

# Neutron Star Merger with Tabulated EOS and Spin

Wolfgang Kastaun



UNIVERSITY  
OF TRENTO - Italy



MICRA, Stockholm, Aug. 2015

# Topics

## Part 1: A recent merger simulation

- ▶ Gauge independent measures
- ▶ Structure of post-merger fluid flow
- ▶ Nature of hot spots
- ▶ Structure of merger remnant
- ▶ Matter ejection

## Part 2: Influence of initial NS spin on

- ▶ Inspiral
- ▶ GW signal
- ▶ Matter ejection

# Measuring Deformations

- ▶ Spatial gauge used in evolution bad for analysis of HMNS
- ▶ Define better coordinates
  - ▶ Consider the equatorial plane
  - ▶ Meaningful coordinate distances

$$g_{rr} = 1, \quad g_{\phi\phi,\phi} = 0$$

- ▶ Prevent spirals

$$\int_{-\pi}^{\pi} g_{r\phi} d\phi = 0$$

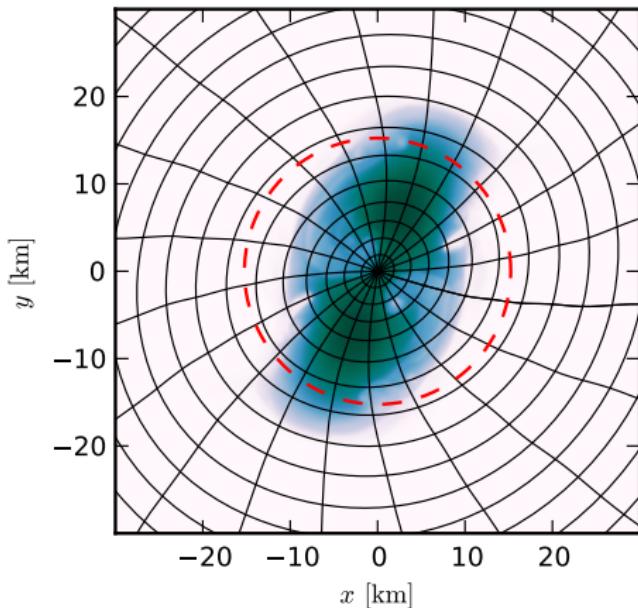
- ▶ Fix global rotation

$$\beta^\phi \rightarrow 0 \quad \text{for} \quad r \rightarrow \infty$$

- ▶ Choice of origin: use  $\pi$ -symmetry axis

# Measuring Deformations

- ▶ Spatial gauge used in evolution bad for analysis of HMNS
- ▶ Define better coordinates



# Measuring Compactness

## Problem

- ▶ Want to quantify density profile and compactness
- ▶ Compactness should not be sensitive to low density parts
- ▶ Should not require symmetries or preferred coordinates

# Measuring Compactness

## Problem

- ▶ Want to quantify density profile and compactness
- ▶ Compactness should not be sensitive to low density parts
- ▶ Should not require symmetries or preferred coordinates

## Solution

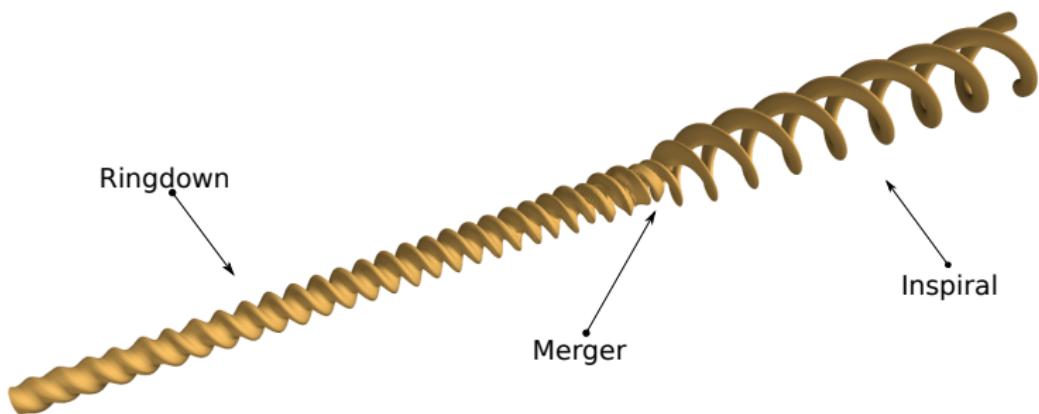
- ▶ Consider shells of constant (rest frame) mass density
- ▶ Each shell contains proper volume  $V$  and baryonic mass  $M_b$   
⇒ Unambiguous baryonic mass versus proper volume relations
- ▶ Compute “volumetric” radius  $R_v$  of Euclidian sphere with same volume
- ▶ Define compactness  $C = M_b/R_v$
- ▶ Define the “bulk” as shell with maximum compactness  
⇒ bulk mass, bulk volume, bulk entropy..

## Initial data

- ▶ Irrotational, equal mass
- ▶ No magnetic field
- ▶ Zero temperature,  $\beta$  equilibrium
- ▶ EOS: G. Shen, Horowitz, Teige
- ▶ Baryonic mass  $2 \times 1.513 M_{\odot}$
- ▶ Bulk mass 98% total mass
- ▶ Grav. mass of single star  $1.4 M_{\odot}$
- ▶ Initial proper separation 57.6 km  $\Rightarrow$  4 Orbits
- ▶ Maximum TOV baryonic mass  $3.33 M_{\odot}$   
 $\Rightarrow$  Remnant is stable !
- ▶ Corner case, probably not realistic

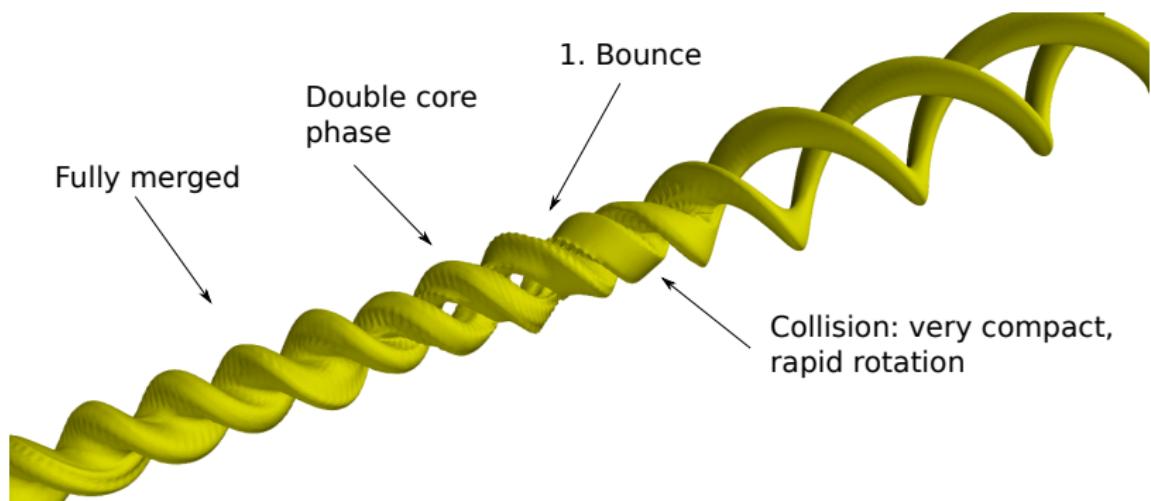
# Merger dynamics

Computed isodensity surfaces that contain  $\frac{1}{4}$  of total mass.  
Cut in  $xy+t$ :



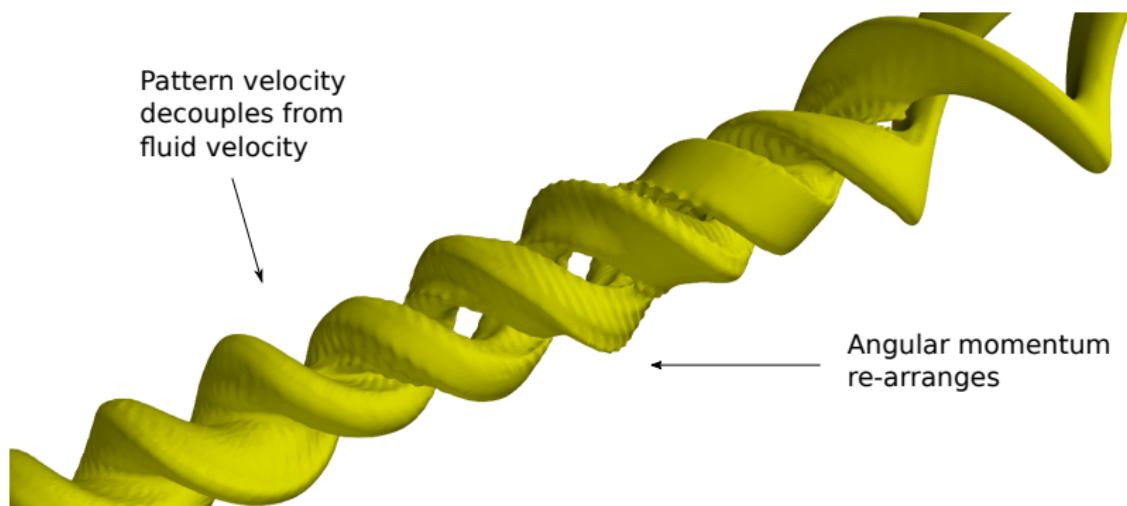
# Merger dynamics

Computed isodensity surfaces that contain  $\frac{1}{4}$  of total mass.  
Cut in  $xy+t$ :



