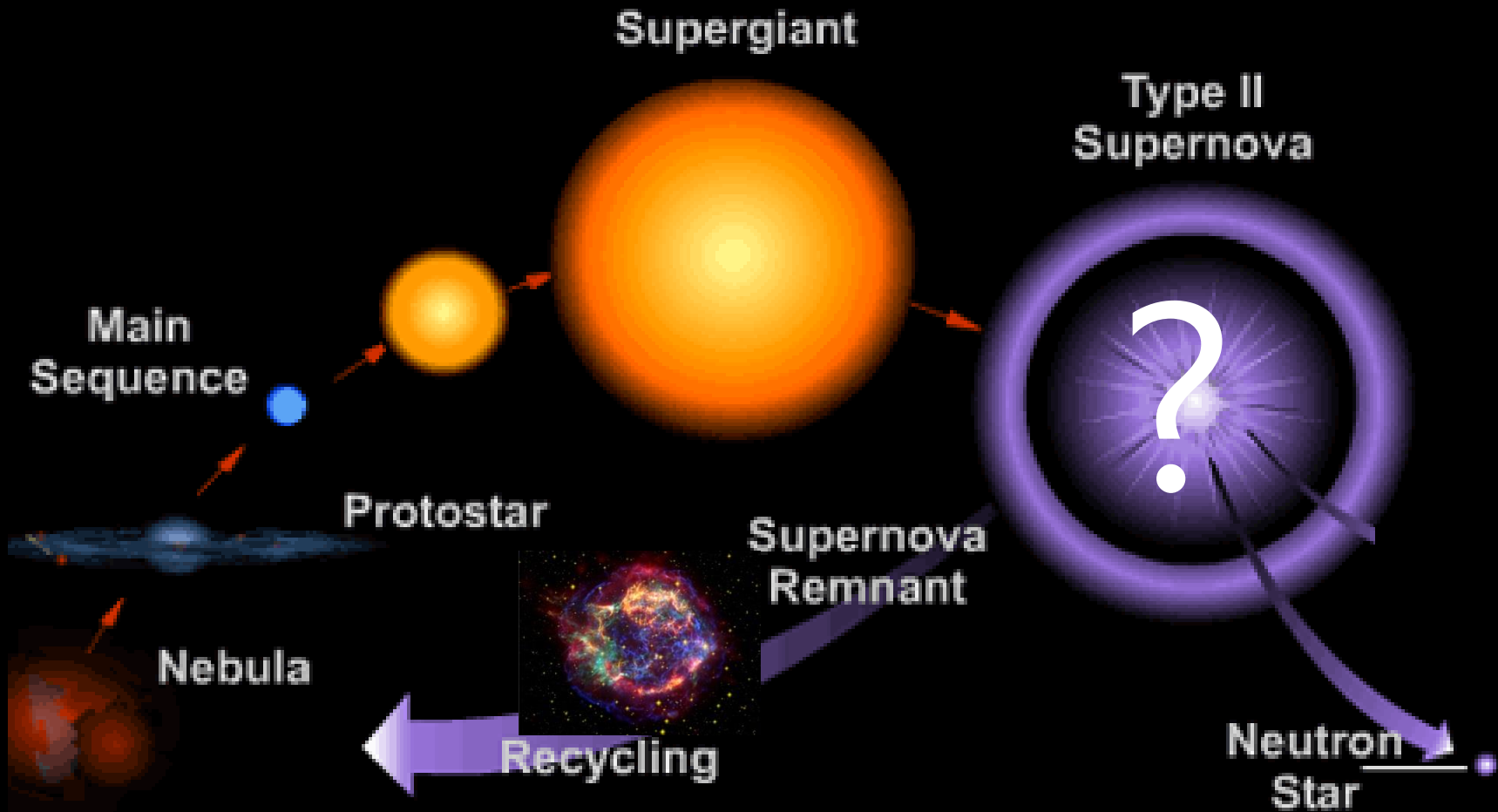
How supernova simulations are affected by input physics



Tomoya Takiwaki
(RIKEN)

Kei Kotake(Fukuoka)
Yudai Suwa(Kyoto/MPA)

Supernovae: the death of the star



Q:How does the explosion occur?

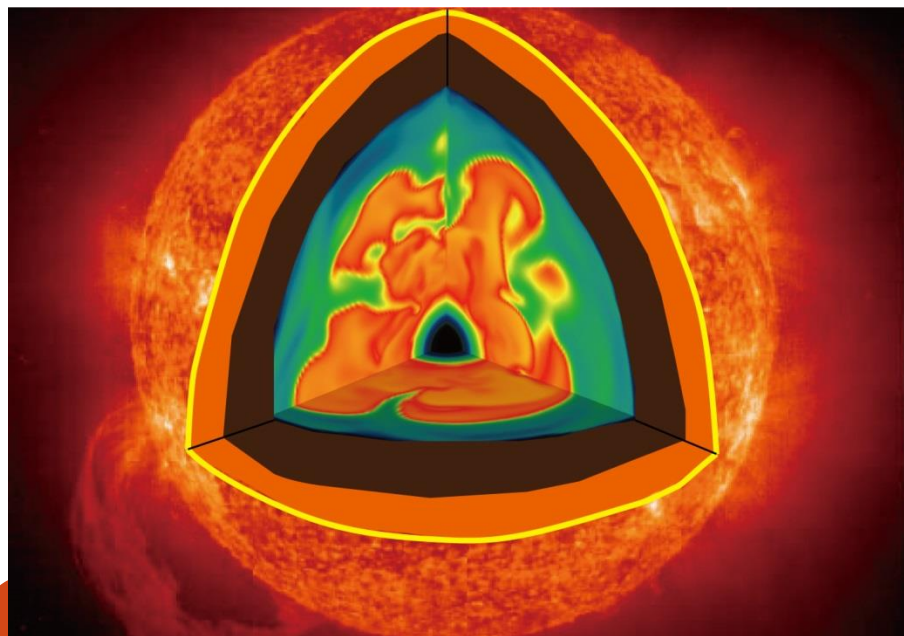
Important gradients for SNe Simulations

- **Gravity** (Newtonian/Phenomenological GR/CFC GR/GR)
- **Neutrino Reaction and Transport**
- **Equation of State**
- **Turbulent and Instability(1D/2D/3D)**
- **Progenitor**

Important gradients for SNe Simulations

- ~~Gravity~~ (Newtonian/Phenomenological GR/CFC GR/GR)
- ~~Neutrino Reaction~~ => Deep discussion will be given in Friday.
- ~~Equation of State~~
- Turbulent and instability(1D/2D/3D)
- Progenitor

How supernova simulations are affected by "initial condition"

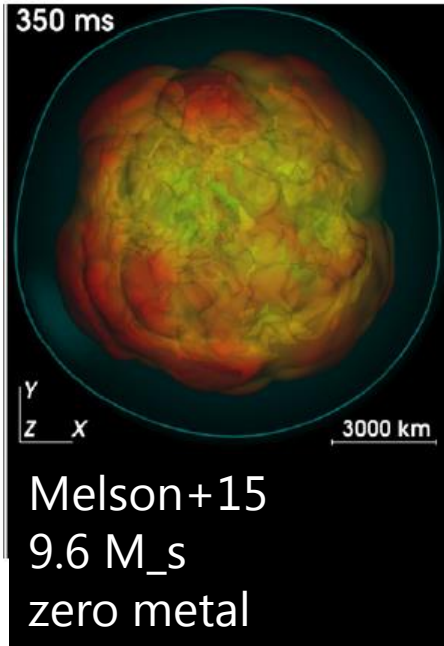


Tomoya Takiwaki
(RIKEN)

Kei Kotake(Fukuoka)
Yudai Suwa(Kyoto/MPA)

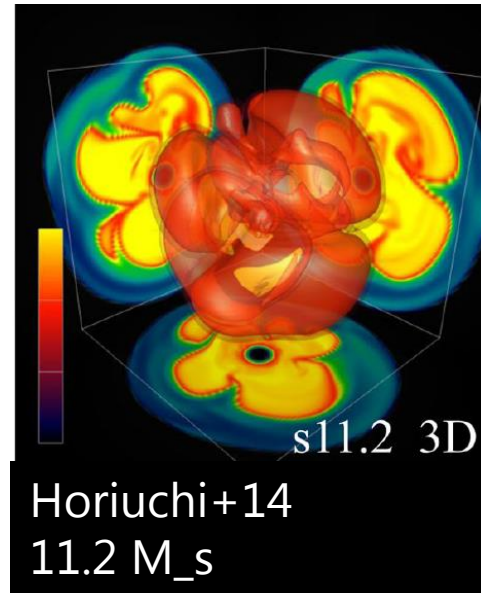
Current Status of SNe Mechanism

$M < 10M_s$



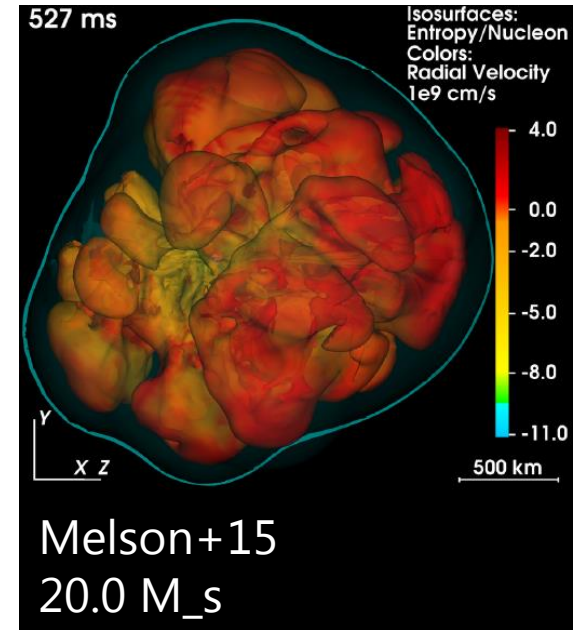
Dilute outer layer
Only ν -heating

$M < 15M_s$



ν -heating and
convection

$M < 40M_s$



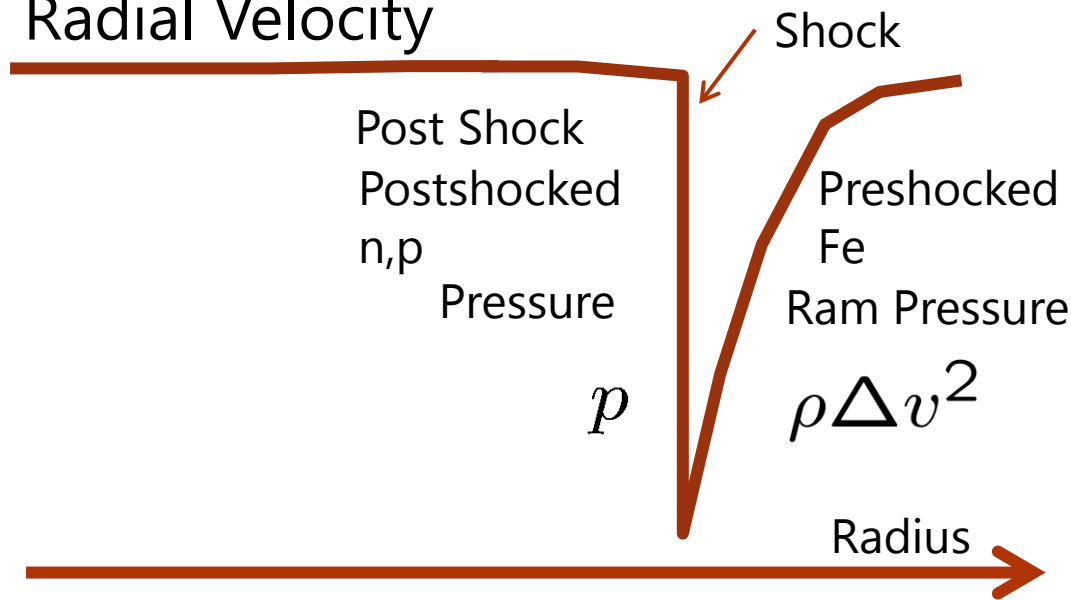
ν -heating, convection
and SASI

Self-consistent 3D simulations with MG ν -transport are available. Different mechanisms are found in different environment.

Typical 1D simulation

Key aspects of Neutrino Mechanism

Radial Velocity

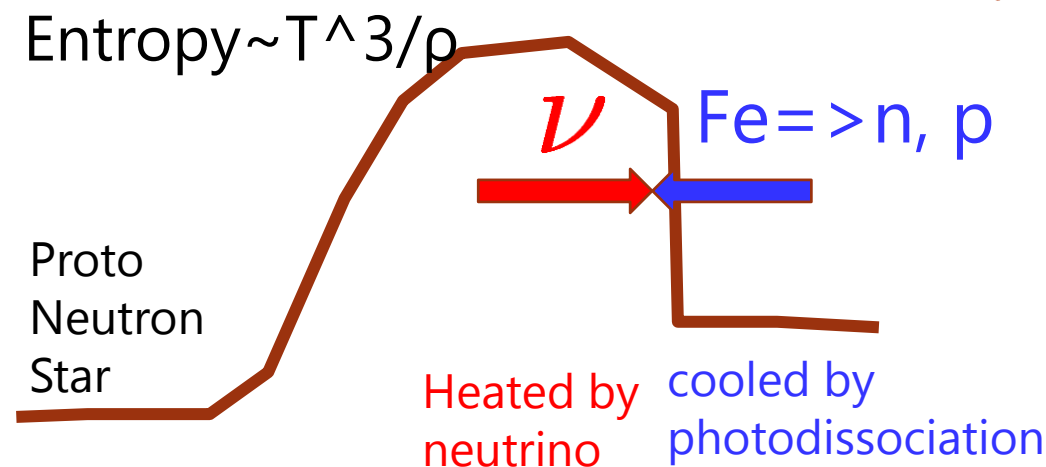


The shock is stalling.
Pressure inside and ram
pressure out side balances.

$$p = \rho \Delta v^2$$

RHS is determined by stellar
structure (density profile).

Entropy $\sim T^3/\rho$



LHS is determined by two
ingredients.

