Simulating Black Hole White Dwarf Encounters

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Abstract

The existence of supermassive black holes lurking in the centers of galaxies and of stellar binary systems containing a black hole with a few solar masses has been established beyond reasonable doubt. The idea that black holes of intermediate masses (~ 1000 M_{\odot}) may exist in globular star clusters has gained credence over recent years but no conclusive evidence has been established yet. An attractive feature of this hypothesis is the potential to not only disrupt solar-type stars but also compact white dwarf stars. In close encounters the white dwarfs can be sufficiently compressed to thermonuclearly explode. The detection of an underluminous thermonuclear explosion accompanied by a soft, transient X-ray signal would be compelling evidence for the presence of intermediate mass black holes in stellar clusters. In this paper we focus on the numerical techniques used to simulate the entire disruption process from the initial parabolic orbit, over the nuclear energy release during tidal compression, the subsequent ejection of freshly synthesized material and the formation process of an accretion disk around the black hole.

Key words: meshfree Lagrangian hydrodynamics, nuclear reactions, reactive flows, black holes *PACS:*

1 Introduction

The existence of two classes of black holes is well-established: supermassive black holes with masses beyond $10^6 M_{\odot}$ are thought to lurk in the centers

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of most galaxies[23] and black holes with just a few solar masses have been identified as the unseen components in X-ray binary systems[12]. Black holes with $M_{\rm bh} \sim 1000 \,\mathrm{M}_{\odot}$, so-called "intermediate mass black holes", represent a plausible, but so far still unconfirmed "missing link" between these two wellestablished classes of black holes. In recent years, the stellar dynamics in the centers of some globular clusters has been interpreted as being the result the gravitational interaction with an intermediate mass black hole[6,8,9,7]. Further circumstantial evidence comes from ultraluminous, compact X-ray sources in young star clusters[35,21] and from n-body simulations[22] that indicate that runaway collisions in dense young star clusters can lead to rapidly growing black holes. None of these arguments is conclusive by itself, but their different nature suggests that the possibility of intermediate mass black holes must be taken seriously.

The tidal disruption of white dwarfs offers the unique possibility to explore the presence of an intermediate mass black hole. The corresponding disruption processes have been explored with various approximations in earlier studies [14,34,5], our simulations for the first time explore the full evolution from the initial parabolic orbit over the disruption process to the subsequent build-up of an accretion disk. We have performed a large set of calculations to identify observational signatures that can corroborate or, alternatively, rule out the existence of intermediate mass black holes. In this paper we focus on the numerical techniques that have been employed in this disruption study, a detailed discussion of the astrophysical implications will be given elsewhere[27,28].

2 Numerical methods

The simulation of a white dwarf disruption by a black hole needs to follow the gas dynamics from the initial spherical star through the distortion and compression while approaching the black hole to the subsequent expansion phase and the formation of an accretion disk. Of paramount importance for the dynamical evolution is the inclusion of the feedback from the nuclear reactions that are triggered by the tidal compression. In the following we will briefly sketch the methods employed in our simulations.

Hydrodynamics

Due to the highly variable geometry and the importance of the strict numerical conservation of physically conserved quantities, we use the smoothed particle hydrodynamics method (SPH) to discretize the equations of an ideal fluid. Using the SPH approximations[3,18] the conservation of mass, momentum and energy translate into

$$\rho_a = \sum_b m_b W_{ab} \tag{1}$$

$$\frac{d\vec{v}_a}{dt} = -\sum_b m_b \left\{ \frac{P_a}{\rho_a^2} + \frac{P_b}{\rho_b^2} + \Pi_{ab} \right\} \nabla_a W_{ab} + \vec{f}_{a,\text{grav}}$$
(2)

$$\frac{du_a}{dt} = \frac{P_a}{\rho_a^2} \sum_b m_b \vec{v}_{ab} \nabla_a W_{ab} + \frac{1}{2} \sum_b m_b \Pi_{ab} \vec{v}_{ab} \nabla_a W_{ab} + \dot{\epsilon}_{\text{nuc,a}}.$$
(3)