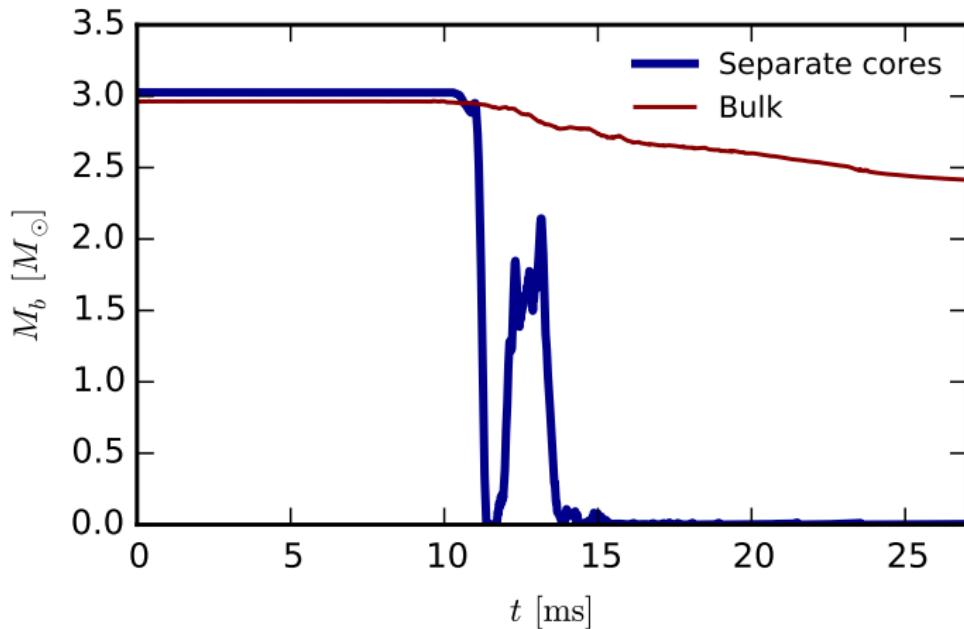
# Merger dynamics

Computed isodensity surfaces that contain  $\frac{1}{4}$  of total mass.  
Cut in  $xy+t$ :

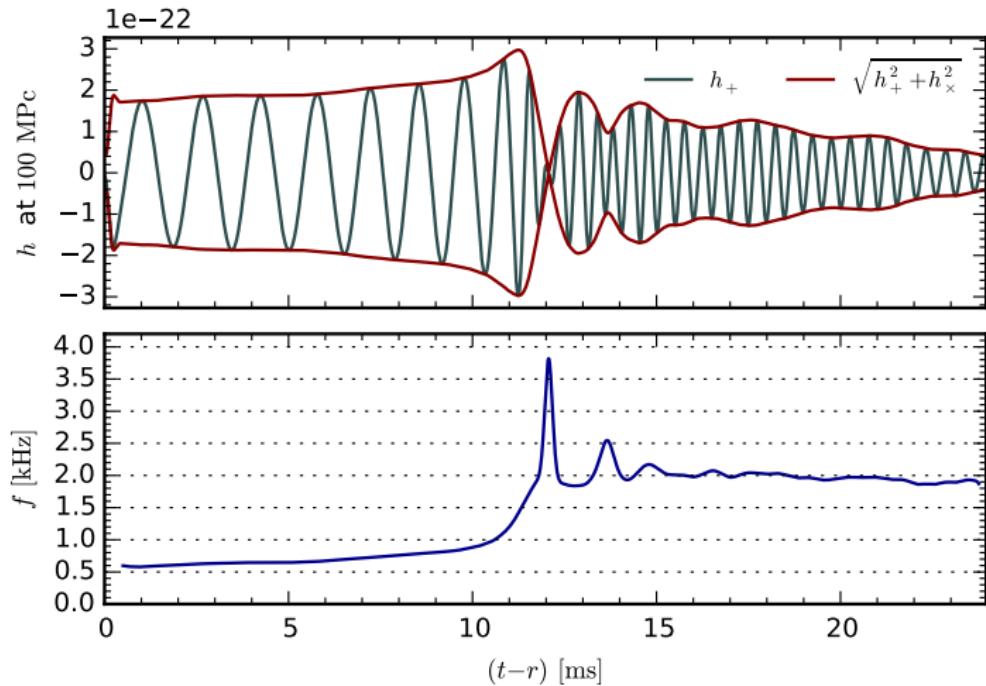


## Merger dynamics

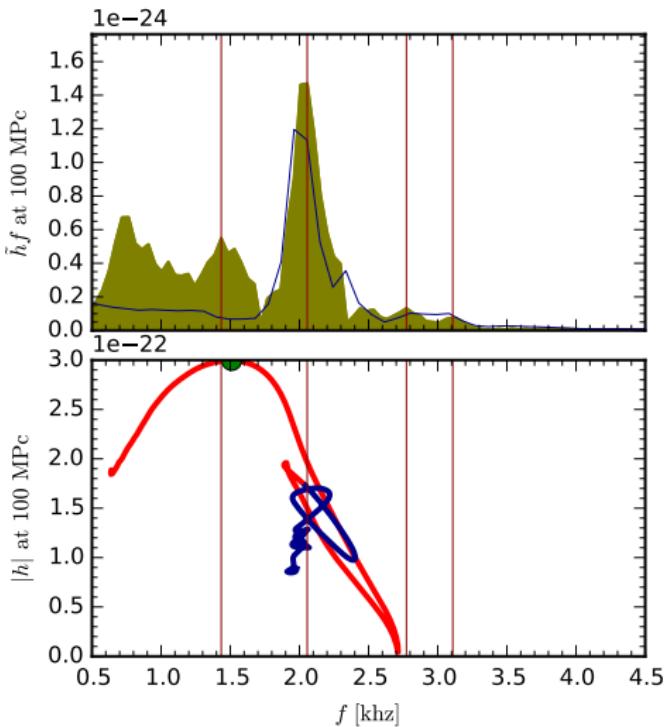
- ▶ Quantify mass in double core
- ▶ Total mass of matter with density > central density