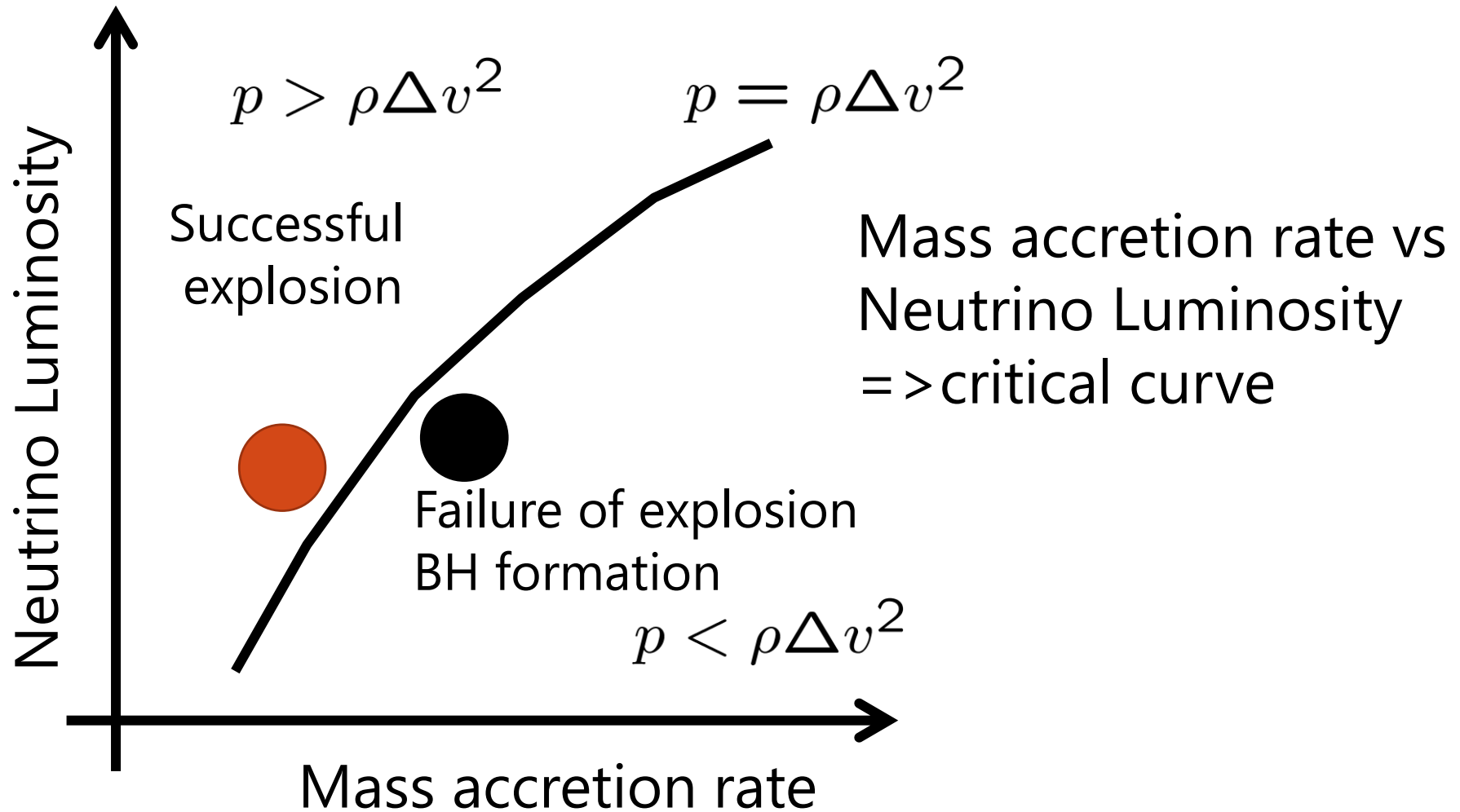
(1) Photodissociation



(2) Neutrino Heating

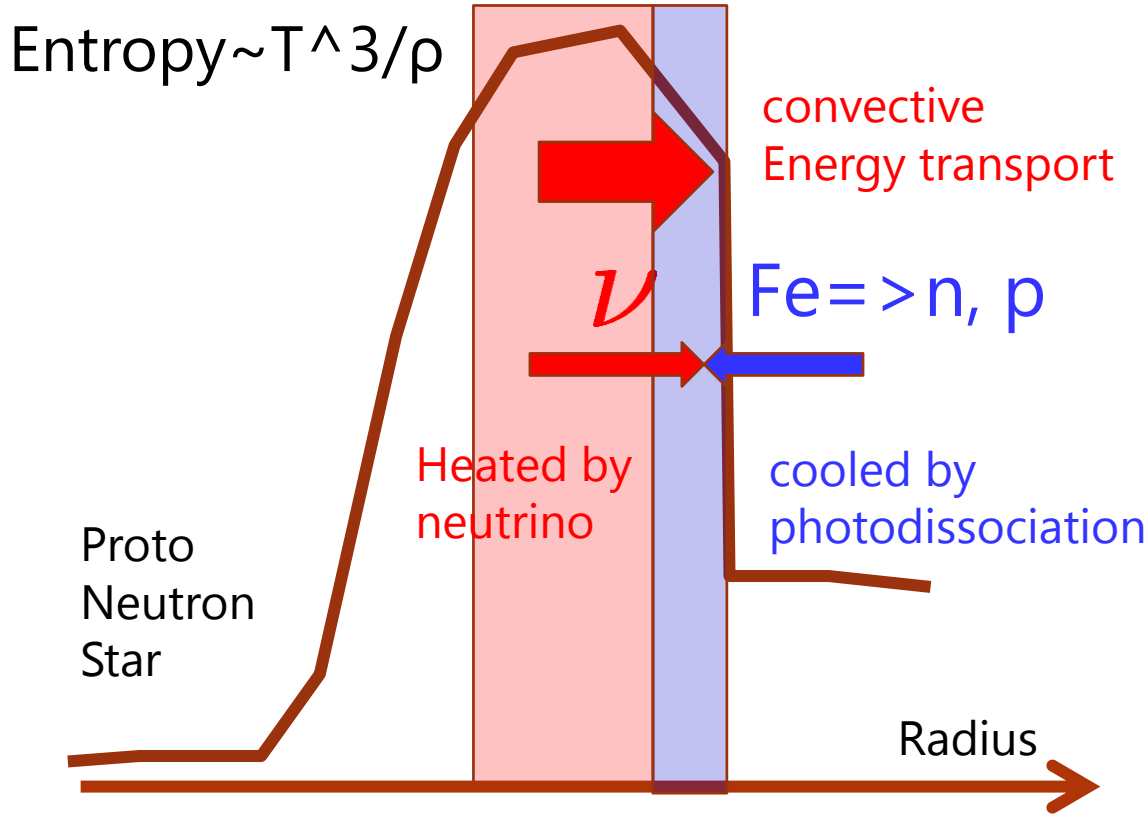


Mass accretion vs neutrino heating



From 1D to 3D

Key aspects of Neutrino Mechanism

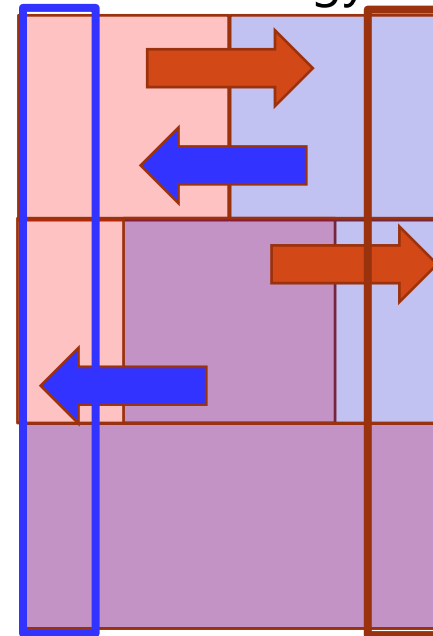


Cooler than the initial state but ν heat is active

Negative entropy gradient leads Rayleigh-Taylor instability

(Cold heavy matter is put over Hot light matter)

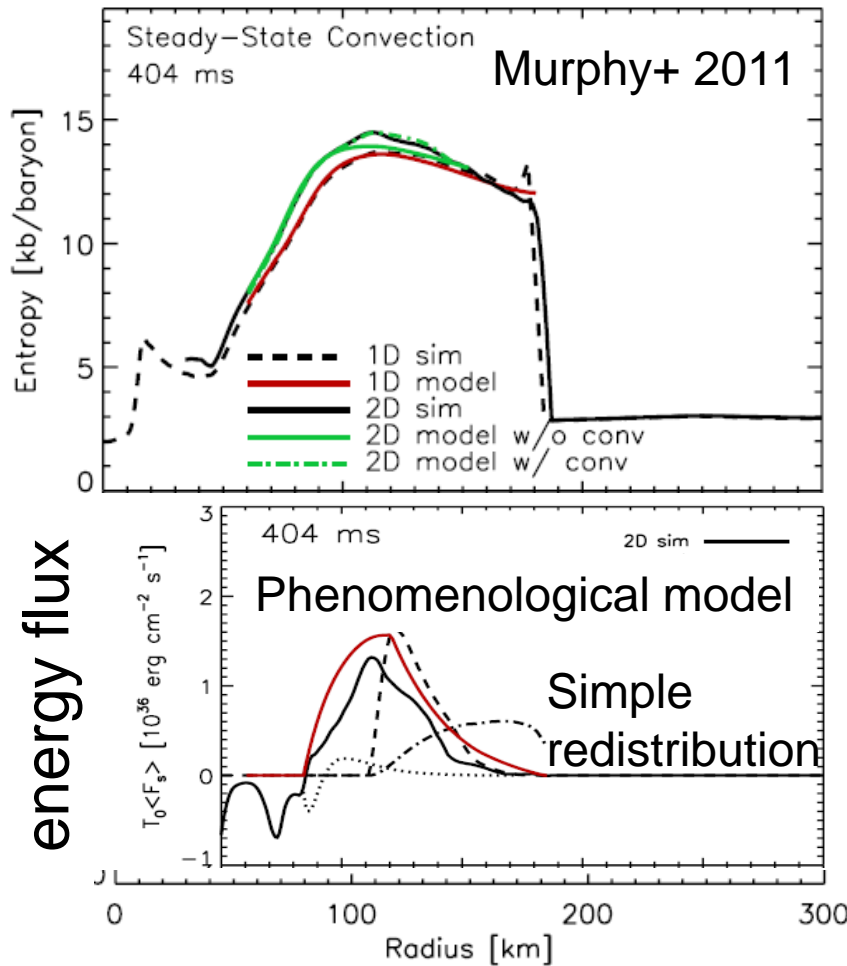
Rayleigh-Taylor convection transfer energy outward.



Hotter than the initial state

Question on ν -driven convection

Convective
energy flux



- Do we reproduce real energy transport?
 - Not obeying simple redistribution of entropy. Effect of ν -heating should be considered.
 - Is our resolution and hydro-method enough to capture the feature correctly?
- => see David Radice's talk

S A S I (Standing accretion shock instability)

Advective-acoustic cycle



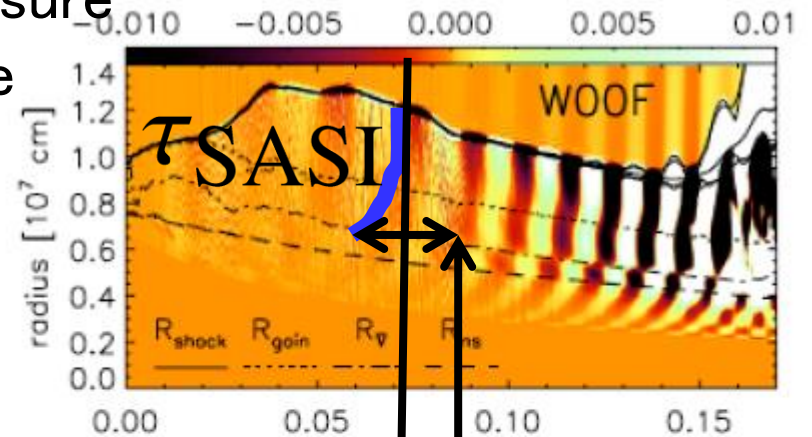
Foglizzo's slides

Standing Accretion Shock Instability (SASI)

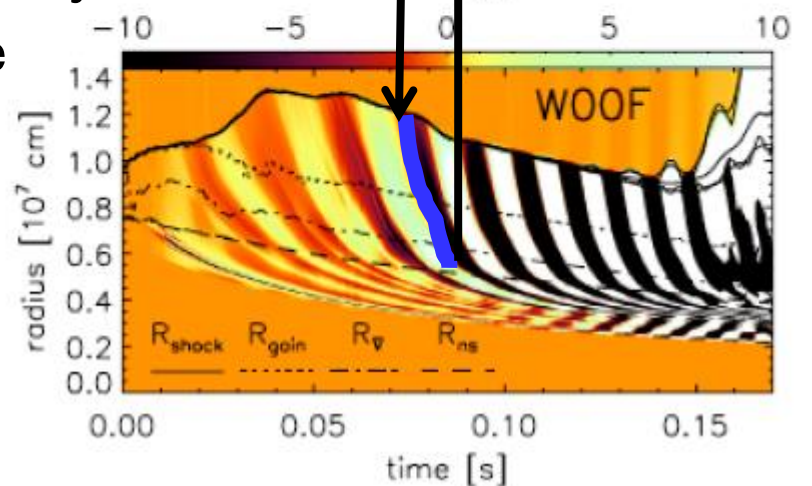
$$\tau_{\text{SASI}} \sim R_{\text{sh}} / v_r$$