Here ρ_a is the density at the position of particle a, m_b the (constant) mass of particle $b, W_{ab} = W(|\vec{r_a} - \vec{r_b}|, h_{ab})$ the cubic spline kernel[15] with compact support whose width is set by the average of the smoothing lengths of particle a and $b, h_{ab} = (h_a + h_b)/2$. P_a refers to the gas pressure, $\vec{f_{a,grav}}$ to the gravitational acceleration of particle a and Π_{ab} is the artificial viscosity tensor, see below, and $\vec{v_{ab}} = \vec{v_a} - \vec{v_b}$ with \vec{v} being the particle velocity. The quantity u_a is the specific internal energy of particle $a, \dot{\epsilon}_{nuc,a}$ is the thermonuclear energy generation, calculated in a operator split fashion as described below. Since SPH is a Lagrangian method, and we ignore mixing, the compositional evolution is a local phenomenon.

In cases where the geometry of the gas distribution varies substantially, it is advisable to adapt the local resolution, i.e. the smoothing length, according to the changes in the matter density. We achieve this by scaling the smoothing length with the density according to

$$\frac{h_a(t)}{h_{a,0}} = \left(\frac{\rho_{a,0}}{\rho_a(t)}\right)^{1/3},\tag{4}$$

where the index 0 labels the quantities at the beginning of the simulation. The initial smoothing lengths are chosen so that each particle has 100 neighbors¹. Taking the Lagrangian time derivative of both sides of Eq. (4) and using the Lagrangian form of the continuity equation, one finds an evolution equation for the smoothing length of each particle:

$$\frac{dh_a}{dt} = \frac{1}{3}h_a(\nabla \cdot \vec{v})_a, \quad \text{where} \quad (\nabla \cdot \vec{v})_a = -\frac{1}{\rho_a}\sum_b m_b \vec{v}_{ab} \nabla_a W_{ab}. \tag{5}$$

This equation is integrated together with the other ODEs required for hydrodynamics, Eqs. (2), (3), (6), and possible changes in the abundances in the case of nuclear reactions. During the integration the resulting new neighbor number is constantly monitored for each particle and, if necessary, an iteration of the smoothing length is performed to keep the neighbor number in the desired range of between 80 and 120.

¹ A "neighbor" is a particle b that yields a non-zero contribution to sums in Eqs. (1)-(3).



Fig. 1. Sod shock tube problem in 1D: the exact solution is given by the solid line, the numerical result is shown by the circles. In the lower left panel (pressure) the value of the time dependent artificial viscosity parameter α is overlaid. It is to be compared with the commonly used value $\alpha = 1 = \text{const.}$

The SPH equations derived from a Lagrangian[31,17] yield different symmetries in the particle indices and additional multiplicative factors with values close to unity, but a recent comparison[29] between these two sets of equations showed only very minor differences in practical applications.

We use the artificial viscosity tensor in the form given in [16], but with the following important modifications: i) the viscosity parameters α and β (commonly set to constants $\alpha = 1$, $\beta = 2$) are replaced by $\alpha \rightarrow \tilde{\alpha}_{ab} =$ $(\alpha_a + \alpha_b)(f_a + f_b)/4$, $\beta \rightarrow 2\tilde{\alpha}_{ab}$, where f_k is the so-called Balsara-switch[2] to suppress spurious forces in pure shear flows, and ii) the viscosity parameter α_k is determined by evolving an additional equation[19] with a decay and a source term[26]:

$$\frac{d\alpha_a}{dt} = -\frac{\alpha_a - \alpha_{\min}}{\tau_a} + S_a \quad \text{with} \quad S_a = \max\left[-(\vec{\nabla} \cdot \vec{v})_a(\alpha_{\max} - \alpha_a), 0\right].$$
(6)

In the absence of shocks α decays to α_{\min} on a time scale $\tau_a = h_a/(0.1 c_a)$, where c_a is the sound velocity. In a shock α rises rapidly to capture the shock properly. A further discussion of this form of artificial viscosity can be found in [25].