# GW signal

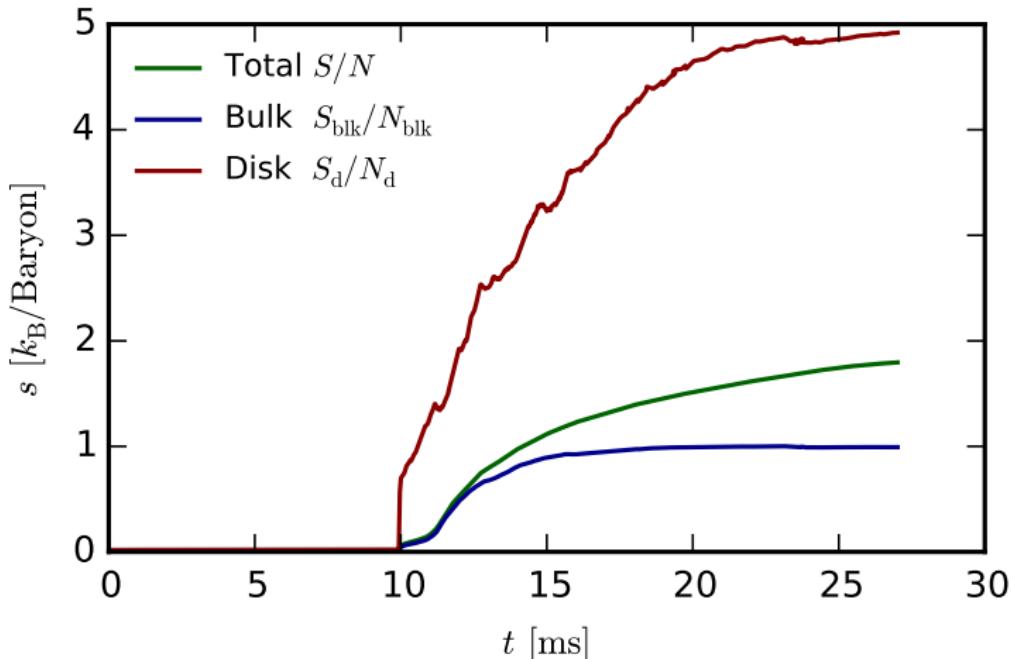


# GW signal

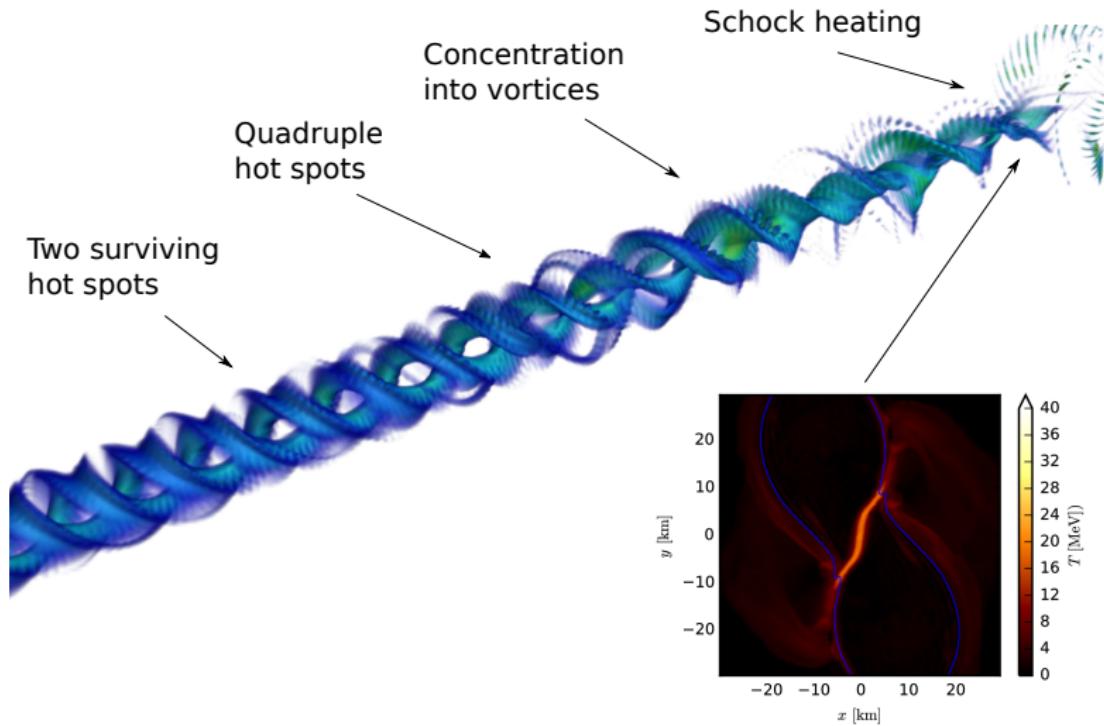


## Thermal evolution

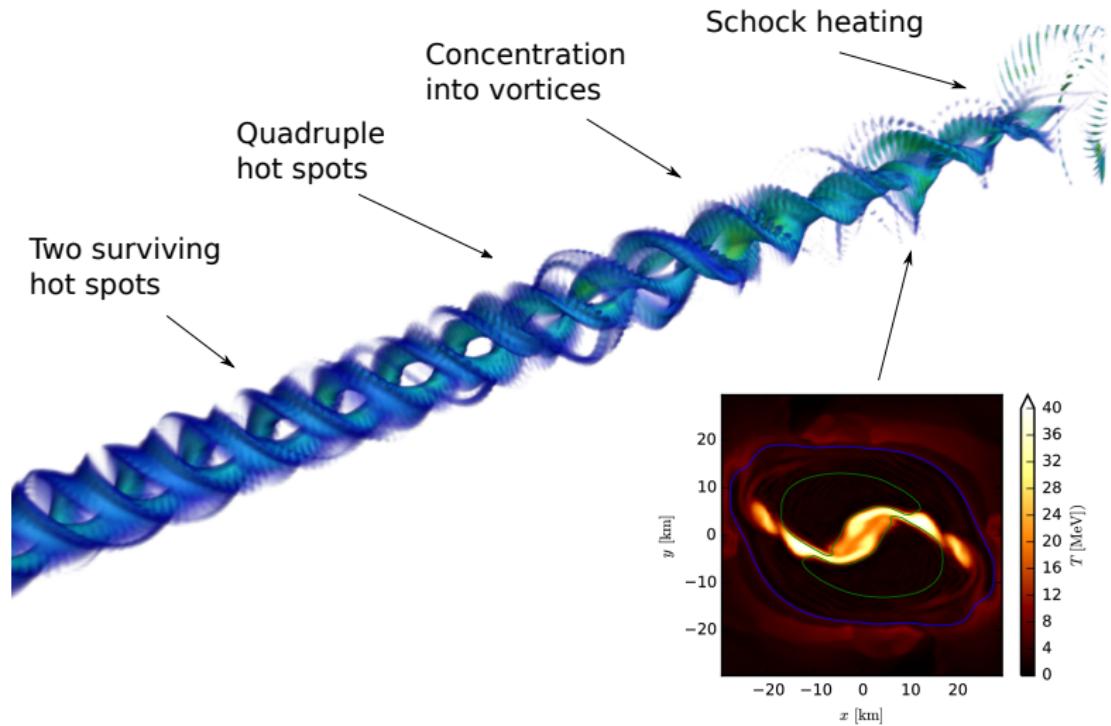
- ▶ Bulk entropy produced at merger, then constant
- ▶ Matter outside bulk hotter, ongoing heating