$\dot{M} \uparrow, v_r \uparrow, \tau_{\text{SASI}} \text{ Rapid!}$

Pressure Wave

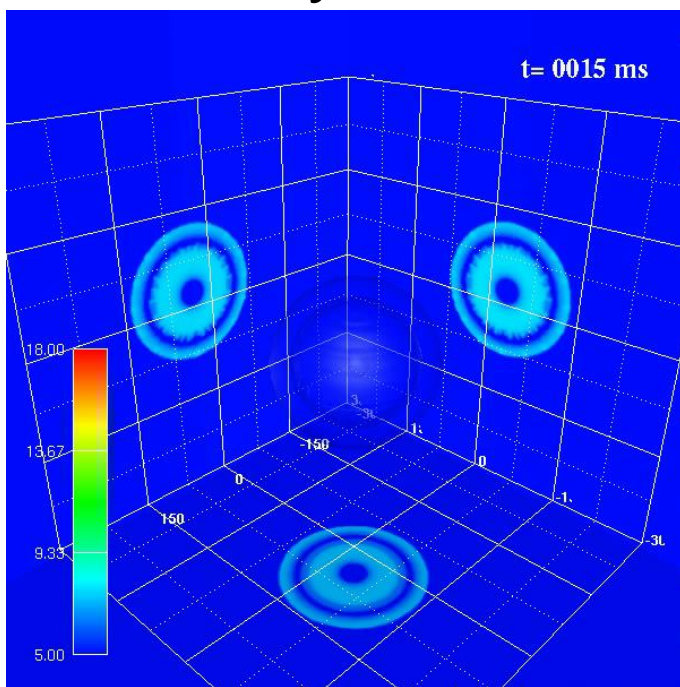


Vorticity Wave

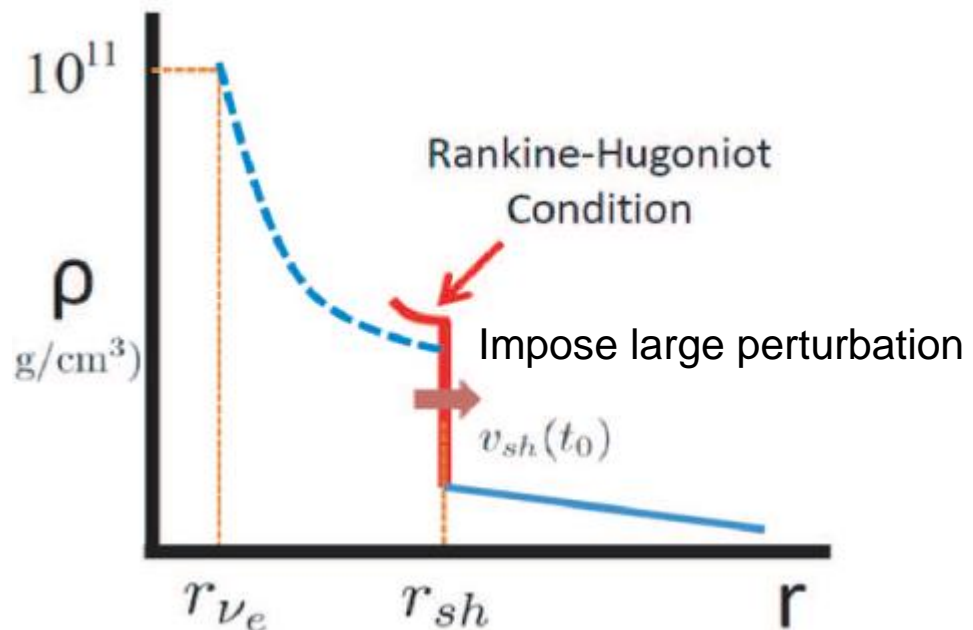


SASI

2D Axi-symmetric



Takiwaki+2012

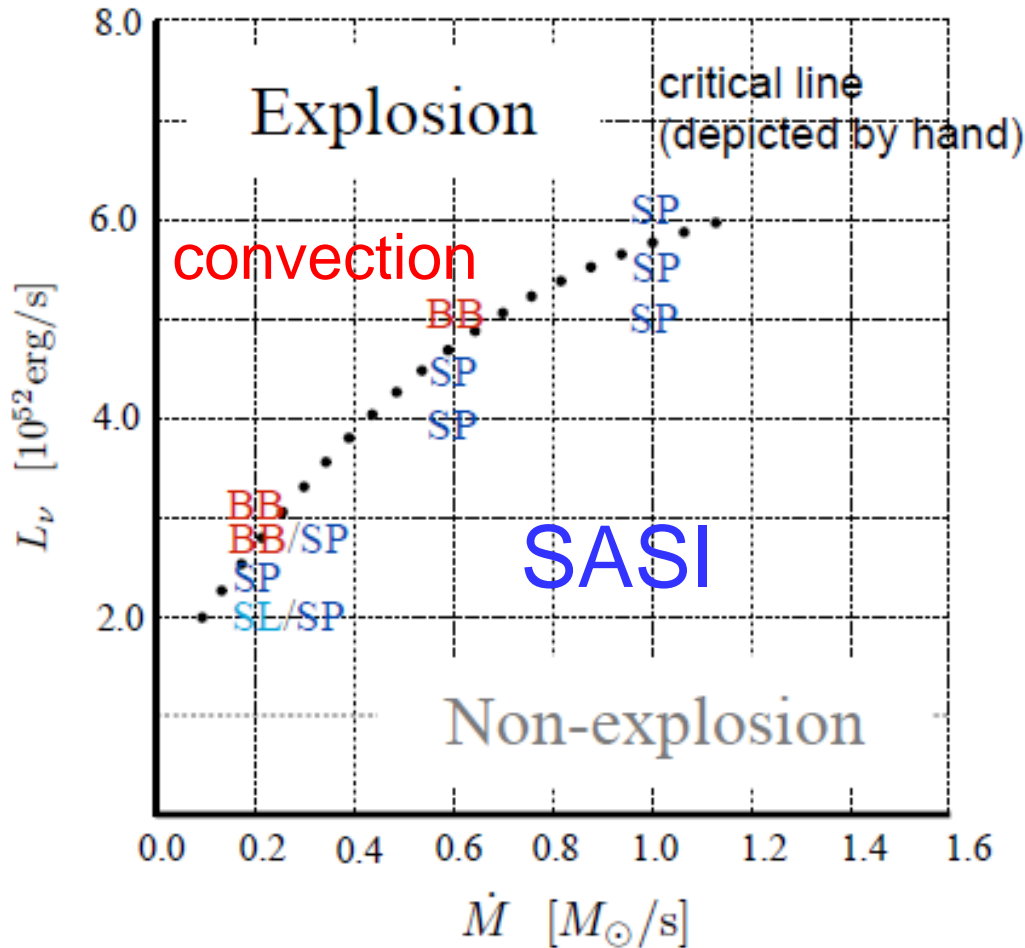


$$f_{crit} \sim 0.8 \times (M_{in}/1.4M_{\odot}) \times \{1 - (r_{sh}/10^8\text{cm})\}$$

Nagakura+2012

SASI focus energy at one direction!
~70% of increase in total pressure can
revive the shock.

Dominant instability in \dot{M} - L_ν plane



=> Light progenitor

Neutrino driven convection grows under low mass accretion rate.

=> Heavy progenitor

SASI grows under high mass accretion rate.

Question:

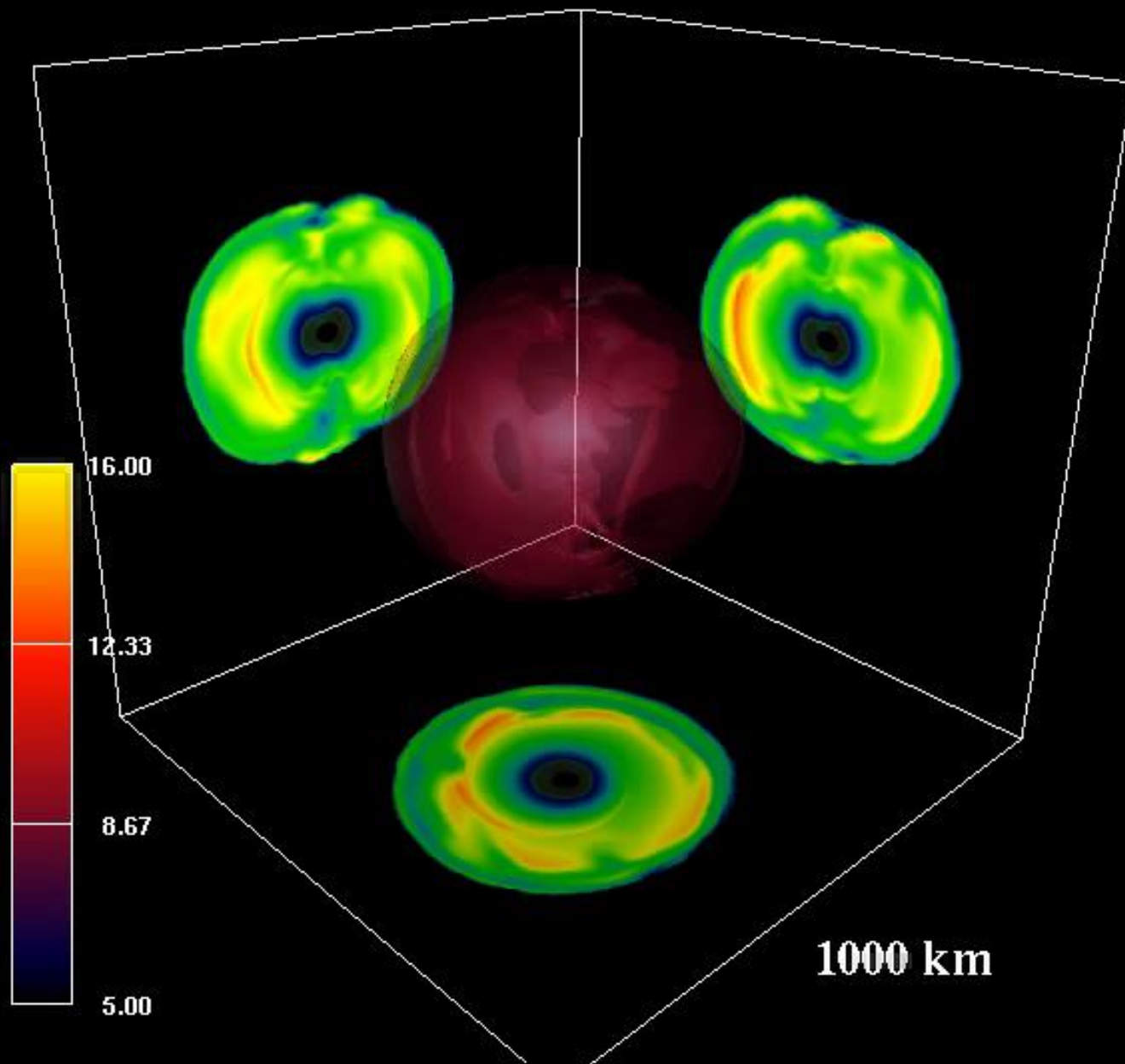
Is this expectation true?

3D model with rotation

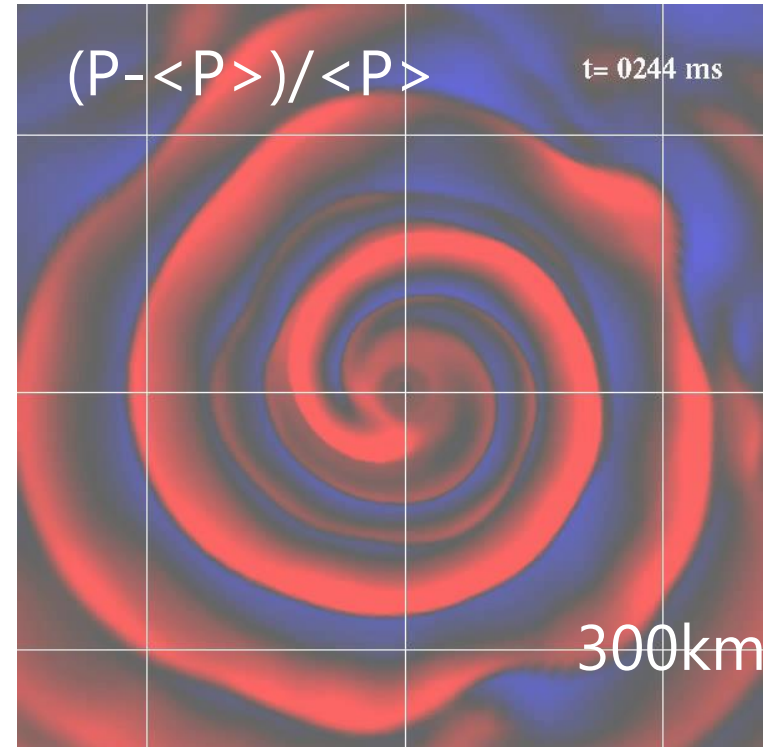
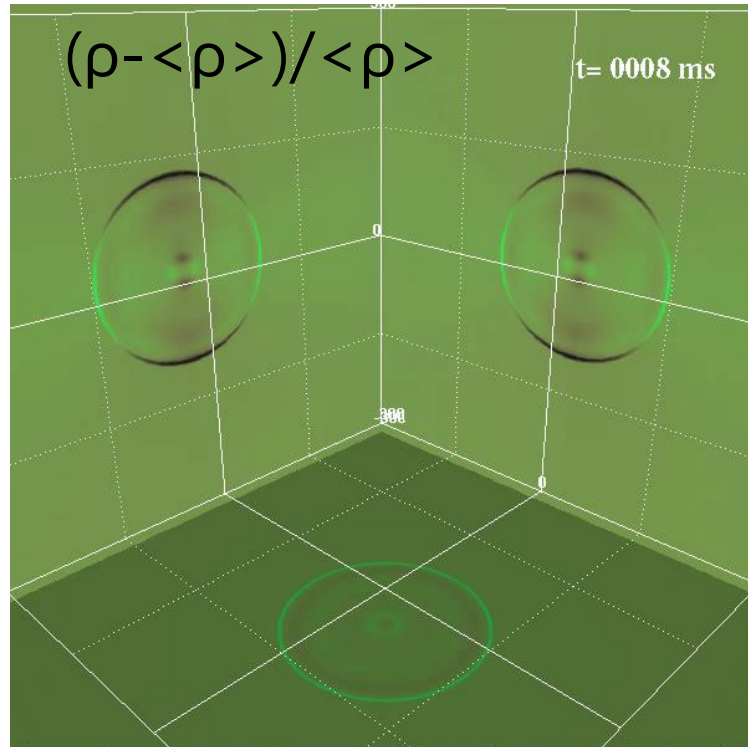
27.0M_s R2.0

Entropy

t= 0102 ms



Spiral Mode



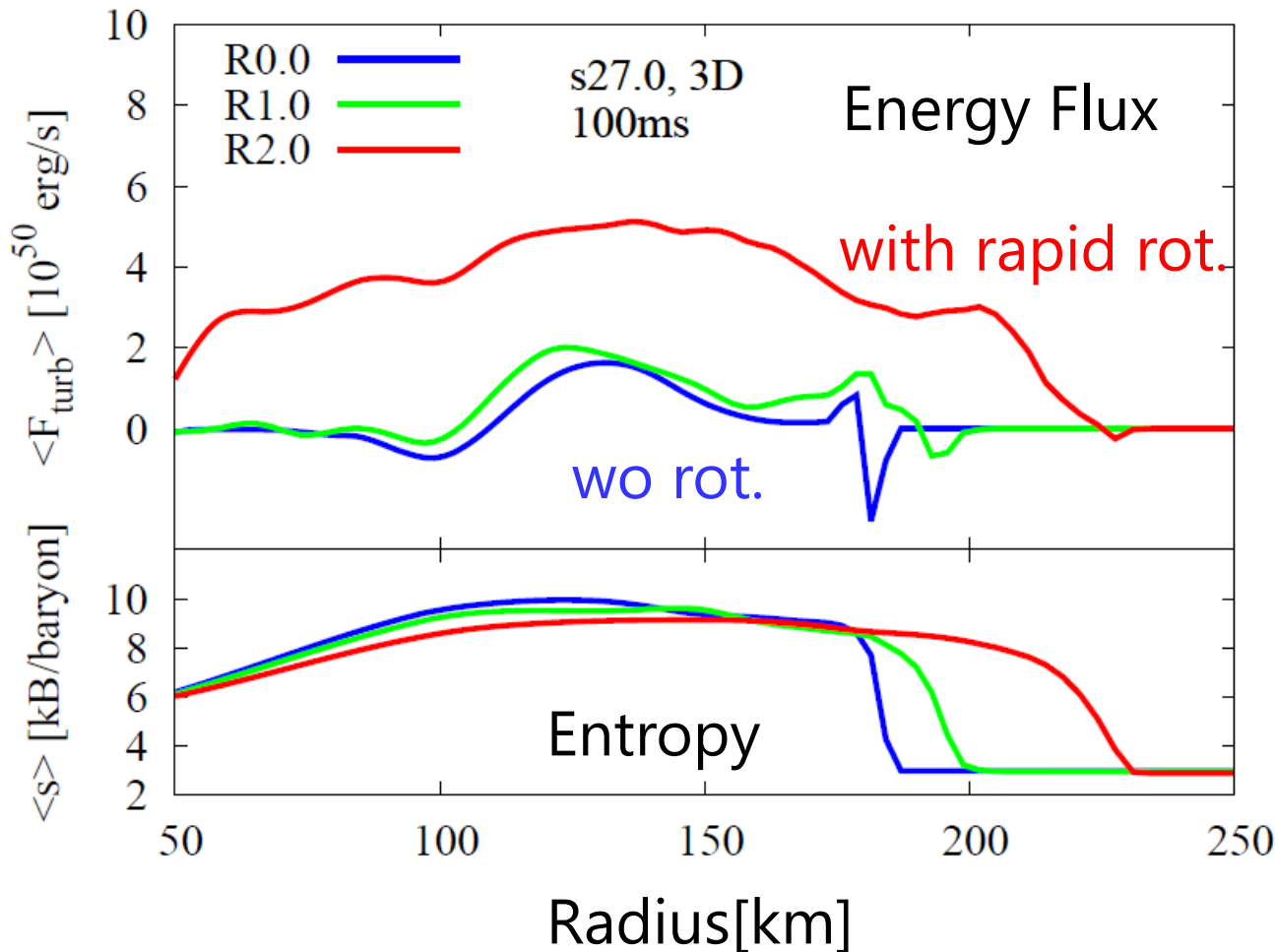
Rotational energy(T)/gravitational energy(W)
reach some criteria => Spiral mode arises