To demonstrate the ability of this scheme to capture shocks without spurious post-shock oscillations we show in Fig. 1 the results of a standard, onedimensional Sod shock tube test[30] (with a polytropic gas of adiabatic exponent $\Gamma = 1.4$) at t=0.17. For this test we used 1000 SPH particles, $\alpha_{\text{max}} = 1.5$ and $\alpha_{\text{min}} = 0.1$. The numerical solution (circles) agrees excellently with the exact solution (solid line), the shock itself is spread over about 10 particles. In the third panel ("pressure") we have overlaid the value of the viscosity parameter α . It deviates substantially from its minimum value only in the direct vicinity of the shock where it reaches values of about 1.3. This is to be compared to the "standard" values $\alpha = 1$ and $\beta = 2$ that are commonly applied in astrophysical simulations to each particle irrespective of the necessity to resolve a shock. This scheme has been shown[26,25] to minimize possible artifacts due to artificial viscosity.

Note that no efforts have been made to include the effects of heat transport. Therefore, deflagration-type combustion cannot be handled adequately with the current code. As will be discussed below, deflagration is of no importance for the disruption processes that we discuss here.

Equation of state

The system of fluid equations (1), (2) and (3) needs to be closed by an equation of state (EOS) that is appropriate for white dwarf matter. We use the HELMHOLTZ EOS developed by the Center for Astrophysical Thermonuclear Flashes at the University of Chicago. It accepts an externally calculated nuclear composition which facilitates the coupling to reaction networks. The ions are treated as a Maxwell-Boltzmann gas, for the electron/positron gas the exact expressions are integrated numerically (i.e. no assumptions about the degree of degeneracy or relativity are made) and the result is stored in a table. A sophisticated, biquintic Hermite polynomial interpolation is used to enforce the thermodynamic consistency at interpolated values[33]. The photon contribution is treated as blackbody radiation. The EOS covers the density range form $10^{-10} \leq \rho Y_e \leq 10^{11}$ g cm⁻³ (Y_e being the electron fraction²) and temperatures from 10^4 to 10^{11} K.

Gravity

The self-gravity of the fluid is calculated via a parallel version of the binary tree described in [4]. The same tree is used to search for the neighbor particles that are required for the density estimate, Eq. (1), and the gradients in Eqs. (2), (3) and (5). The gas acceleration due to a (Schwarzschild) black hole is treated in the Paczyński-Wiita approximation[20]. This approach has been shown[1] to yield accurate results for the accretion onto non-rotating black holes. To avoid numerical problems due to the singularity at the Schwarzschild radius the pseudo potential is smoothly extended in a non-singular way down to the hole[24] with an absorbing boundary placed at a distance of $3GM_{\rm bh}/c^2$ from the black hole with mass $M_{\rm bh}$.

² In the presence of electron-positron pairs it is given by $Y_e = \frac{n_{e^-} - n_{e^+}}{\rho N_A}$, where n_{e^-}/n_{e^+} are the number densities of electrons/positrons.

A minimal nuclear reaction network

To address whether tidal compression can trigger a thermonuclear explosion, we need to evolve the nuclear composition and to include the feedback onto the gas from the energy released by nuclear burning. Running a full nuclear network with hundreds of species for each SPH particle would be computationally prohibitive, therefore a "minimal" network designed to provide the accurate energy generation[10,32] is used. It couples a conventional α -network stretching from He to Si with a quasi-equilibrium-reduced α -network. The QSE-reduced network neglects reactions within small equilibrium groups that form at temperatures above 3.5 GK to reduce the number of abundance variables needed. Although a set of only seven nuclear species is used, this network reproduces all burning stages from He-burning to nuclear statistical equilibrium accurately. For more details and tests we refer to [10].

In the presence of nuclear reactions the energy produced (or consumed) by nuclear reactions is given by

$$\dot{\epsilon}_{\rm nuc,a} = N_{\rm A} \sum_{j} B_j \frac{dY_{j,a}}{dt},\tag{7}$$

where $N_{\rm A}$ is Avogadro's number, B_j is the nuclear binding energy of the nucleus j, $Y_{j,a} = n_{j,a}/(\rho_a N_{\rm A})$ its abundance and $n_{j,a}$ is the number density of species j. Again, the subscript a indicates that these quantities are evaluated at the position of particle a.