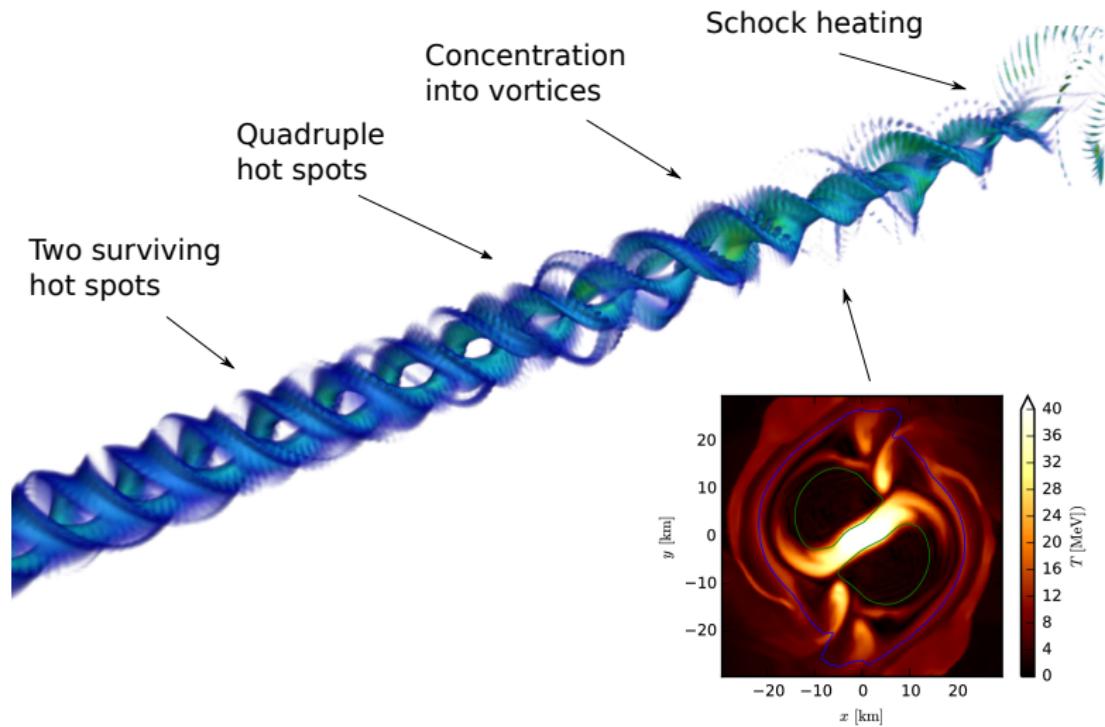
# Thermal evolution



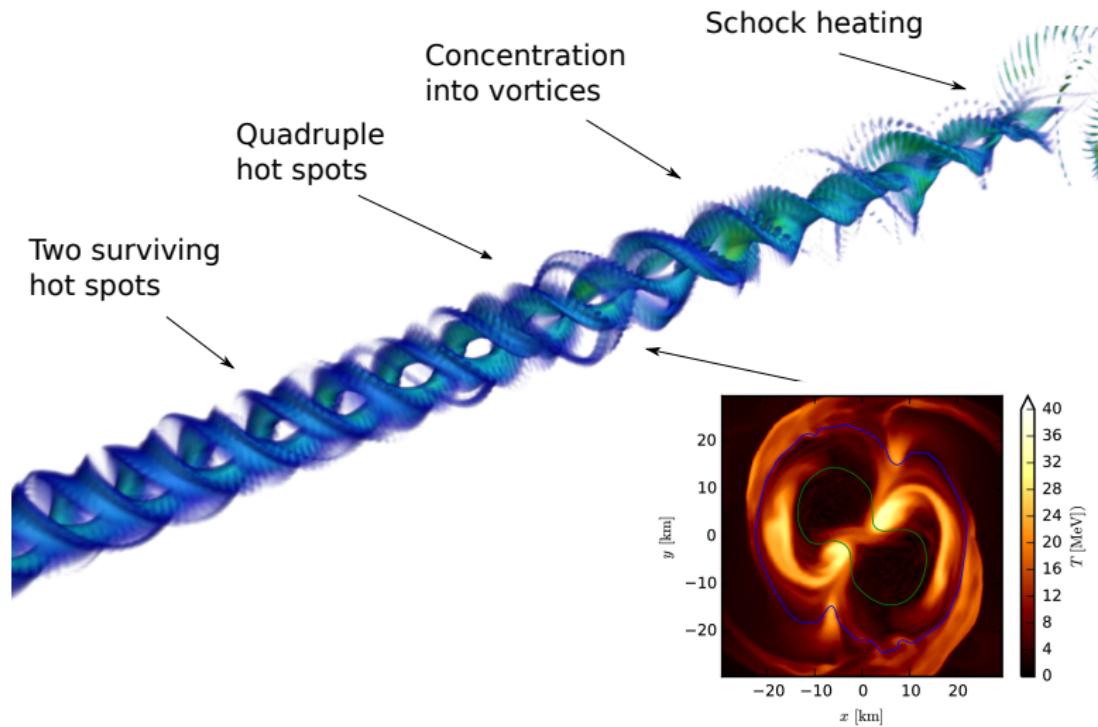
# Thermal evolution



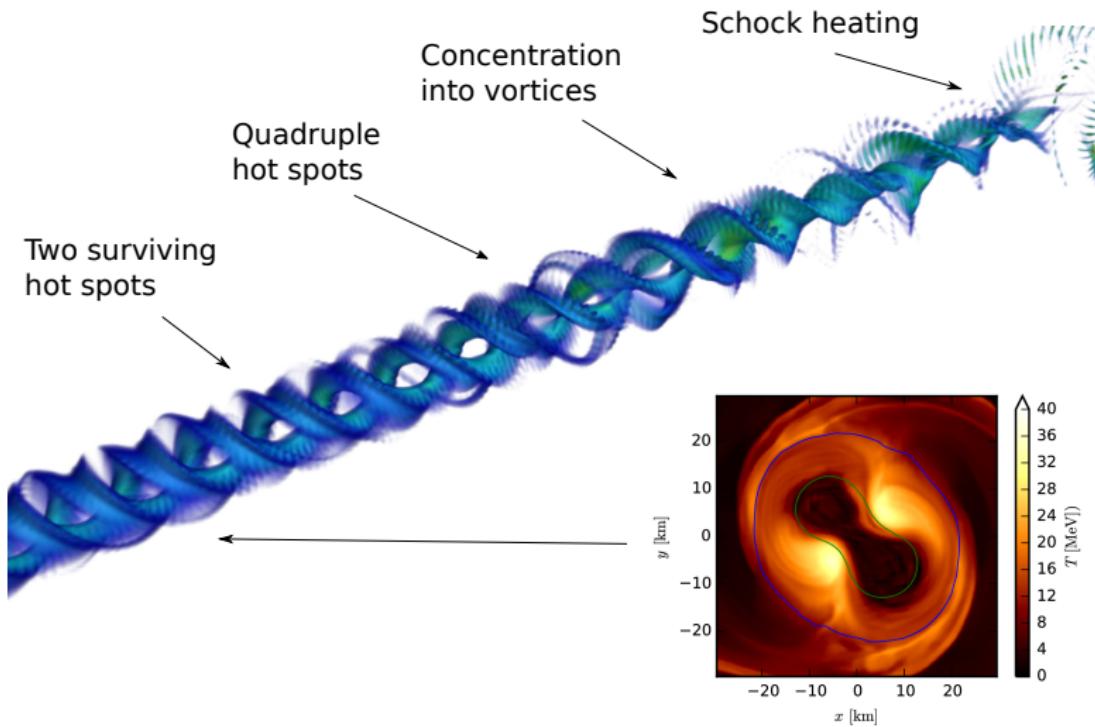
# Thermal evolution



# Thermal evolution

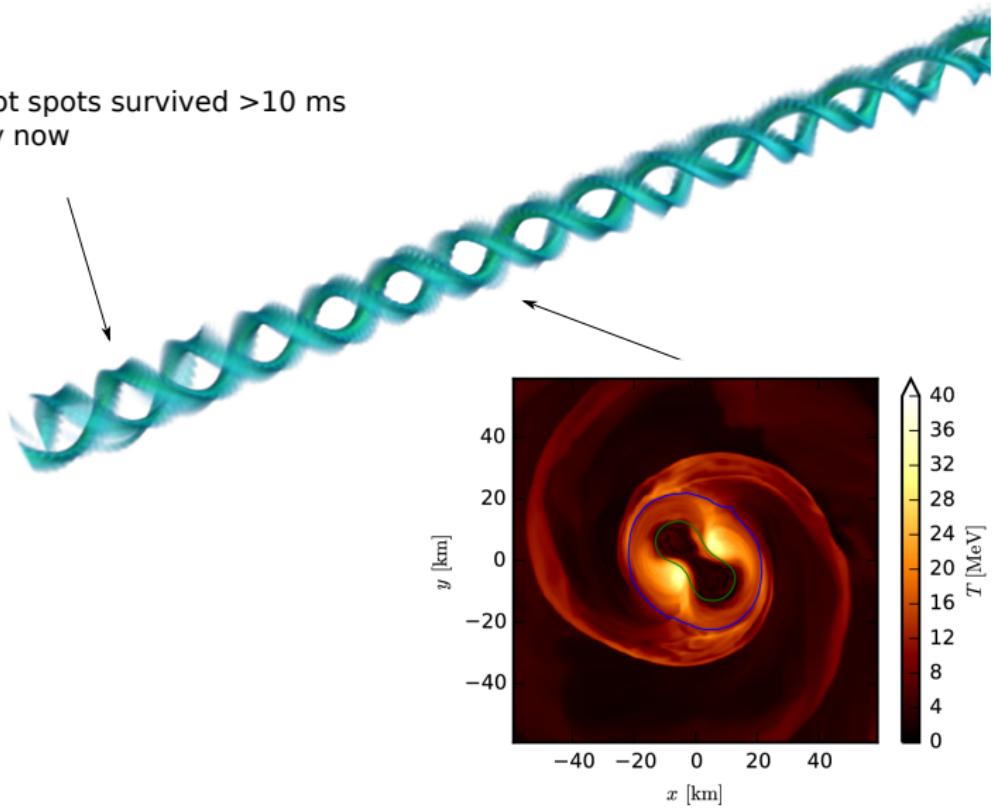


# Thermal evolution



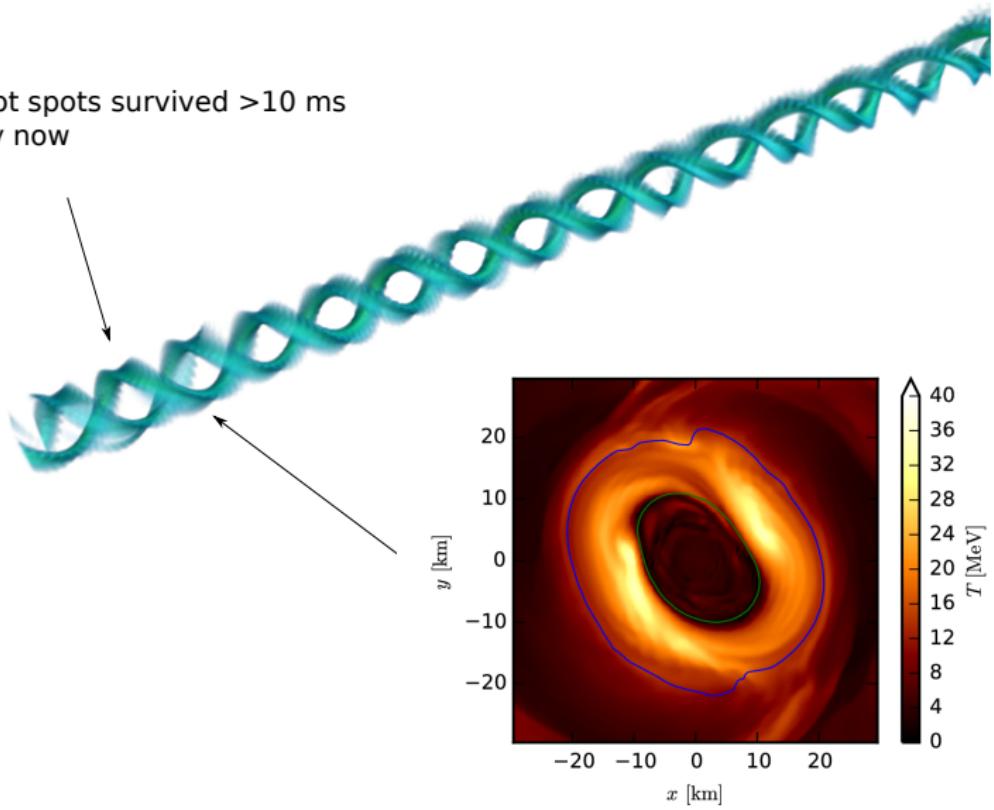
# Thermal evolution

Hot spots survived >10 ms  
by now

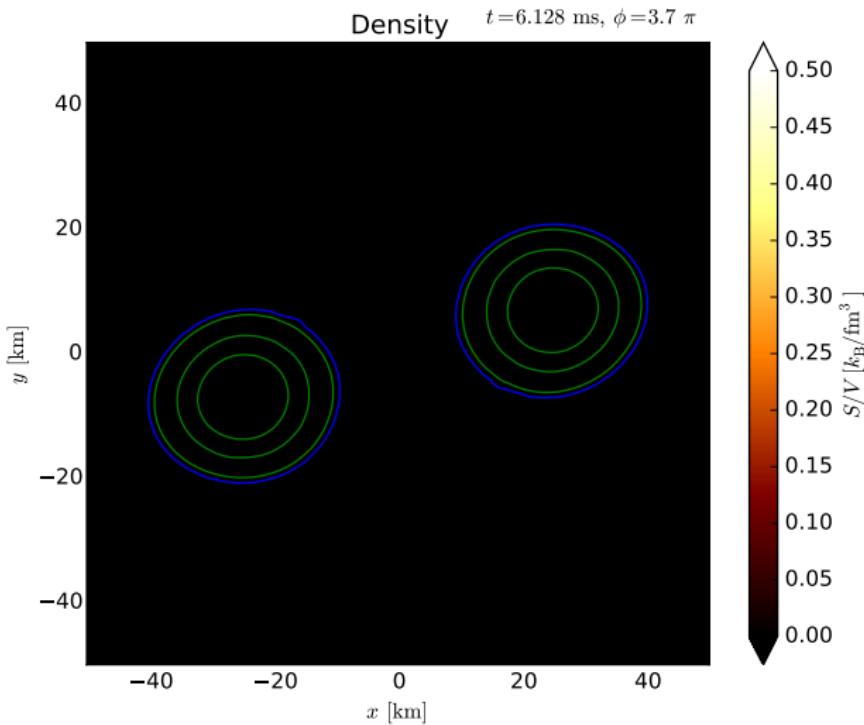


# Thermal evolution

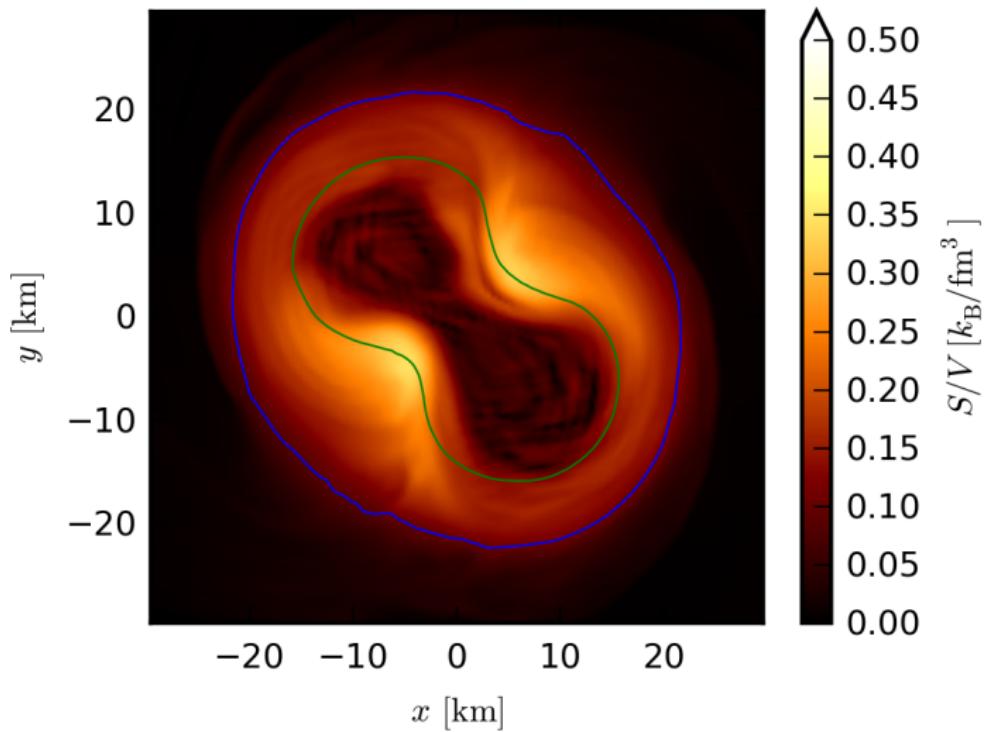
Hot spots survived >10 ms  
by now



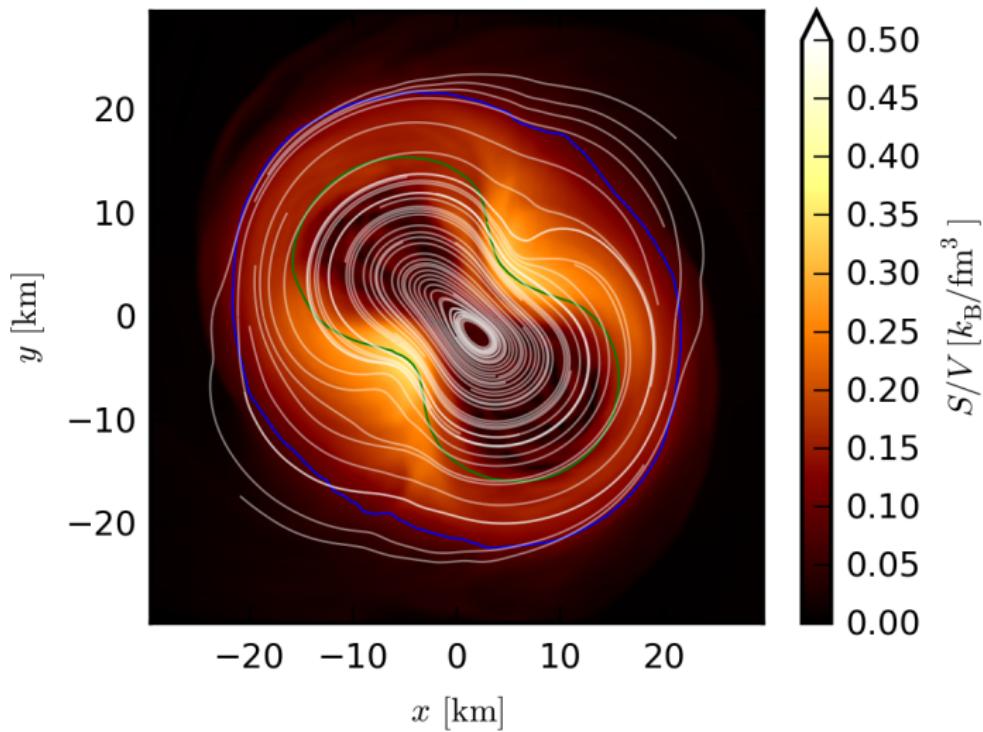
# Thermal evolution



# Thermal evolution

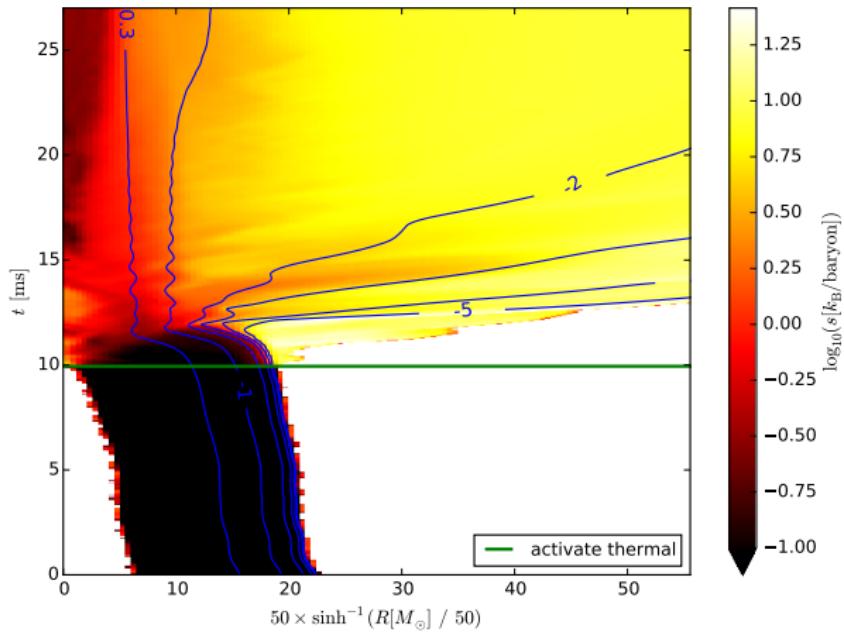