In the rigid ball: 14%

Ott+ 2005

In SNe case: ~ 6% (Called low-T/W instability)

Energy Transport by spiral mode

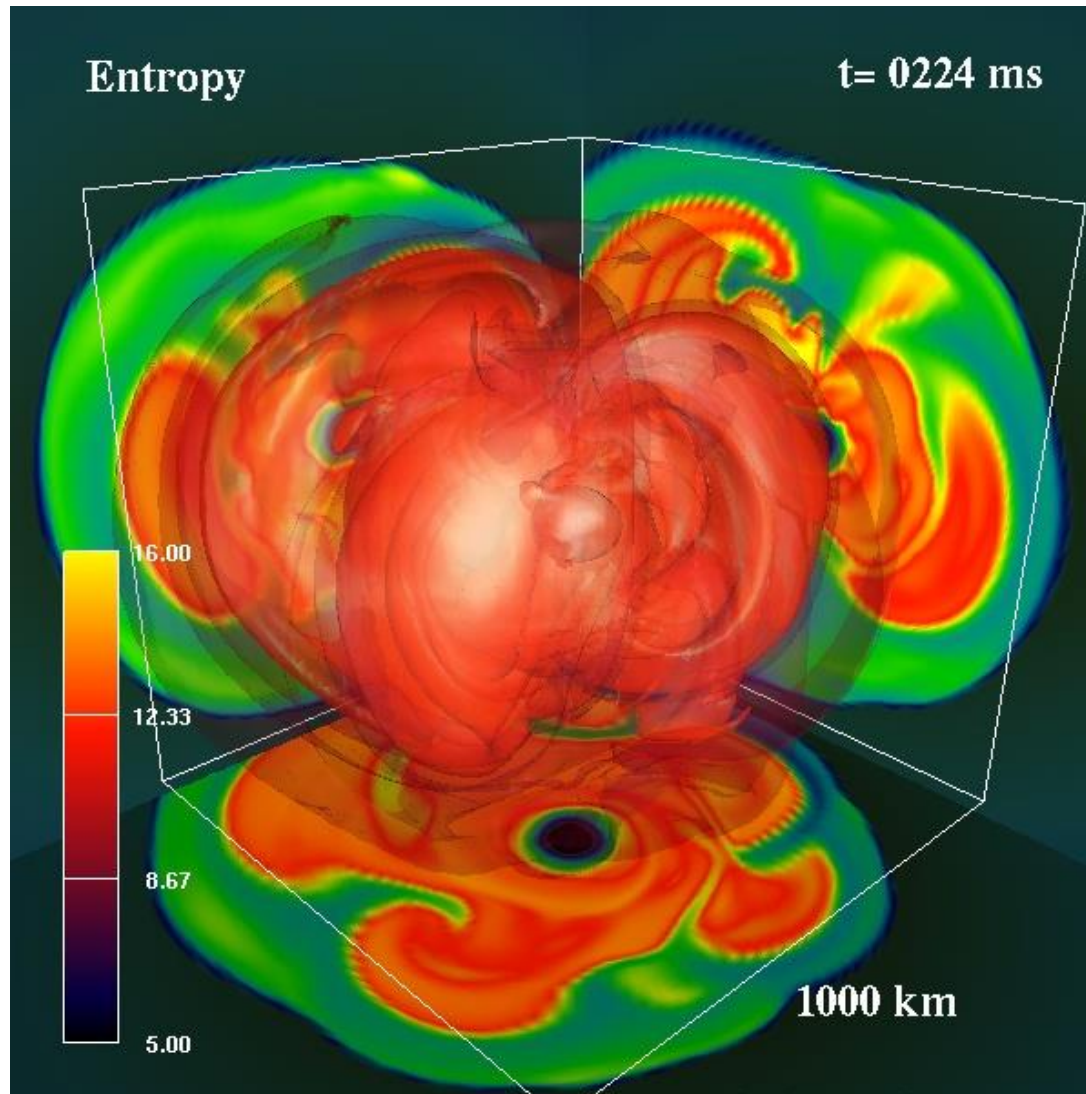


Power of ν heating = 10^{52} erg/s

Power of Spiral mode = 0.5×10^{52} erg/s

Spiral mode transport energy from center to outer region and helps explosion.

Rotational Explosion



Strong expansion is found at equatorial plane

$E_{\text{exp}} \sim 5 \times 10^{50} \text{ erg}$

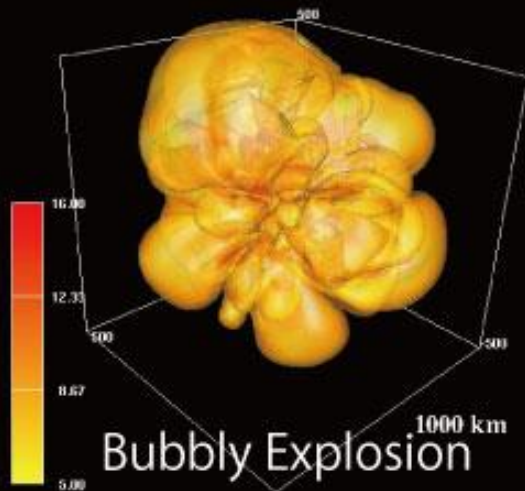
Nucleosynthesis?

Question on rotational explosion

- In my model, initial $\Omega = 2$ rad/s and final $\Omega = 2000$ rad/s at 400 ms after bounce.
- Period of the zero-age pulsar is expected as ~ 10 ms,
 $\Omega = 100$ rad/s. Ott+ 2006
- Is the fast rotation allowed?
Very efficient angular transport are required to justify the model.

11.2 wo rotation

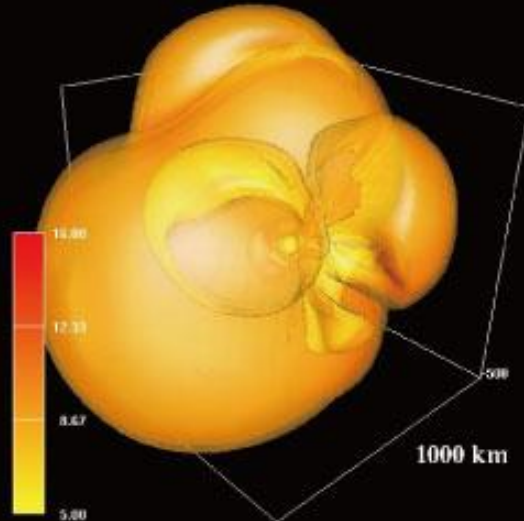
t= 0220 ms



Bubbly Explosion

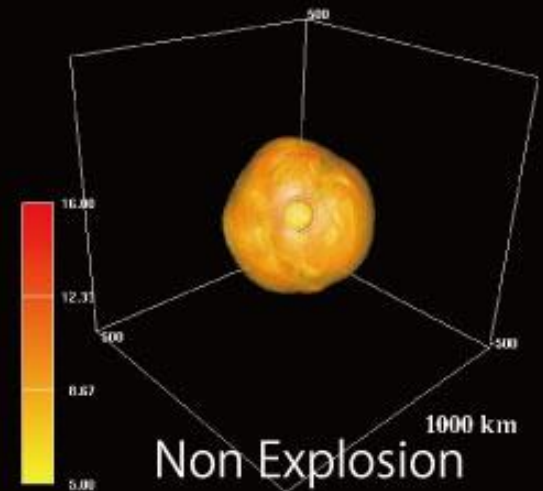
13.0 wo rotation

t= 0270 ms



27.0 wo rotation

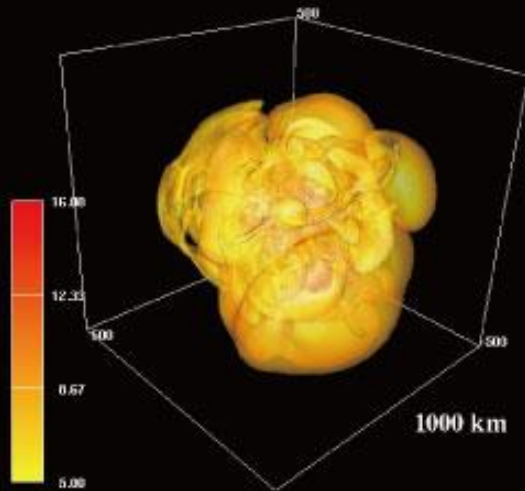
t= 0250 ms



Non Explosion

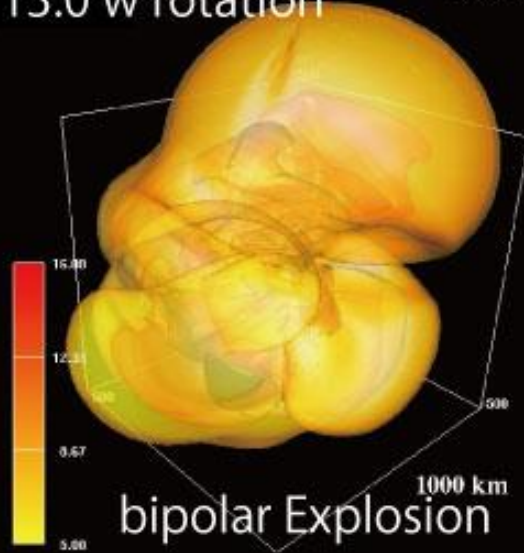
11.2 w rotation

t= 0200 ms



13.0 w rotation

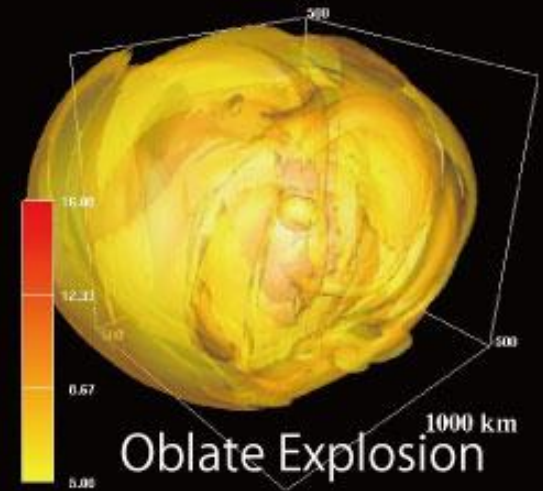
t= 0290 ms



bipolar Explosion

27.0 w rotation

t= 0250 ms



Oblate Explosion

Summary

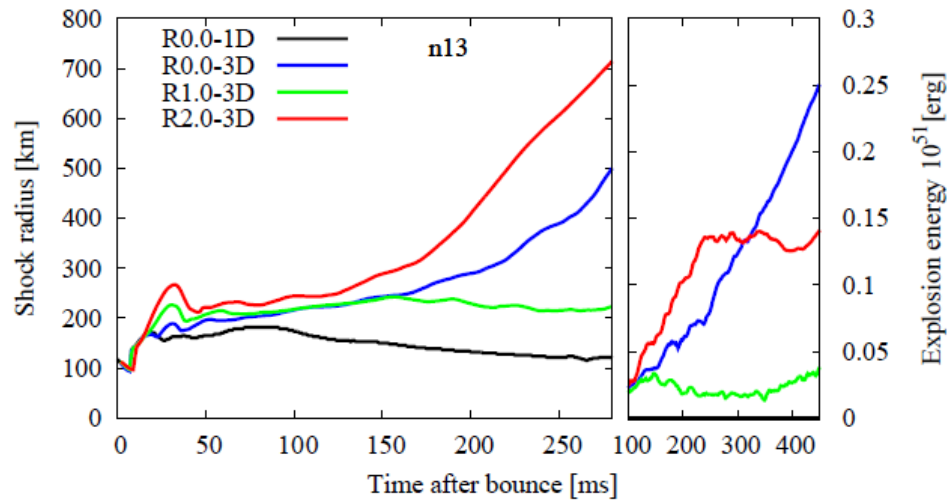
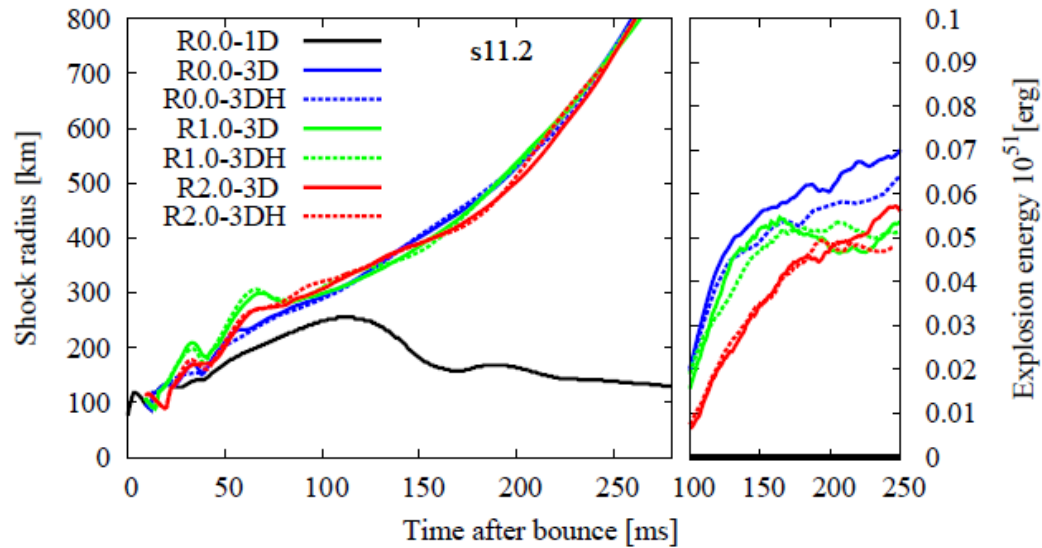
- Simulations of SNe depend on the employed methods (will be discussed in Friday).
- The energy Transport of turbulence plays important role. That's why 1D fails and 2D or 3D tend to succeed.
- SASI can be important for heavier progenitor.
- We found interesting type of explosion. With rapid rotation, low-T/W instability arises. Spiral mode is promoted. Energy transport due to that helps explosion.