Since the nuclear reaction and the hydrodynamic time scales can differ by many orders of magnitude, the network is coupled to the hydrodynamics in an operator splitting fashion. In a first step, Eqs. (2),(3),(5),(6) are integrated forward in time via a MacCormack predictor-corrector scheme[13] with individual time steps[29] to obtain new quantities at time t^{n+1} . In this step we ignore the nuclear source term in Eq. (3), the result is denoted by \tilde{u}_a^{n+1} . This value has to be corrected for the energy release that occurred from t^n to t^{n+1} :

$$\epsilon_{a,n \to n+1} = N_{\rm A} \sum_{j} B_{j} \int_{t^n}^{t^{n+1}} \frac{dY_{j,a}}{dt} (\rho_a(t), T_a(t), Y_{k,a}(t)) dt$$
(8)

$$=N_A \sum_{j=1}^{n} B_j (Y_{j,a}^{n+1} - Y_{j,a}^n),$$
(9)

where $\rho_a(t) \approx \rho_a(t^n) + \frac{t-t^n}{t^{n+1}-t^n} \{\rho_a(t^{n+1}) - \rho_a(t^n)\}$ and $T_a(t) \approx T_a(t^n)$ has been used to integrate the abundances $Y_{j,a}$ via the implicit backward Euler method (the network integration is described in detail in[10]). The final value for the specific energy at time t^{n+1} is given by

$$u_a^{n+1} = \tilde{u}_a^{n+1} + \epsilon_{a,n \to n+1}.$$
 (10)



Fig. 2. Comparison of nuclear energy produced (from an initial pure He composition) and the energy lost via various neutrino reactions during 1 s (the typical pericentre passage time, see Fig. 3). The thick solid line that starts at about $\log(T) = 9.1$ and ends at about $\log(T) = 8.3$ shows the trajectory of the hottest 10% of the particles of the simulation shown in Fig. 3). To see clearly where neutrino emission becomes dominant, we have also thickened the contour where nuclear and neutrino contributions are equal.

Now the EOS is called again to make all thermodynamic quantities consistent with this new value u_a^{n+1} . Once the derivatives have been updated, the procedure can be repeated for the next time step.

For the hydrodynamic time step we use the minimum of several criteria. We use a force criterion and a combination of Courant-type and viscosity-based criterion[16]

$$\Delta t_{f,a} = \sqrt{h_a/|\vec{f_a}|}$$
 and $\Delta t_{C,a} = \frac{h_a}{v_{s,a} + 0.6(v_{s,a} + 2\max_b \mu_{ab})},$ (11)

where f_a is the acceleration, $v_{s,a}$ is the sound velocity and μ_{ab} a quantity used in the artificial viscosity tensor (for its explicit form see [16]). To ensure a close coupling between hydrodynamics and nuclear reactions in regions where burning is expected, we apply two additional time step criteria. One triggers on matter compression, the other on the distance to the black hole:

$$\Delta t_{\rm comp,a} = -0.03/(\nabla \cdot \vec{v})_a \quad \text{and} \quad \Delta t_{\rm bh,a} = 0.03/\sqrt{GM_{\rm bh}/r_{\rm bh,a}^3}.$$
 (12)

The "desired" hydro time step of each particle is then chosen as $\Delta t_{\text{des},a} = 0.2 \min(\Delta t_{f,a}, \Delta t_{C,a}, \Delta t_{\text{comp},a}, \Delta t_{\text{bh},a})$. How these desired time steps are transformed into the individual block time steps is explained in detail in[29]. As a test, low-resolution versions of the production runs were run once with this



Fig. 3. Tidal disruption of a 0.2 M_{\odot} He white dwarf by a 1000 M_{\odot} black hole (located at the origin).

time step prescription and once with halved time steps. No noticeable differences could be found.

One may wonder whether neutrino emission could subduct substantial amounts of energy during the burning phase. To test for this, we have plotted in Fig. 2 the ratio of the nuclear energy produced and the energy lost to neutrinos within a typical pericentre passage of 1 s duration. For the neutrino emission pair annihilation, plasma, photoneutrino, bremsstrahlung and recombination processes were considered according to the fit formulae of [11] as coded by F. Timmes³. For the conditions relevant to this study neutrino emission was never relevant.