# Thermal evolution



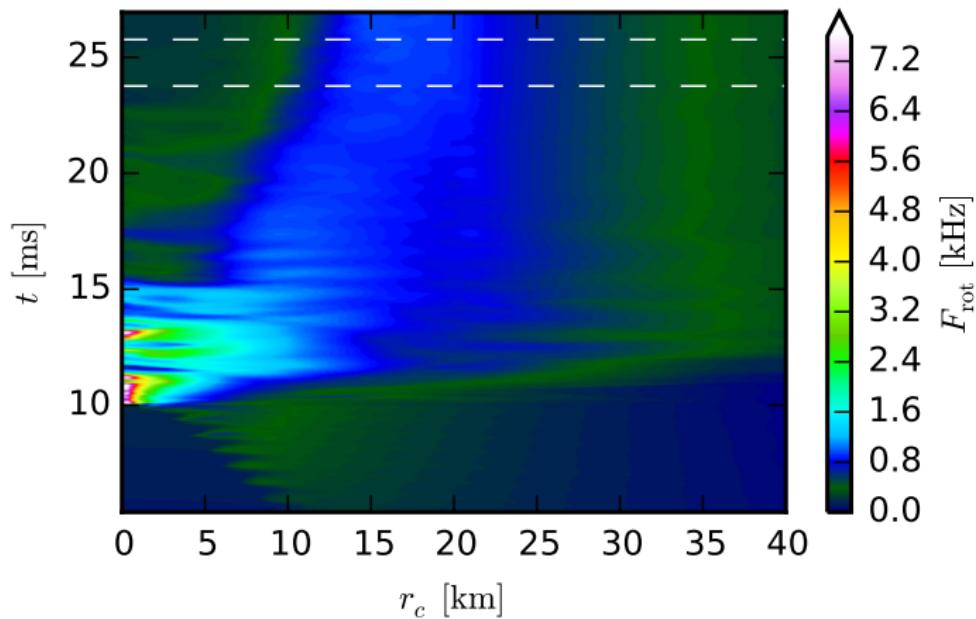
# Thermal evolution

- ▶ Final state convectively stable
- ▶ Evolve adiabatically during inspiral



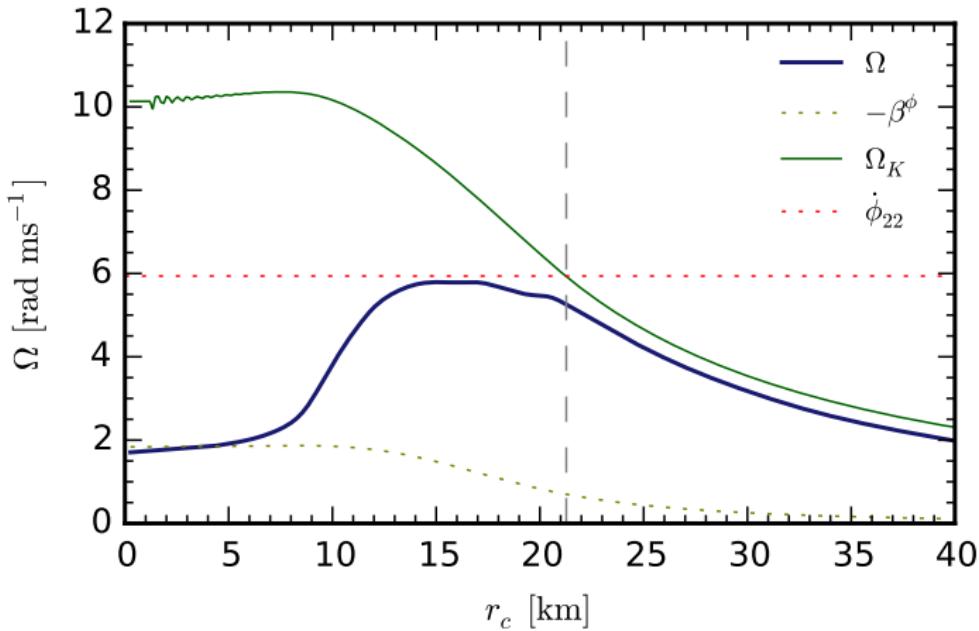
## Rotation profile

- ▶ Violent rearrangement of rotation profile after merger



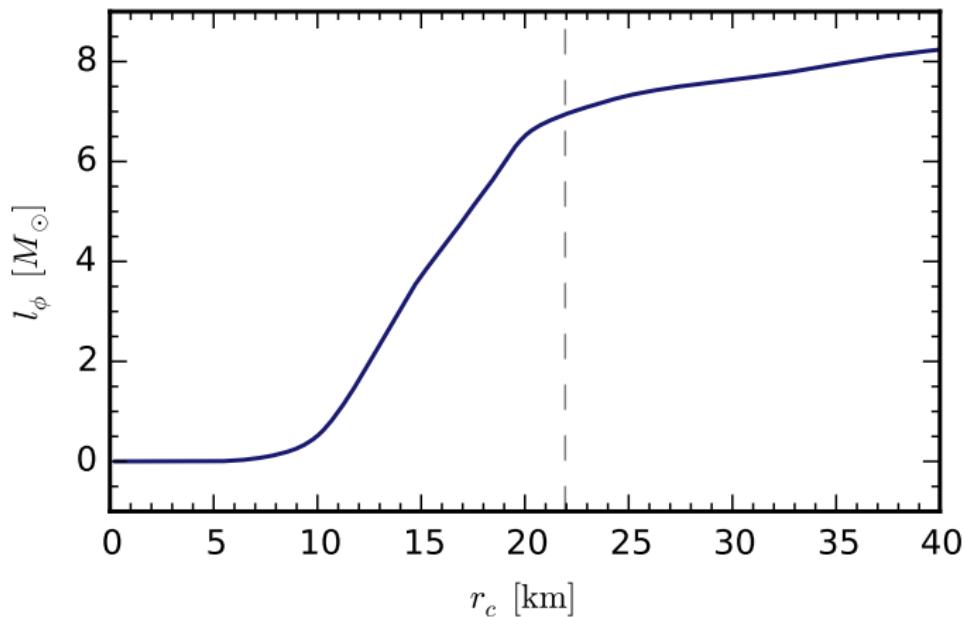
## Rotation profile

- ▶ Remnant rotation profile has slowly rotating core
- ▶ Outer layers close to Kepler rate



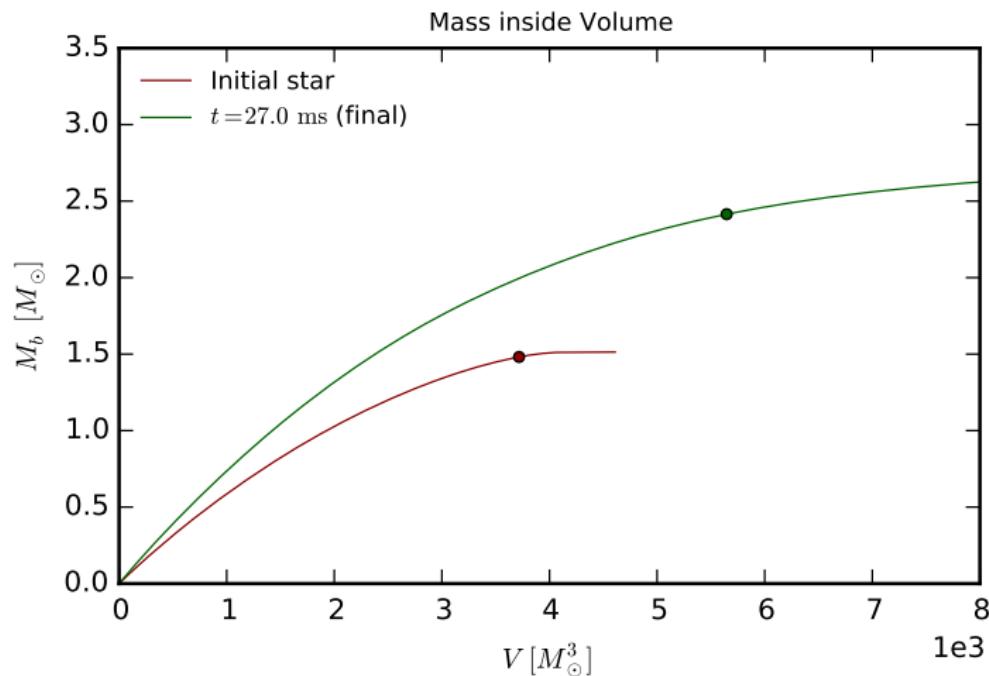
## Rotation profile

- ▶ Final specific angular momentum profile stable
- ▶ Specific entropy profile adds even more stability