Questions

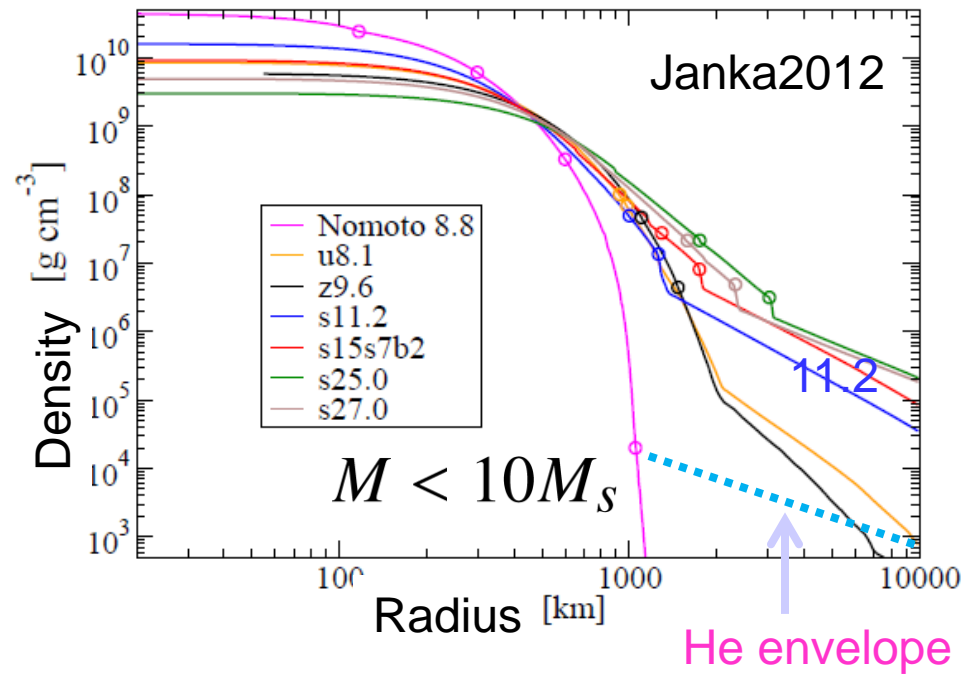
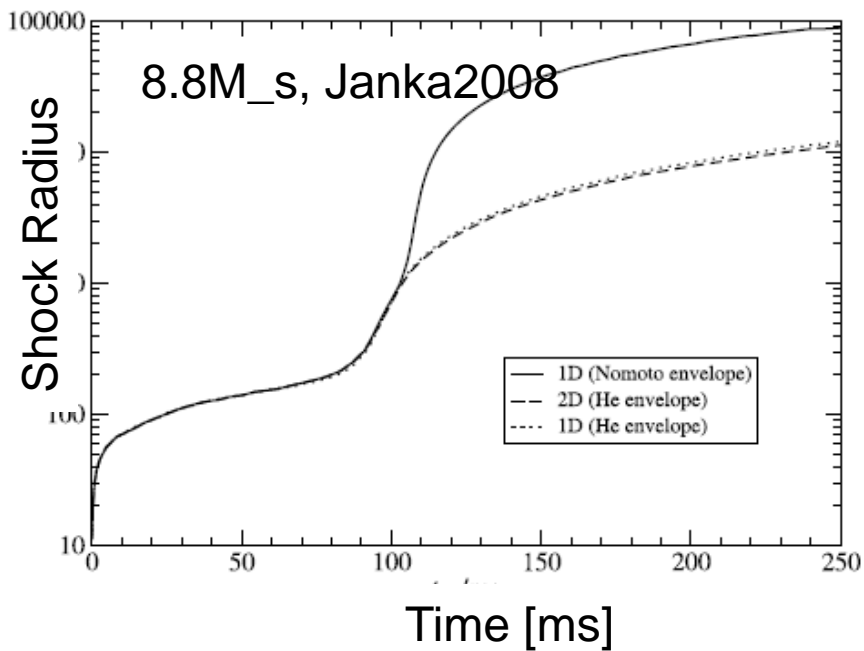
- Can we grasp the feature of convection?
- Is the expectation below is correct?
For light progenitor, with only ν -heating SNe explode.
For normal progenitor convection helps SNe explosion.
For heavy progenitor convection and SASI helps SNe explosion.
- Explosion triggered by fast rotation is allowed?

Appendix

Averaged shock radius and Exp. Energy

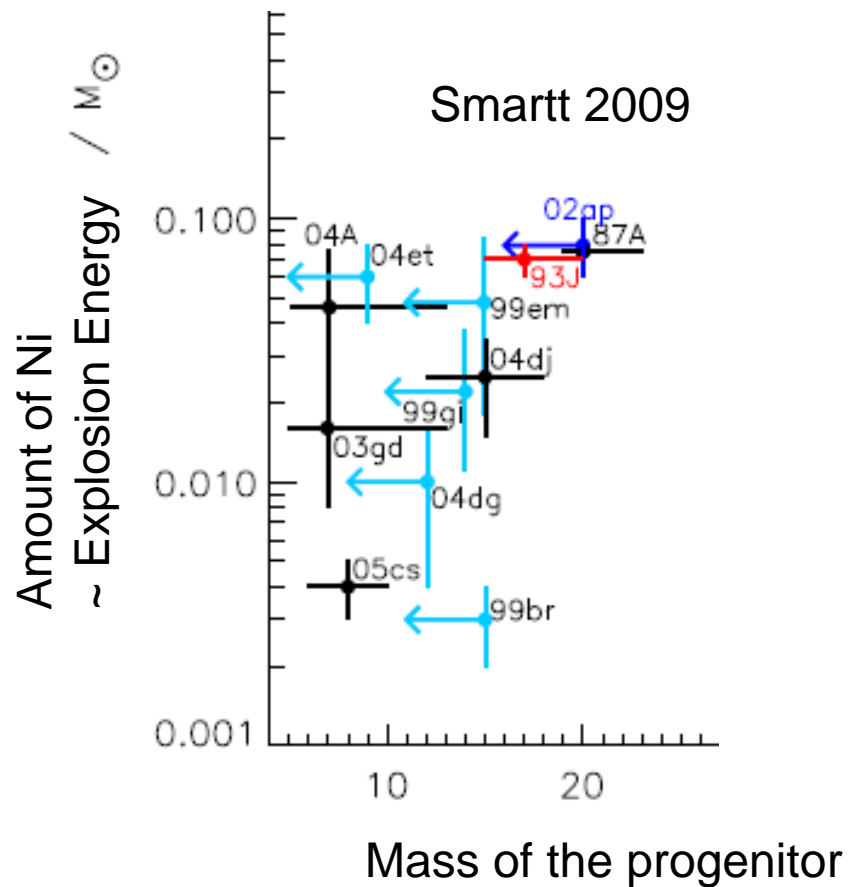
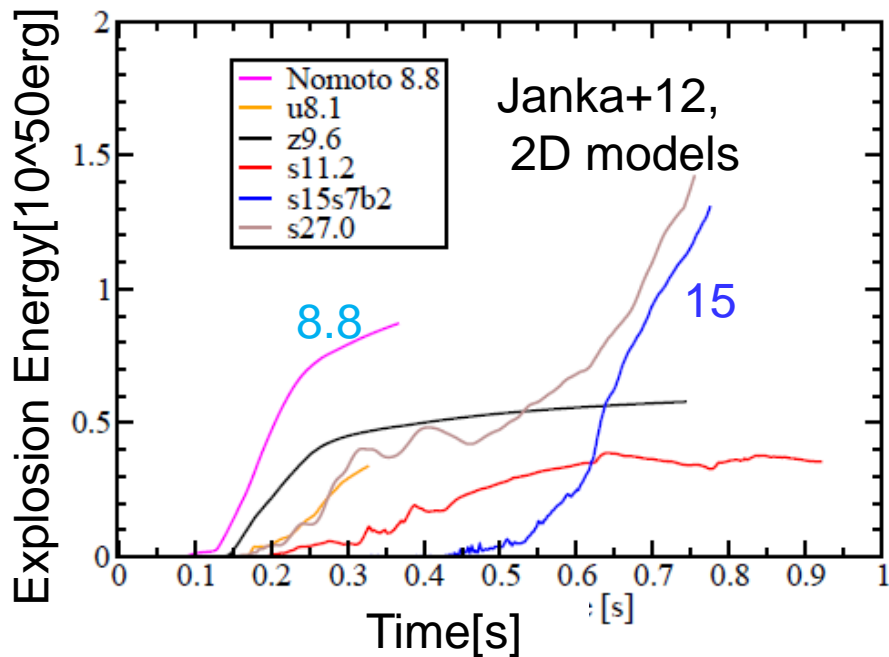


Pure ν heating



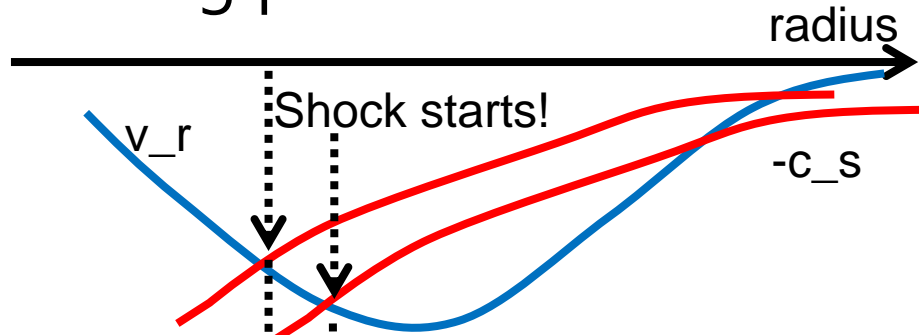
Easy shock revival
Dilute outer layer



Pure ν heating



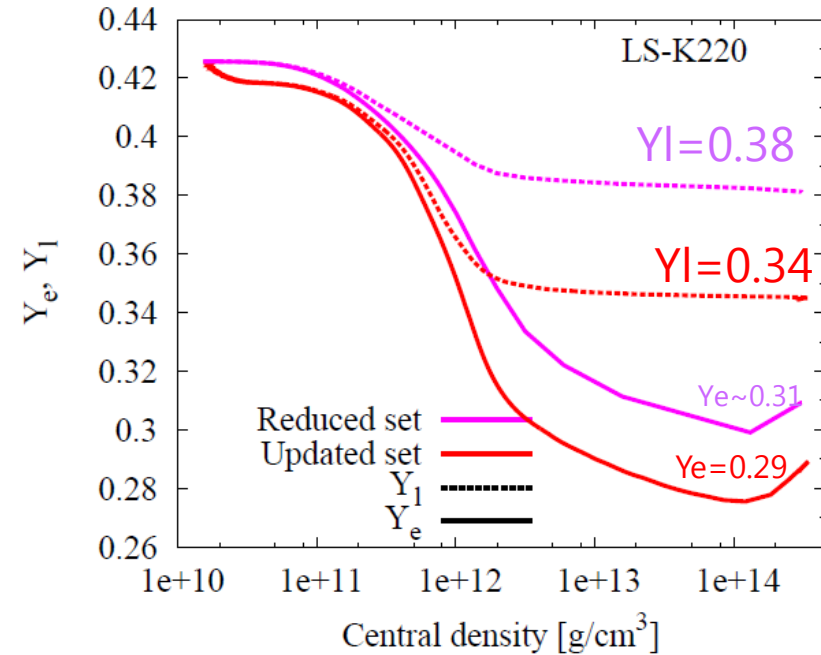
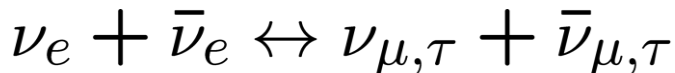
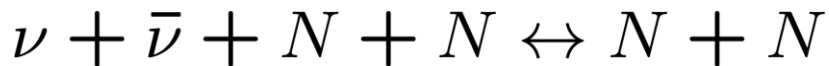
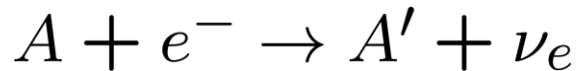
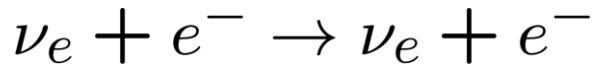
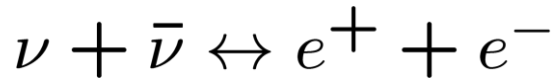
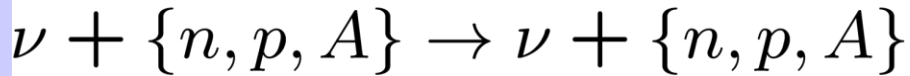
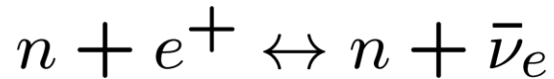
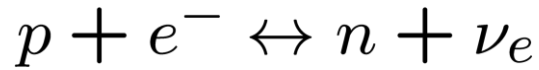
How does Y_I affect the evolution of the shock?

1. Electron capture rate \downarrow , $Y_I \uparrow$ $p + e^- \rightarrow n + \nu_e$
2. Pressure \uparrow , Sound speed \uparrow , $P \propto (Y_I \rho)^{4/3}$, $c_s \sim \sqrt{P/\rho}$
starting position of the shock \uparrow



3. Mass of iron to dissociate \downarrow
Hot water 
Hot water  \leq Energetic Shock!
4. The energy of the Shock \uparrow

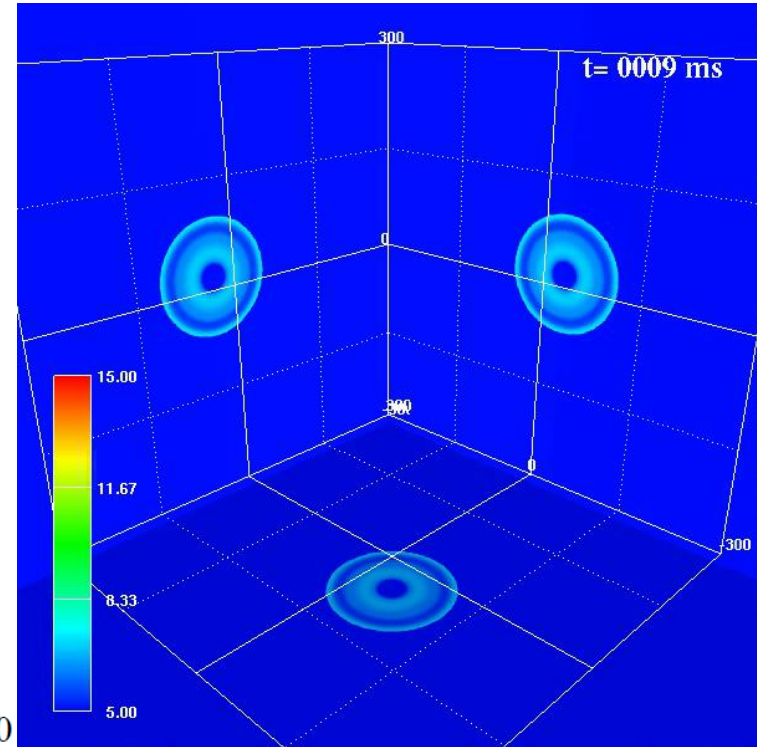
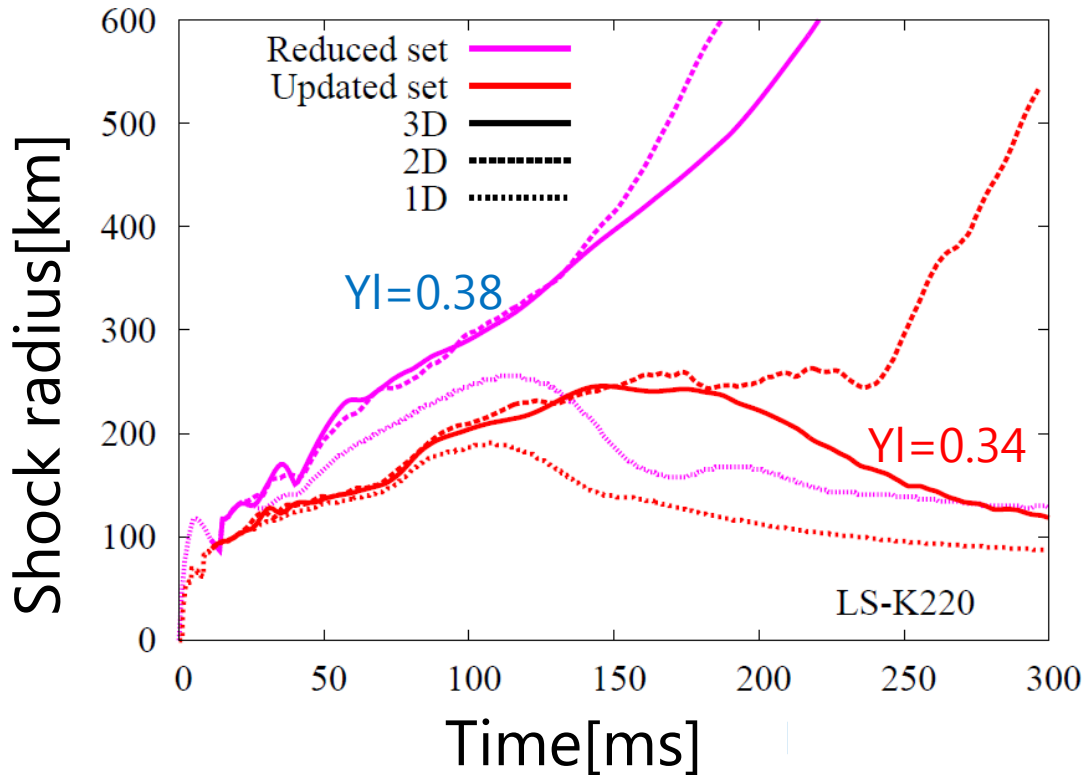
Neutrino Reactions



There are still several minor points that are remaining to be updated.