3 Results

As initial condition we set up a white dwarf on a parabolic orbit around the black hole with an initial separation of several tidal radii $R_{\rm tid} = R_{\rm WD} \left(\frac{M_{\rm bh}}{M_{\rm WD}}\right)^{1/3}$. In a large set of simulations we explored black hole masses of 100, 500, 1000, 5000 and 10 000 M_{\odot} and white dwarf masses of 0.2, 0.6 and 1.2 M_{\odot}. Each time several "penetration factors", $P = R_{\rm tid}/R_{\rm peri}$, where $R_{\rm peri}$ is the pericentre separation, were explored. To be conservative, we set the initial white dwarfs to very low temperatures ($T_0 = 5 \cdot 10^4$ K). The numerical resolution varied from 500 000 to more than $4 \cdot 10^6$ SPH particles. In all cases we found explosions (nuclear energy release larger than the white dwarf gravitational

³ http://cococubed.asu.edu

binding energy) whenever the penetration factors exceeded values of about 3. Further details of these simulations will be discussed elsewhere [28].

For conciseness we focus here on one exemplary simulation of a 0.2 M_{\odot}, pure He white dwarf (modeled with more than $4 \cdot 10^6$ SPH particles) and a 1000 M_{\odot} black hole, see Fig. 3. The first snapshot (0.12 minutes after the simulation start) shows the stage of maximum white dwarf compression at pericentre passage, in which the white dwarf is also severely compressed perpendicular to the orbital plane. The peak compression occurs at a spatially fixed point (seen as the density peak in Fig. 3, left). The white dwarf fuel is fed with free-fall velocity $v_{\rm ff} = (2GM_{\rm bh}/R_{\rm peri})^{1/2} = 1.6 \cdot 10^5 {\rm km \ s^{-1}} \ (M_{\rm bh}/1000 {\rm M}_{\odot})^{1/2} \ (R_{\rm peri}/10^4 {\rm km})^{-1/2}$ into this compression point. The comparison with typical flame propagation speeds (~ 100 km/s) shows that combustion effects can be safely neglected for this investigation.

During the short compression time (of order one second), the peak density increases by more than one order of magnitude (with respect to the initial, unperturbed star) to $> 6 \cdot 10^5$ g cm⁻³, the peak temperatures get close to nuclear statistical equilibrium (> $3.9 \cdot 10^9$ K). During this stage 0.11 M_{\odot} are burnt, mainly into silicon group (74%), iron group (22.5%) elements and carbon. The nuclear energy release triggers a thermonuclear explosion of the white dwarf. Since a much smaller fraction ends up in iron group nuclei (nickel), this explosion is underluminous in comparison to a normal type I a supernova which produces $\sim 0.5 \,\mathrm{M}_{\odot}$ of nickel. Due to the very different geometry, the lightcurves of such explosions are expected to deviate substantially from standard type Ia light curves. This topic deserves further detailed investigations. About 35 % of the initial stellar mass remain gravitationally bound to the black hole and will subsequently by accreted. During infall, matter trajectories become radially focused towards the pericentre. The large spread in the specific energy across the accretion stream width produces a large spread of apocentric distances and thus a fan-like spraying of the white dwarf debris after pericentre passage. This material interacts with the infalling material in an angular momentum redistribution shock, see Fig. 4, which results in the circularization of the forming accretion disk. The subsequent accretion onto the black hole produces a soft X-ray flare close the Eddington-luminosity for a duration of months.

For other combinations of black hole and white dwarf masses with P > 3 we found a similar behavior. Therefore, an underlumious thermonuclear explosion accompanied by soft X-ray flare may whistle-blow the existence of intermediate mass black holes in globular clusters. The rate of this particular type of explosion amounts to a few tenths of a percent of "standard" type Ia supernovae. Future supernova surveys such as SNF could be able to detect several of these events.

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Fig. 4. Zoom-in on the forming accretion disk. Color-coded is the column density (in g/cm^2), angular momentum is redistributed in the shock that forms when the accretion stream interacts with itself.

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