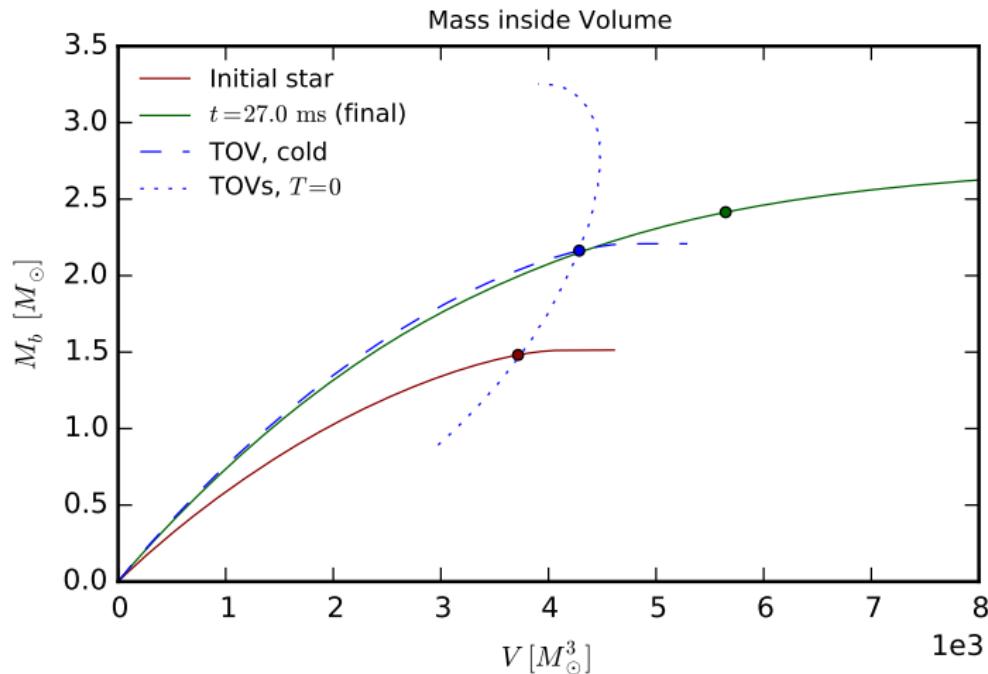
## Remnant mass distribution

- Central region of remnant very similar to a TOV star



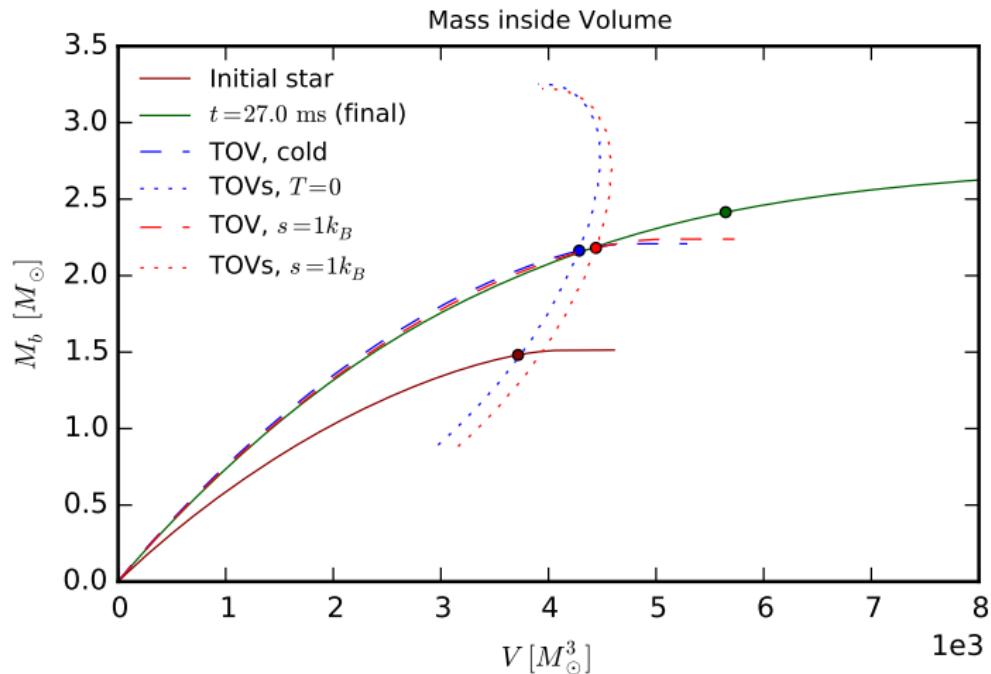
## Remnant mass distribution

- ▶ Central region of remnant very similar to a TOV star
- ▶ Define TOV core equivalent by matching bulk properties



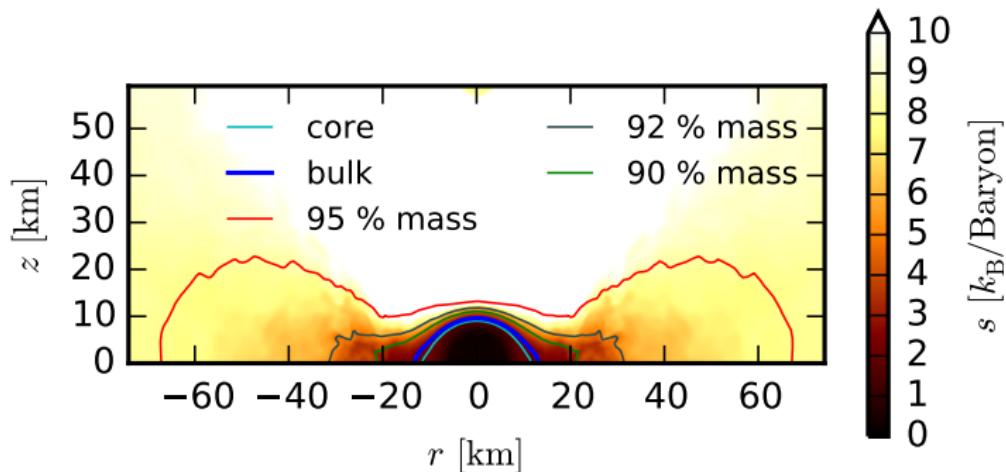
# Remnant mass distribution

- ▶ Central region of remnant very similar to a TOV star
- ▶ Define TOV core equivalent by matching bulk properties



## Remnant mass distribution

- ▶ Bulk baryonic mass  $2.4 M_{\odot}$
- ▶ TOV core equivalent mass  $2.2 M_{\odot}$
- ▶ Mass outside bulk (Envelope+Disk)  $0.62 M_{\odot}$
- ▶ Mass at  $r > 20$  km (Disk)  $0.3 M_{\odot}$



## Measuring matter ejection

Previous estimate for unbound mass

- ▶ Assume stationary spacetime
- ▶ Assume fluid moves along geodesics
- ▶ Compute volume integral of “unbound” mass

# Measuring matter ejection

Previous estimate for unbound mass

- ▶ Assume stationary spacetime
- ▶ Assume fluid moves along geodesics
- ▶ Compute volume integral of “unbound” mass

Problem

- ▶ Patently wrong close to remnant
- ▶ Too far from remnant matter diluted below cut-off

# Measuring matter ejection

Previous estimate for unbound mass

- ▶ Assume stationary spacetime
- ▶ Assume fluid moves along geodesics
- ▶ Compute volume integral of “unbound” mass

Problem

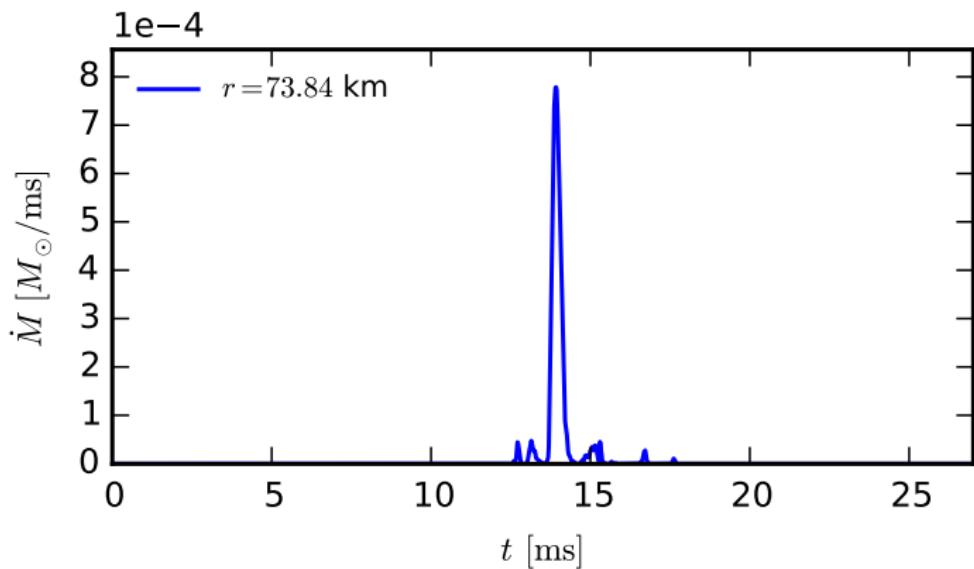
- ▶ Patently wrong close to remnant
- ▶ Too far from remnant matter diluted below cut-off

Solution

- ▶ Use flux of unbound baryonic mass through spherical shell
- ▶ Also compute flux of entropy, electron fraction