Updated set is roughly consistent with the more sophisticated works(e.g. Mueller+2010).

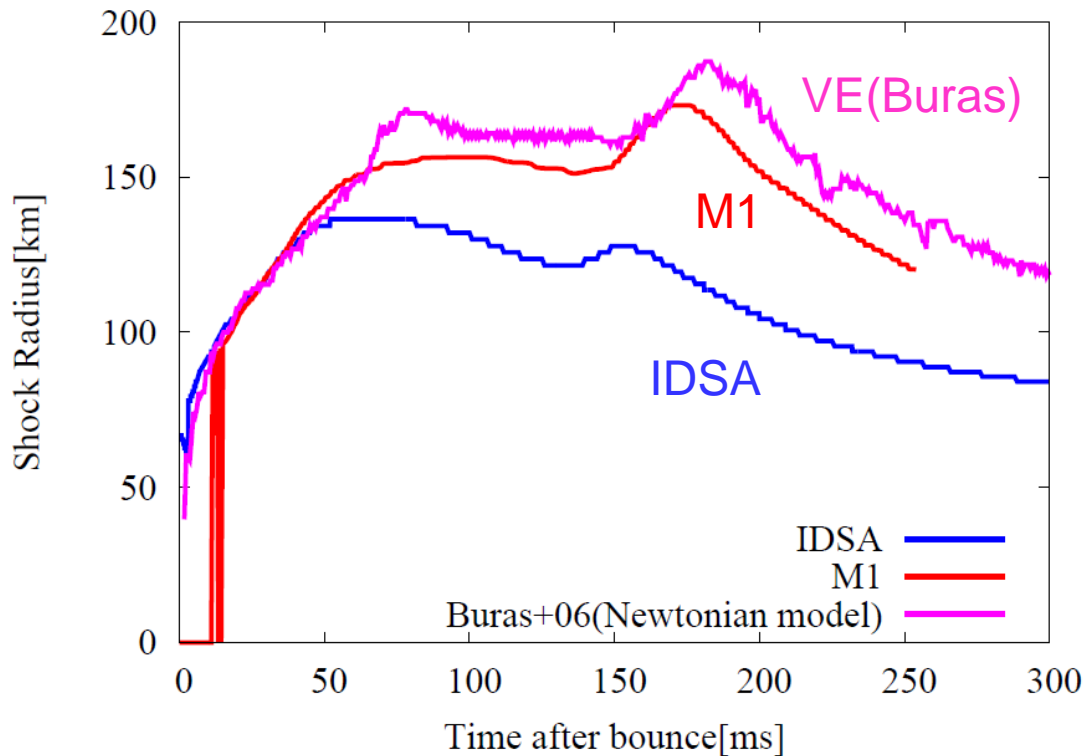
Multi-Dimensional Simulations



Unfortunately our 3D model with updated neutrino reaction does not explode.

But do not forget that we now ignore GR Effect that should help the explosion!

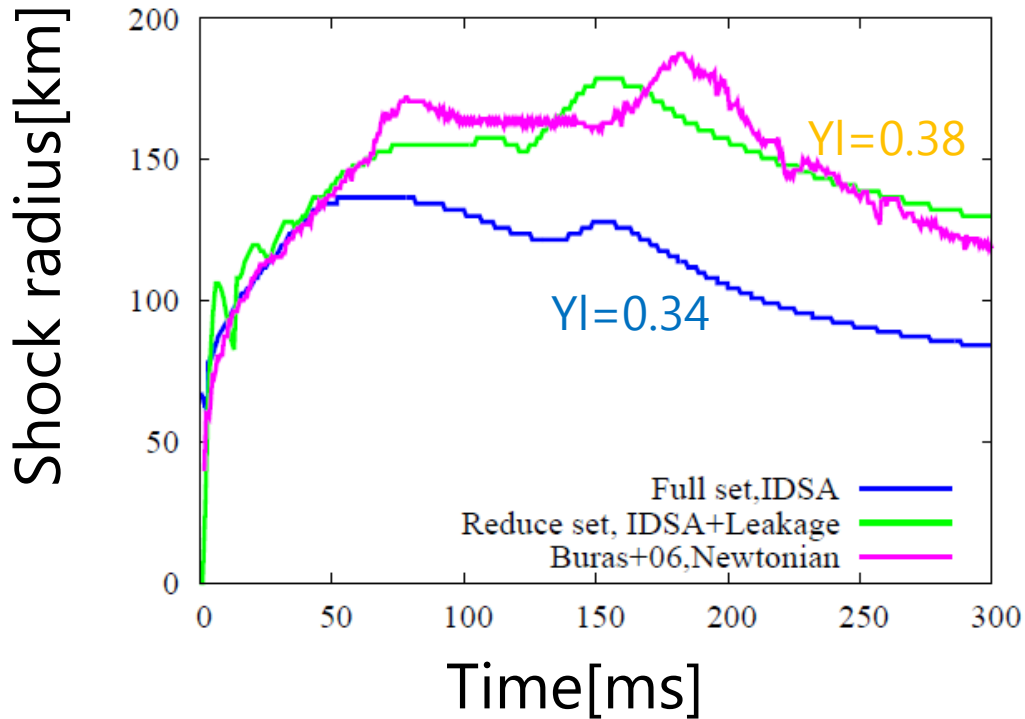
Dependence on Radiation Hydro



VE > M1 > IDSA

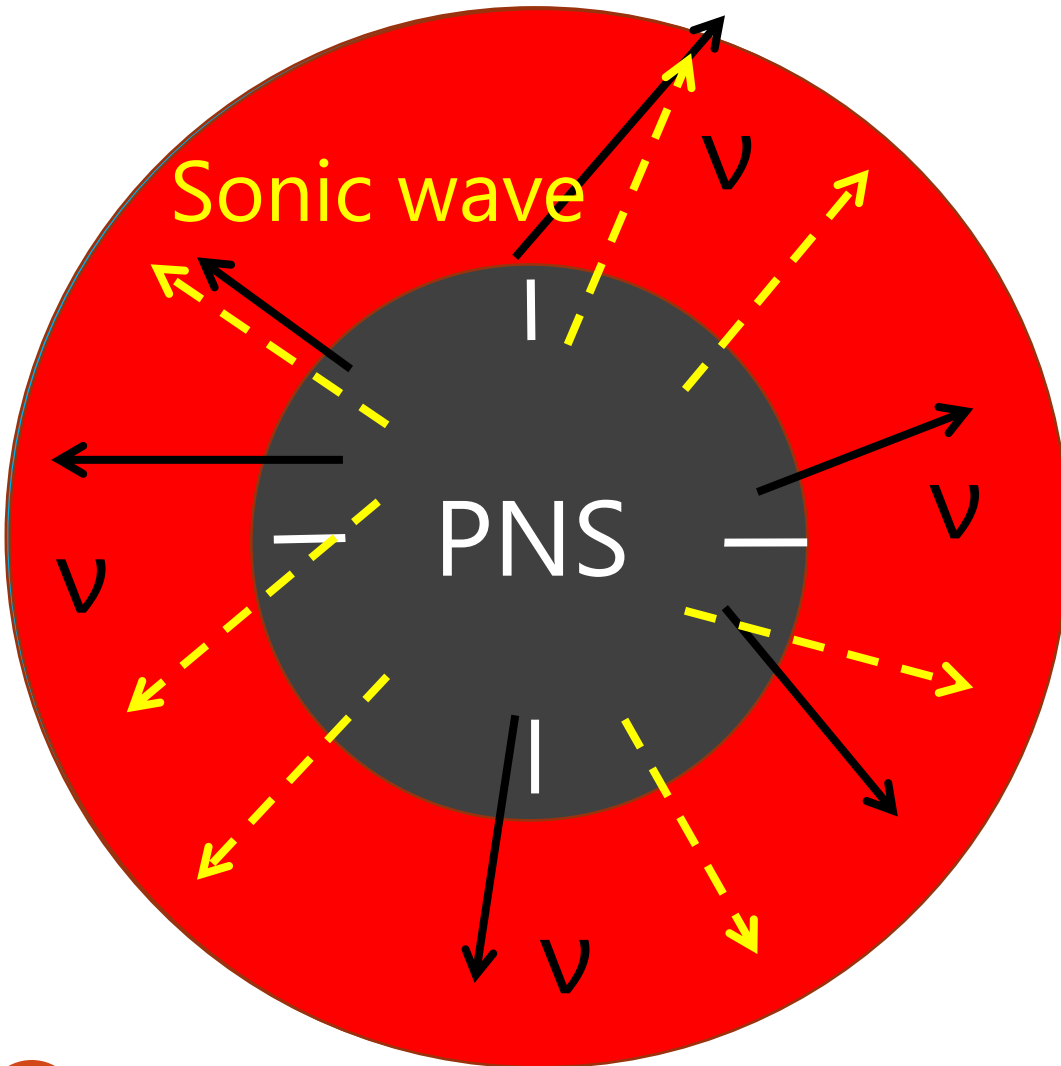
Density of neutrino could be larger in more sophisticated method.

Comparison of the shock radius in 1D



Smaller Y_I results in smaller shock radius!
It's strange but reduced set is closer to the trajectory of more sophisticated calculation.

Basic idea to connect EOS and Explosion

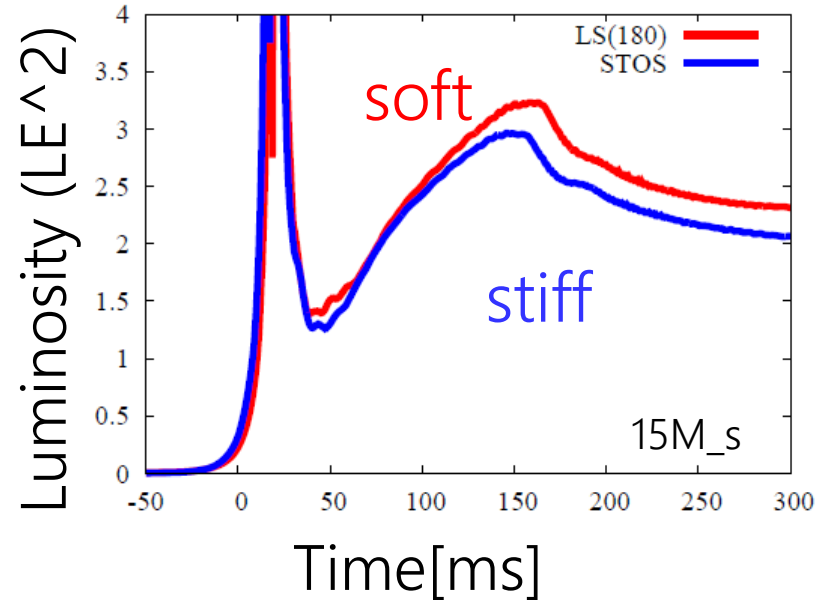
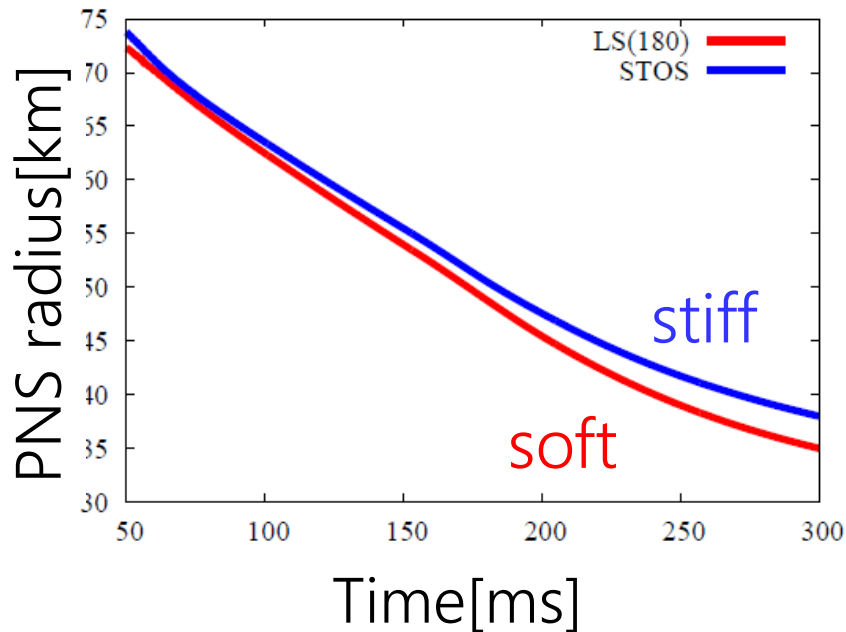


1. The PNS gradually shrinks by the gravity.
2. E_{grav} is released.
3. E_{thermal} is increased.
4. The L_{ν} and sonic waves are emitted from the surface of PNS.

Soft EOS releases large energy and makes the PNS dense, that produce strong acoustic wave.

Softer EOS is preferable to the explosion.