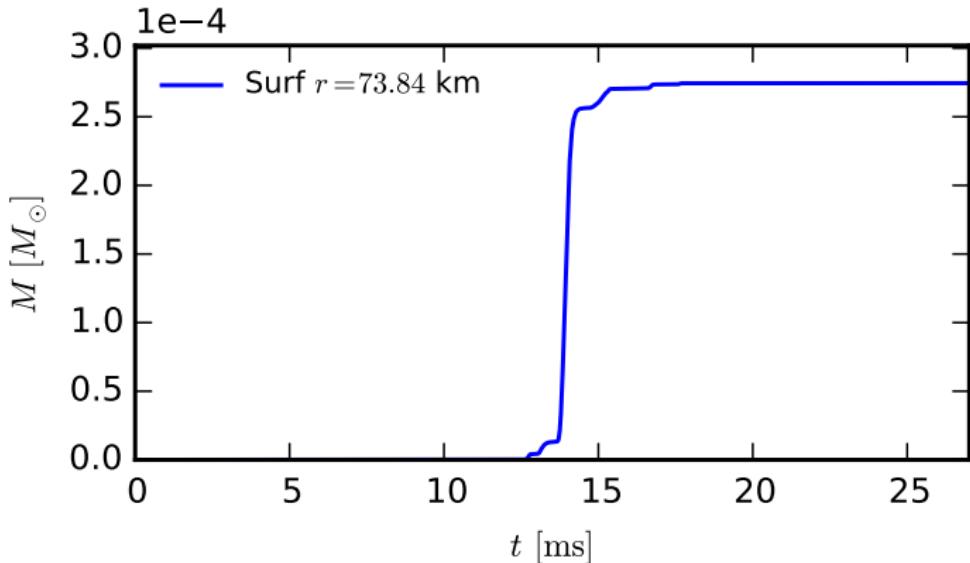
## Matter Ejection

- One wave, launched at merger, escape velocity  $\approx 0.17 c$



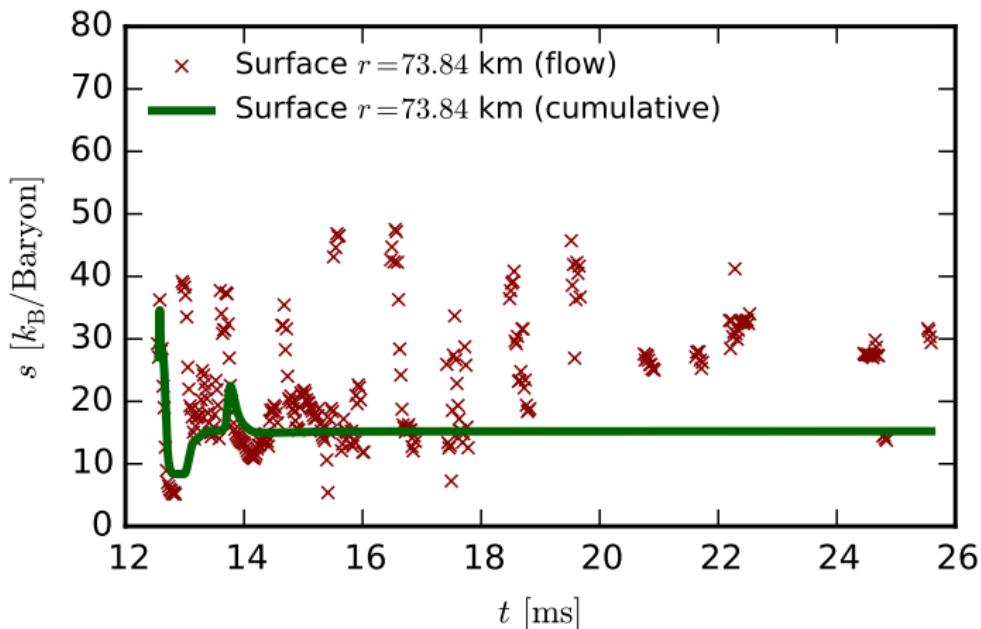
## Matter Ejection

- ▶ One wave, launched at merger, escape velocity  $\approx 0.17 c$
- ▶ Relatively low amount of unbound matter



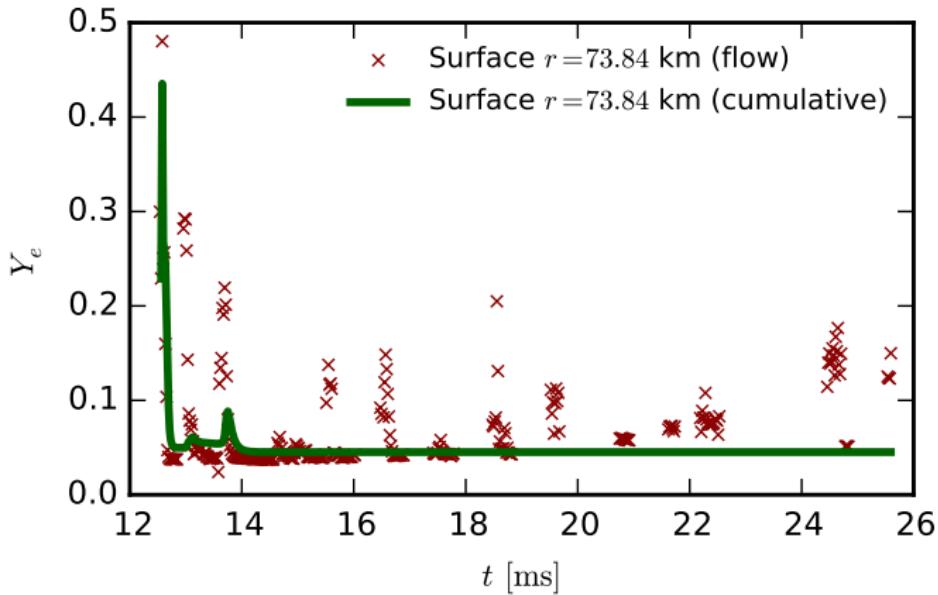
# Matter Ejection

- ▶ One wave, launched at merger, escape velocity  $\approx 0.17 c$
- ▶ Relatively low amount of unbound matter
- ▶ Average specific entropy  $\approx 15 k_B/\text{Baryon}$



# Matter Ejection

- ▶ One wave, launched at merger, escape velocity  $\approx 0.17 c$
- ▶ Relatively low amount of unbound matter
- ▶ Average specific entropy  $\approx 15 k_B/\text{Baryon}$
- ▶ Electron fraction (not accurate without neutrino radiation)



## Spin – Initial data

Lattimer-Swesty ( $K = 220$  MeV) EOS

Equal mass,  $M_B = 3.12 M_\odot = 1.10 M_{\text{Kepler}}$

Irrational

Aligned rotation  
 $\Delta F_R \approx 160$  Hz

G. Shen, Horowitz, Teige (NL3) EOS

Equal mass,  $M_B = 4.01 M_\odot = 1.01 M_{\text{Kepler}}$

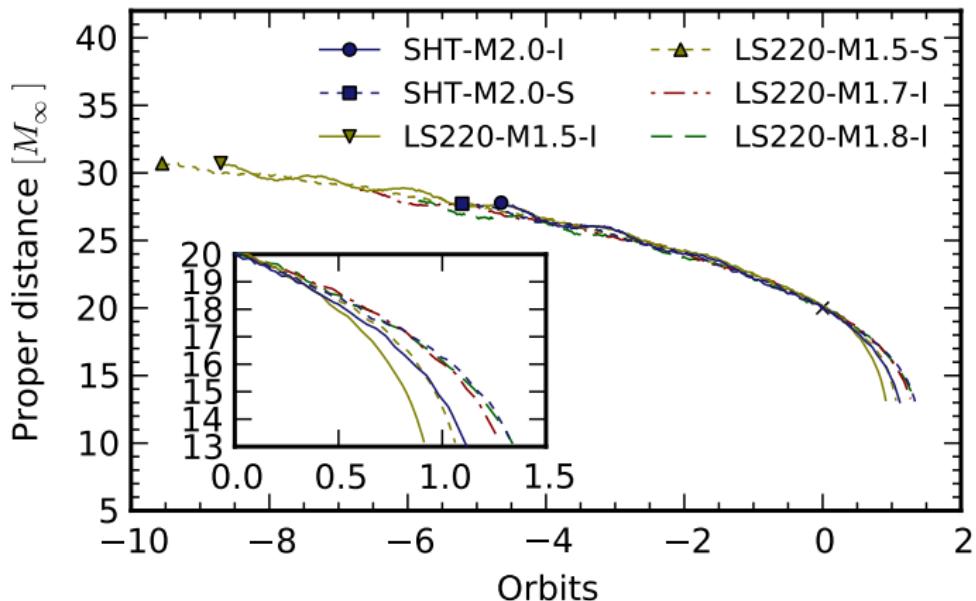
Irrational

Aligned rotation  
 $\Delta F_R \approx 155$  Hz

W. Kastaun, F. Galeazzi, *Properties of hypermassive neutron stars formed in mergers of spinning binaries*, Phys. Rev. D 91, 064027 (2015)

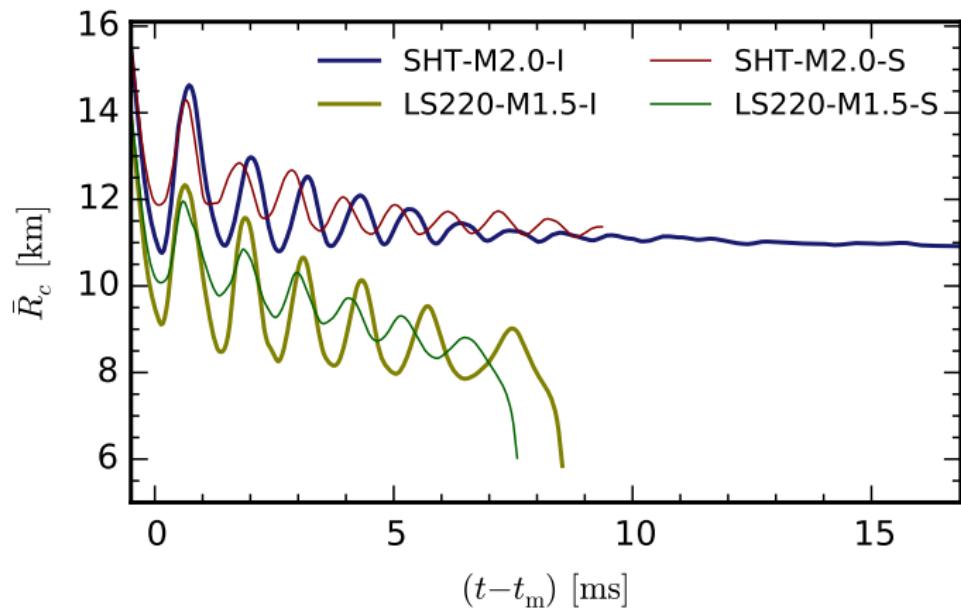
# Spin – Inspiral

- ▶ Inspiral takes longer with spin
- ▶ Different impact trajectory



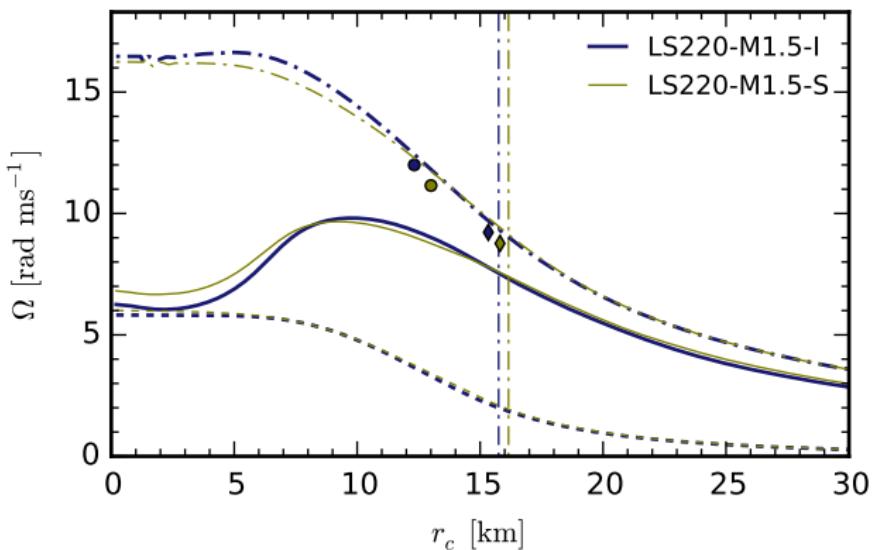
# Spin – Radial Oscillations

- ▶ Strong quasi-radial oscillation
- ▶ Oscillation amplitude smaller for spinning NSs