Neutrino Luminosity

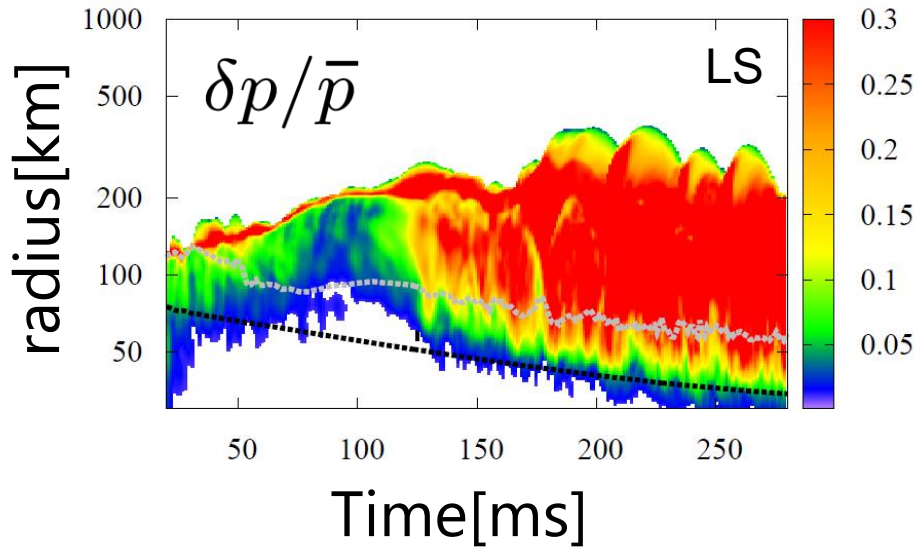


LS(K220): Soft EOS \Rightarrow rapidly shrink \Rightarrow Large L_ν

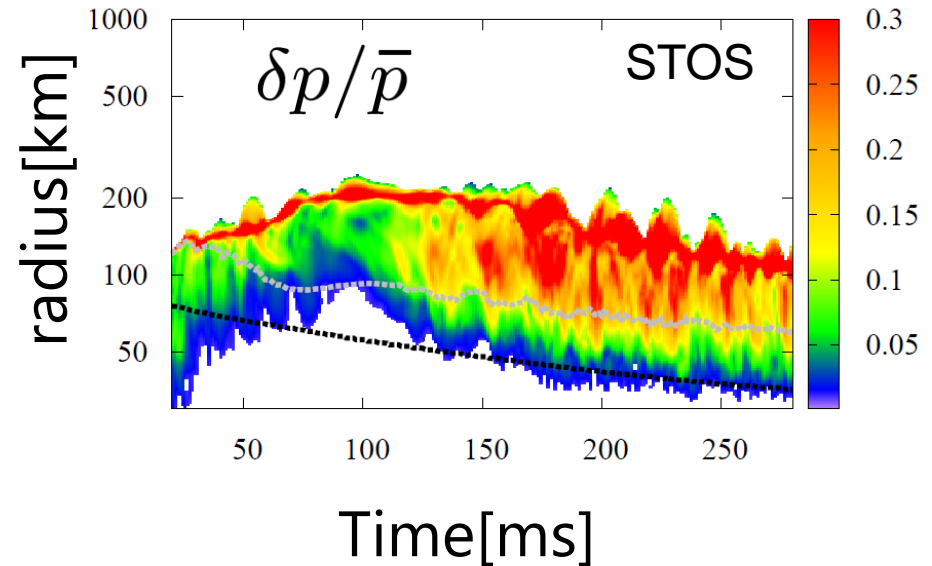
Shen: Stiff EOS \Rightarrow slowly shrink \Rightarrow small L_ν

Sonic Wave

s11.2(WHW02)-LS



s11.2(WHW02)-STOS

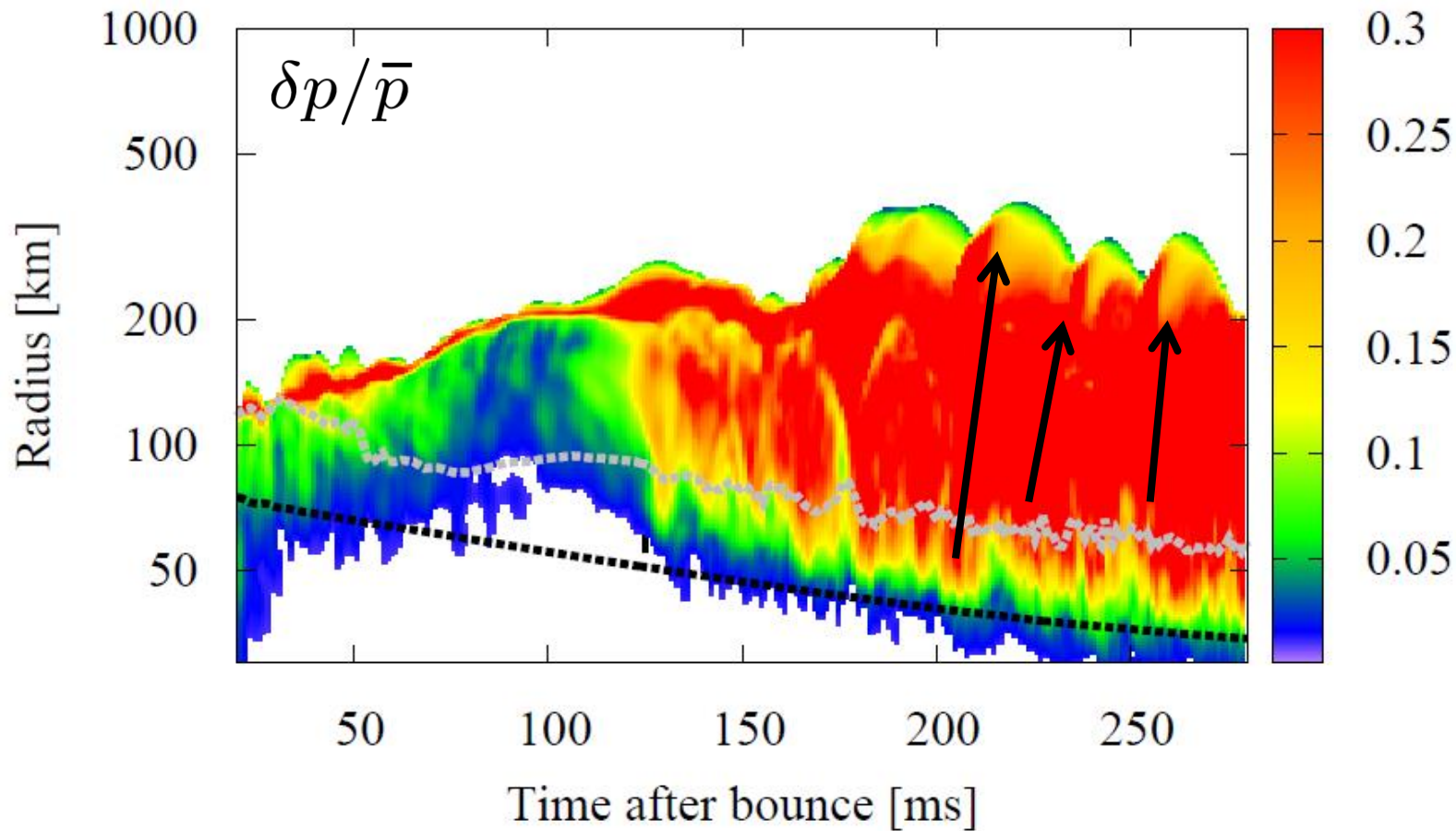


Gray: gain radius, black PNS radius

Strong sonic wave is reflected at the PNS!
(It is a little bit hard to see, but) softer EOS
make stronger sonic wave.

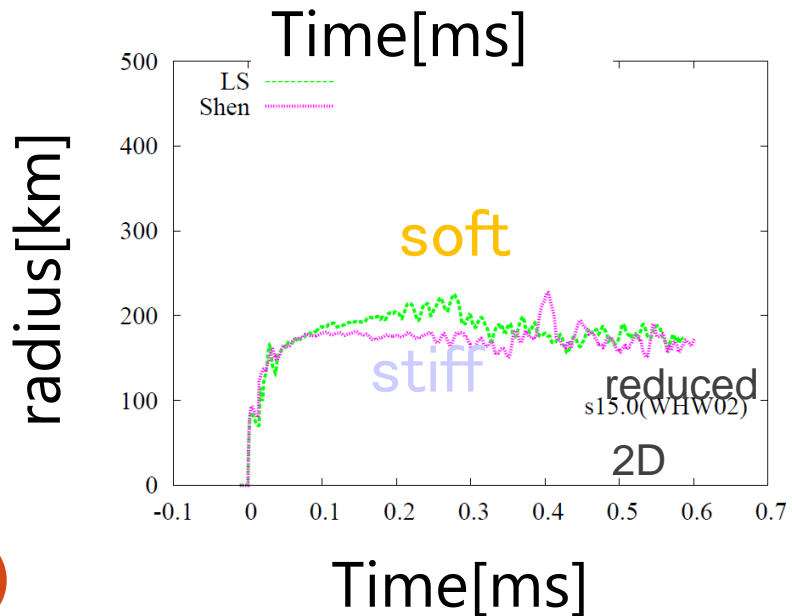
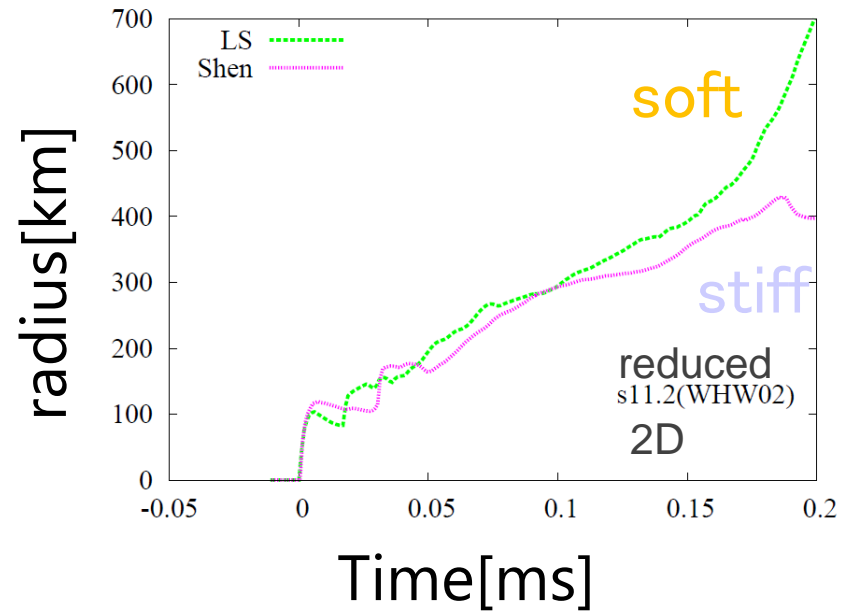
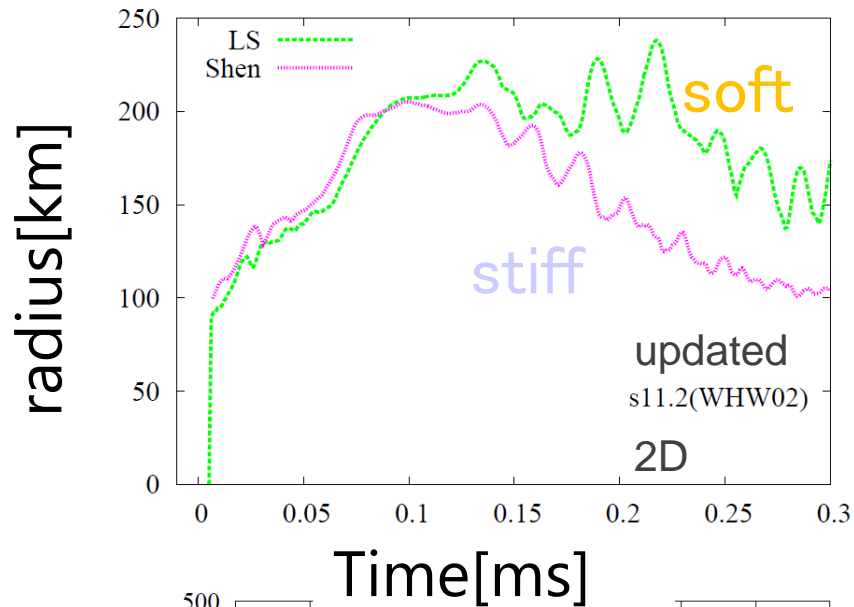
Sonic Wave

s11.2(WHW02)-LS



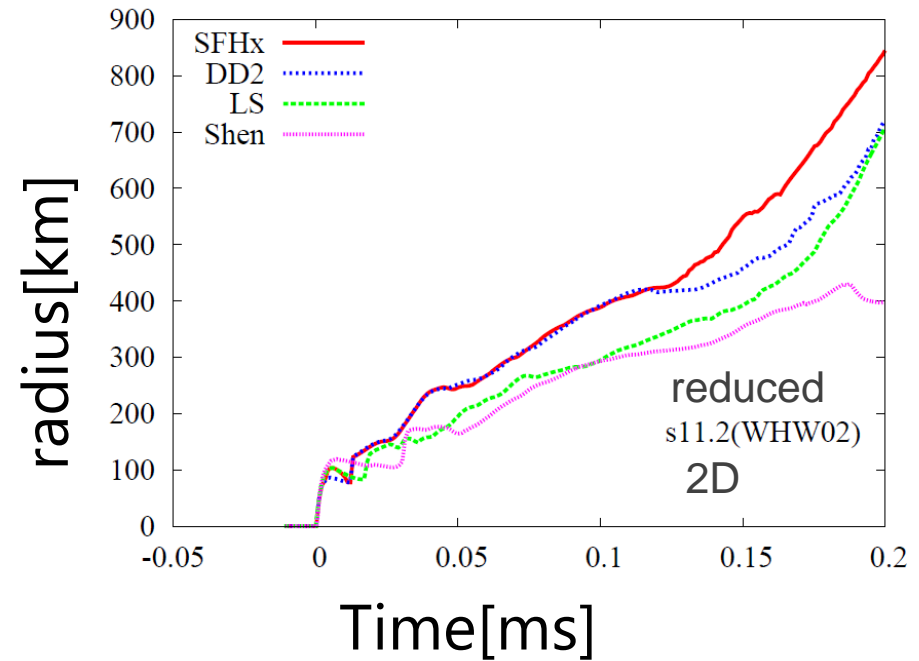
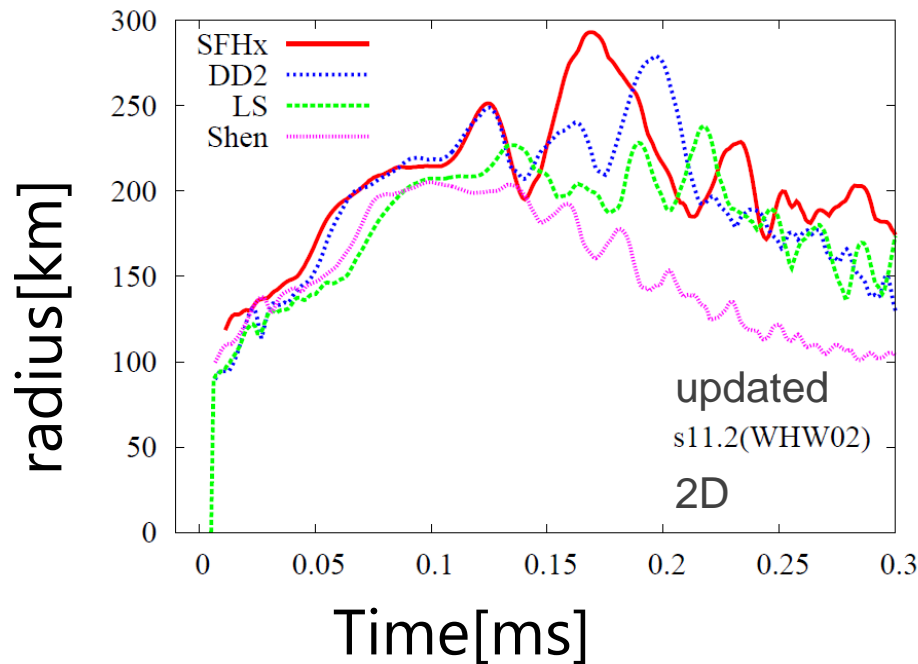
Gray: gain radius, black PNS radius

Evolution of the shock



Softer EOS shows larger shock radius.