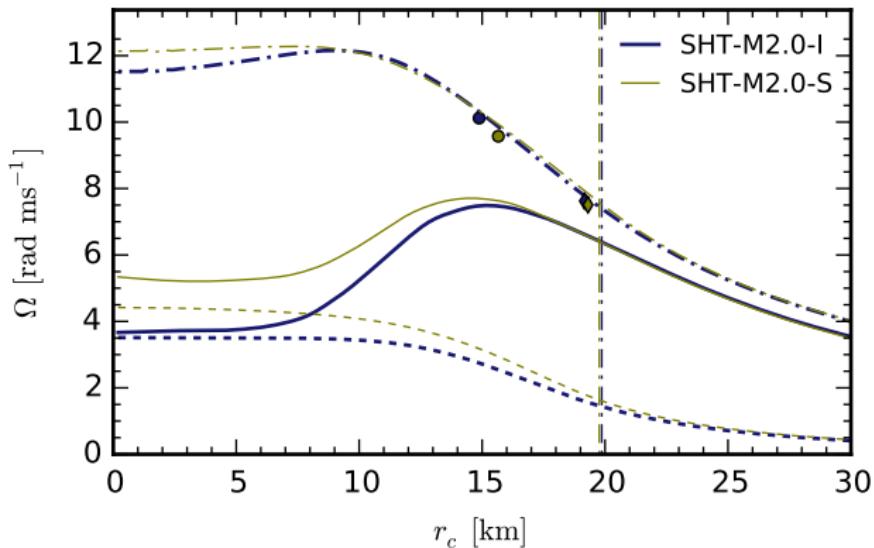
# Spin – Rotation Profile

- ▶ Average rotation rate has central dip again



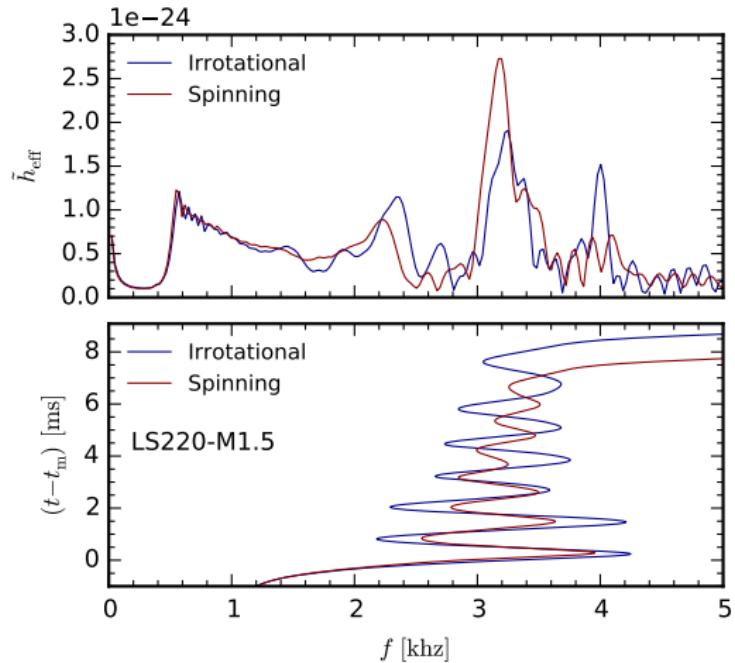
## Spin – Rotation Profile

- ▶ Average rotation rate has central dip again
- ▶ Influence of initial spin varies



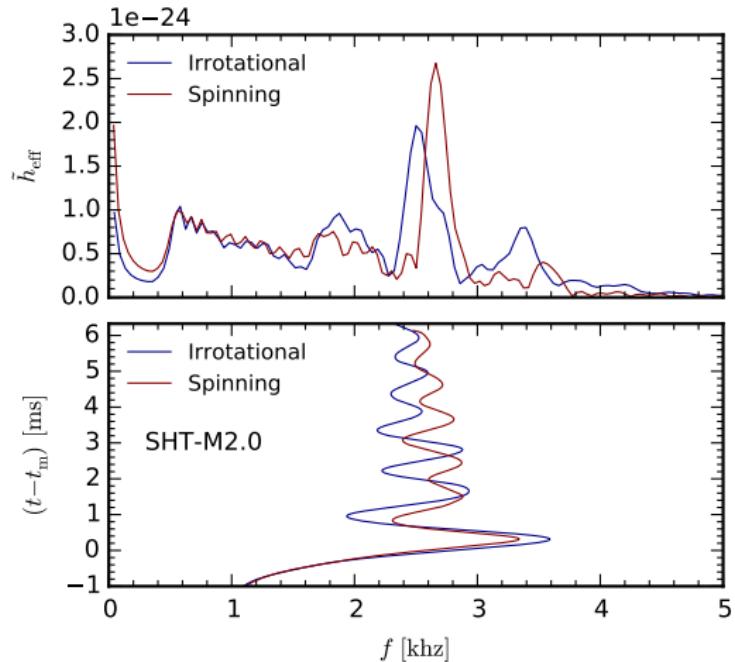
# Spin – GW Spectrum

- ▶ No clear spin signature in post-merger spectra
- ▶ Better chances for inspiral+plunge



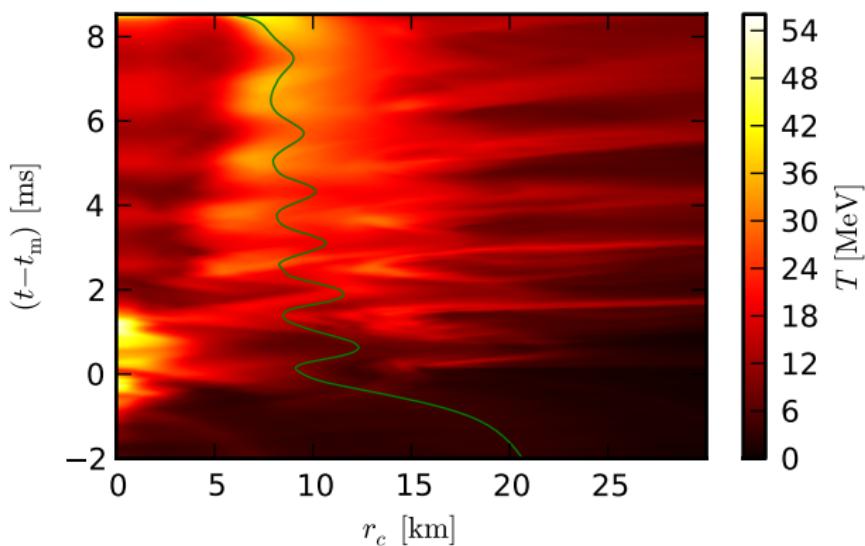
# Spin – GW Spectrum

- ▶ No clear spin signature in post-merger spectra
- ▶ Better chances for inspiral+plunge



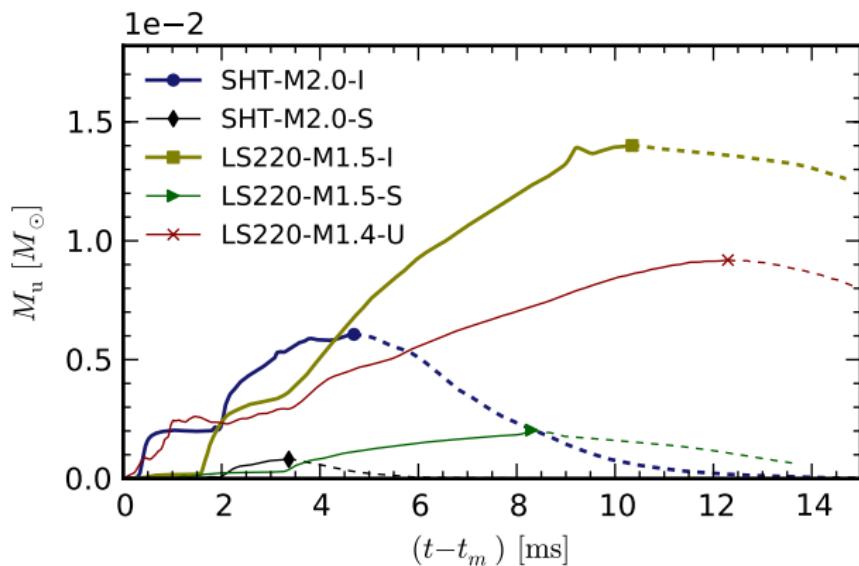
## Spin – Matter ejection

- ▶ Matter ejected in spiral waves caused by  $m = 2$  mode.
- ▶ Modulated by radial oscillation.



## Spin – Matter ejection

- ▶ Matter ejected in spiral waves caused by  $m = 2$  mode.
- ▶ Modulated by radial oscillation.
- ▶ Initial spin influences amount of ejected matter.



## Summary

- ▶ Merger remnant cores rotate slowly
- ▶ Thermal effects unimportant for core profile
- ▶ Outer envelope supported mainly by centrifugal force
- ▶ New measure: Mass versus volume relation
- ▶ Observed dynamic hot spots,  
resilient to differential rotation
- ▶ Spin seems to influence matter ejection
- ▶ Weak and complicated influence on GW

Thanks!