Emergence of Multi-species EOS



SFHx and DD2: Multi species of heavy nuclei is included.

SFHx and DD2 \succ LS and STOS

Employing MS may help SNe explosion.

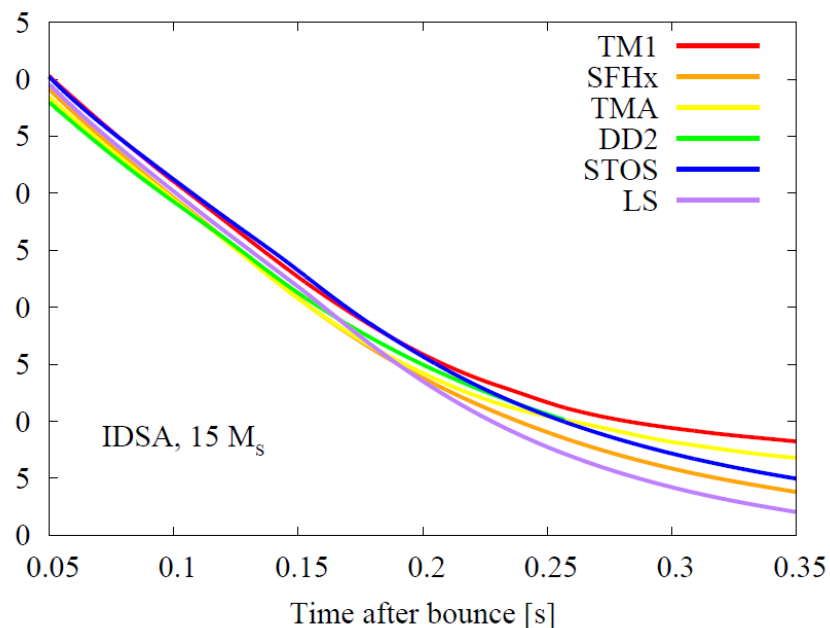
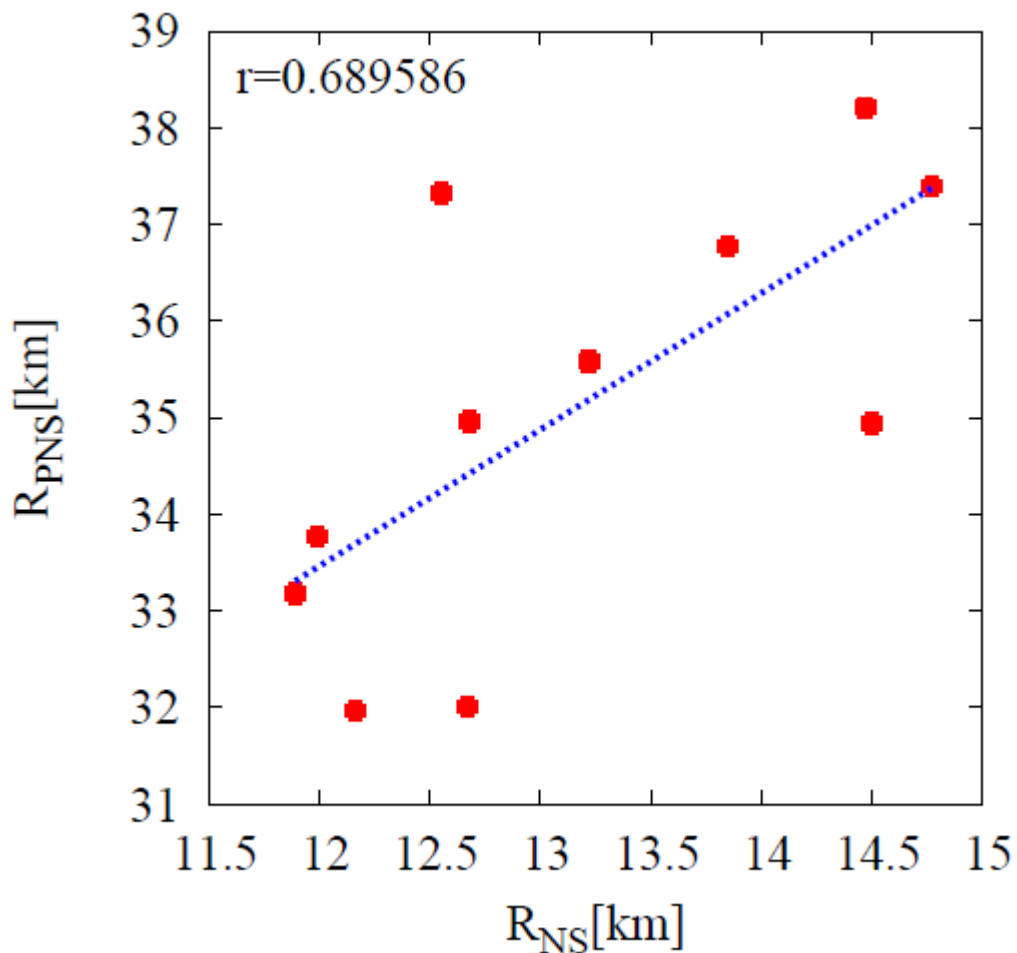
But in one-dimensional GR sim, that situation is contradictory. (Fisher+2014)

In other words?

We understand **the radius of PNS** is very important probe to determine success or failure of supernovae.

Is the result translated to **the terms of nuclear physics**?

NS radius vs PNS radius

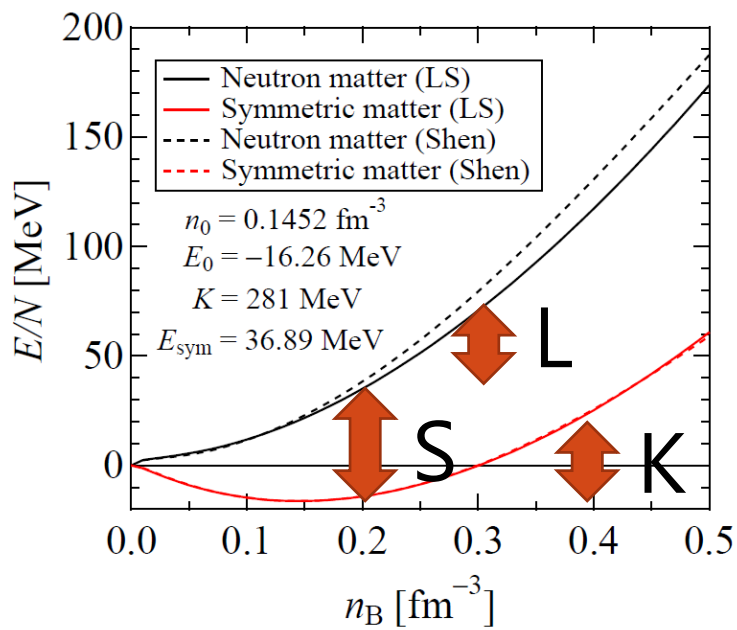


Takiwaki in prep

PNS radius:
 TM1 > TMA ~ DD2 > SFHx
 STOS > LS

PNS radius is "roughly" predicted by the NS radius at zero-temperature.

Many theories for EOS



$$p = n^2 \frac{\partial (E/N)}{\partial n}$$

Fisher+2014

| EOS | n_0 [fm^{-3}] | E_0 [MeV] | K [MeV] | S [MeV] | L [MeV] | $R_{1.4}$ [km] | M_{max} [M_{\odot}] |
|-------------|-------------------------------|----------------|--------------------|---------------------------|---------------------------|---------------------------|-------------------------------------|
| SFHo | 0.1583 | 16.19 | 245 | 31.57 | 47.10 | 11.89 | 2.06 |
| SFHx | 0.1602 | 16.16 | 238 | 28.67 | 23.18 | 11.99 | 2.13 |
| HS(TM1) | 0.1455 | 16.31 | 281 | 36.95 | 110.99 | 14.47 | 2.21 |
| HS(TMA) | 0.1472 | 16.03 | 318 | 30.66 | 90.14 | 13.85 | 2.02 |
| HS(FSUgold) | 0.1482 | 16.27 | 229 | 32.56 | 60.43 | 12.55 | 1.74 |
| HS(DD2) | 0.1491 | 16.02 | 243 | 31.67 | 55.04 | 13.22 | 2.42 |
| HS(IUFSU) | 0.1546 | 16.39 | 231 | 31.29 | 47.20 | 12.68 | 1.95 |
| HS(NL3) | 0.1482 | 16.24 | 272 | 37.39 | 118.49 | 14.77 | 2.79 |
| STOS(TM1) | 0.1452 | 16.26 | 281 | 36.89 | 110.79 | 14.50 | 2.22 |
| LS (180) | 0.1550 | 16.00 | 180 | 28.61 | 73.82 | 12.16 | 1.84 |
| LS (220) | 0.1550 | 16.00 | 220 | 28.61 | 73.82 | 12.67 | 2.05 |
| Exp. | ~ 0.15 | ~ 16 | $240 \pm 10^{(a)}$ | $29.0\text{--}32.7^{(b)}$ | $40.5\text{--}61.9^{(c)}$ | $10.4\text{--}12.9^{(c)}$ | $\gtrsim 2.0^{(d),(e)}$ |

Parametric EoS

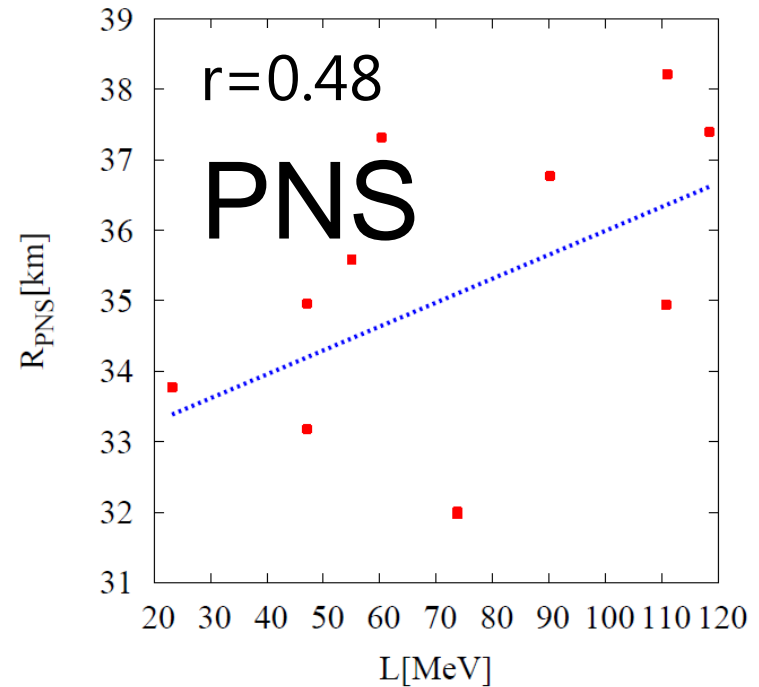
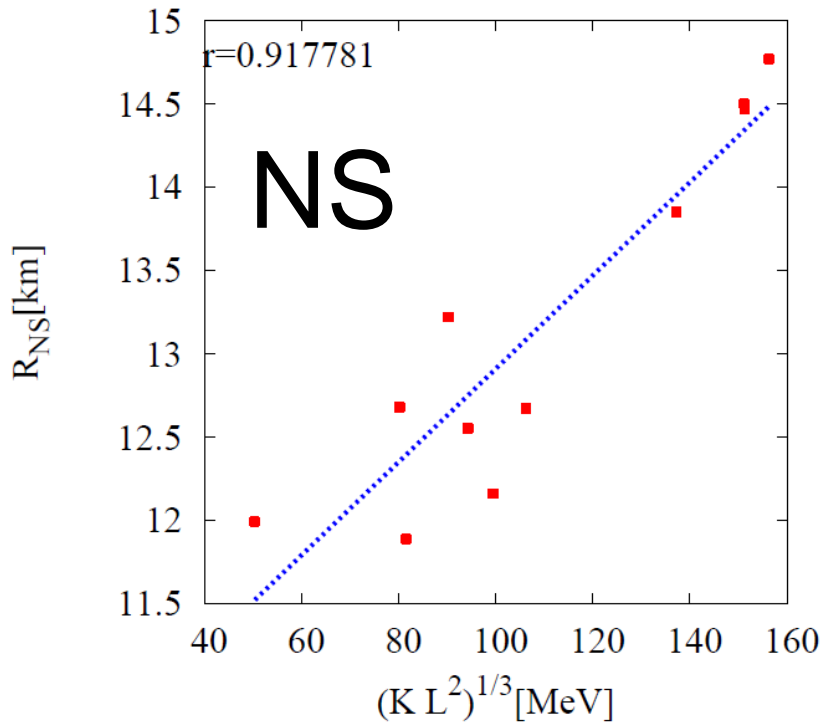
| EOS | n_0 [fm ³] | E_0 [MeV] | K [MeV] | E_{sym} [MeV] | L [MeV] |
|------------------------|--------------------------|-------------|-------------|------------------------|-----------|
| STOS (original) | 0.1452 | -16.26 | 281 | 36.89 | 110.79 |
| LS (original) | 0.1550 | -16.00 | 180/220/375 | 29.30 | 73.82 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 180 | 25.00 | 60.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 180 | 30.00 | 75.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 180 | 35.00 | 90.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 230 | 25.00 | 60.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 230 | 30.00 | 75.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 230 | 35.00 | 90.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 280 | 25.00 | 60.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 280 | 30.00 | 75.62 |
| STOS (low) + LS (high) | 0.16 | -15.80 | 280 | 35.00 | 90.62 |
| STOS (low) + LS (high) | 0.1452 | -16.26 | 281 | 36.89 | 97.19 |

Togashi+ in prep

Is it fair to compare the EOS using different “theory”?
Togashi-san uses LS parametrization and make EOSs
of different K,S,L.

That enable us to compare the EOS fairly and extract
information of K,S and L from the simulations.

What parameter determine PNS radius



Radius of NS ($T \sim 0$ and $Y_e \sim 0$) is determine by L .

Radius of PNS is not determine by L .

S and K have stronger correlation to PNS.

$r=0.71$ for S . $r=0.69$ for K .